

# Parton distributions in BSM theories

*for Argonne National Laboratory, April 2023*



**James Moore, University of Cambridge**



# PBSP: Physics Beyond the Standard Proton

- The **PBSP group** is based at the **University of Cambridge**, and is headed by **Maria Ubiali**; the project is **ERC-funded**.
- The aim is to **investigate interplay between BSM physics and proton structure** - the subject of the rest of this talk!
- The team members are:
  - *Postdocs*: Zahari Kassabov, Maeve Madigan, Luca Mantani
  - *PhD students*: Mark Costantini, Shayan Iranipour (*former*), Elie Hammou, **James Moore**, Manuel Morales, Cameron Voisey (*former*)



# Talk overview

**1. PDFs: a lightning introduction**

**2. PDF fitting**

**3. Joint PDF-SMEFT fits**

**4. The SIMUnet methodology**

**5. The top quark legacy of the LHC Run II for PDF and SMEFT analyses**

**6. The dark side of the proton (if time permits...!)**

# 1. - PDFs: a lightning introduction



# Hadron structure through PDFs

- Hadrons are **QCD bound states** - they are **strongly-coupled, non-perturbative** objects.

$$\mathcal{L} = -\frac{1}{4}G_{\mu\nu}^a G^{a,\mu\nu} + \sum_q \bar{q}(i\gamma_\mu D^\mu - m_q)q \longrightarrow \text{hadrons?}$$

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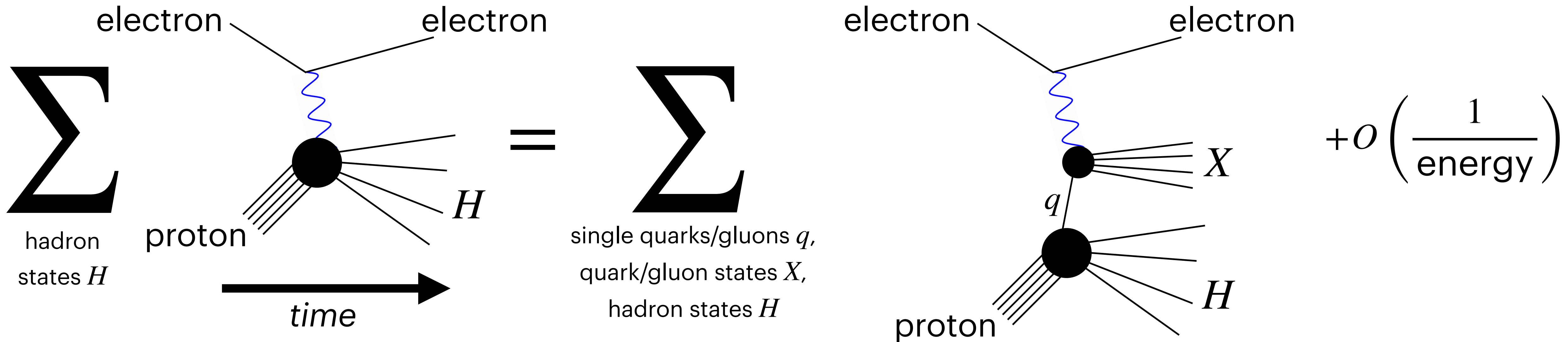
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- But we still want to make predictions for experiments involving hadrons!
- **Solution:** package all non-perturbative elements into unknown functions, called **parton distribution functions (PDFs)**.

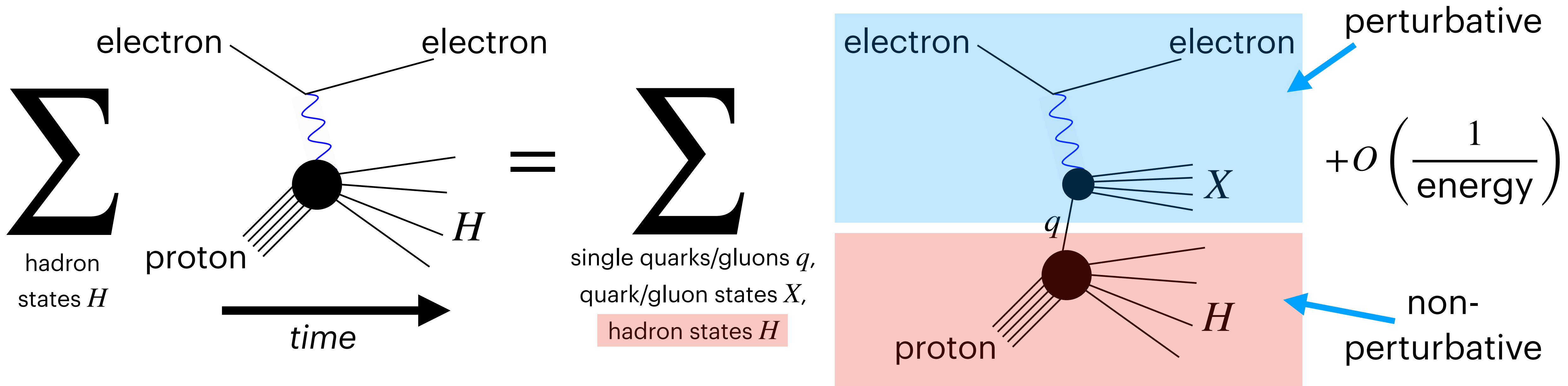
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- This is formalised through **factorisation theorems**.
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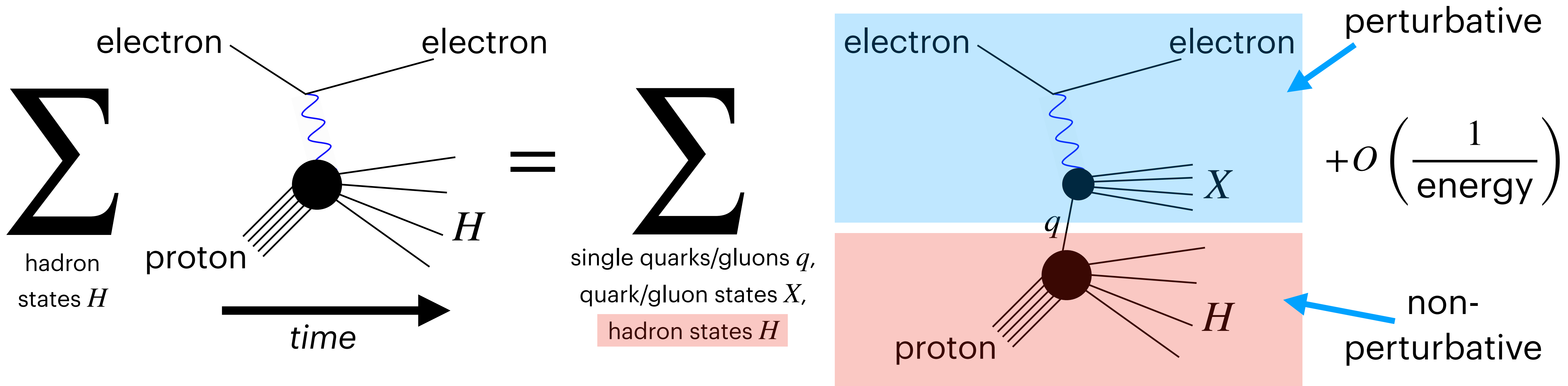
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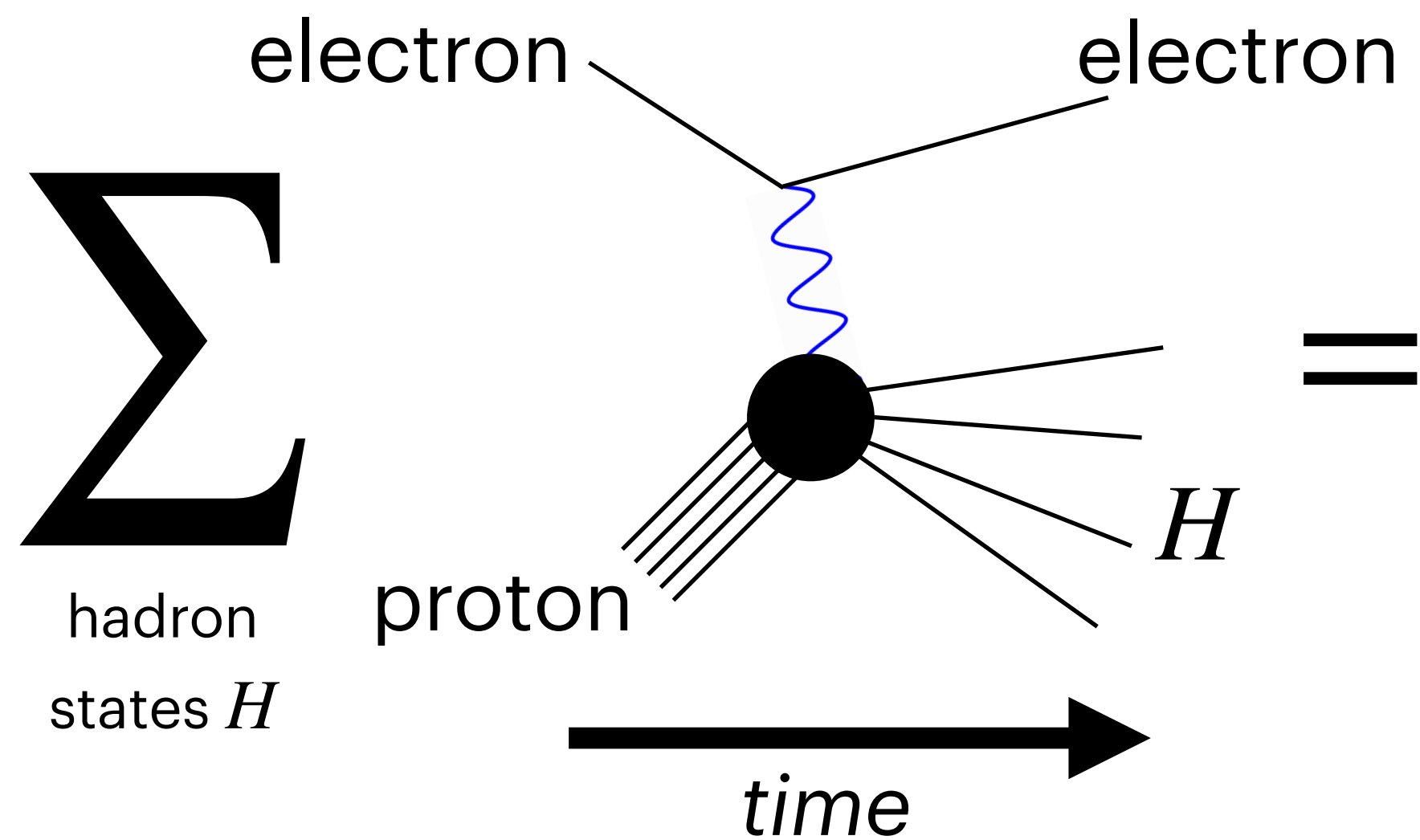
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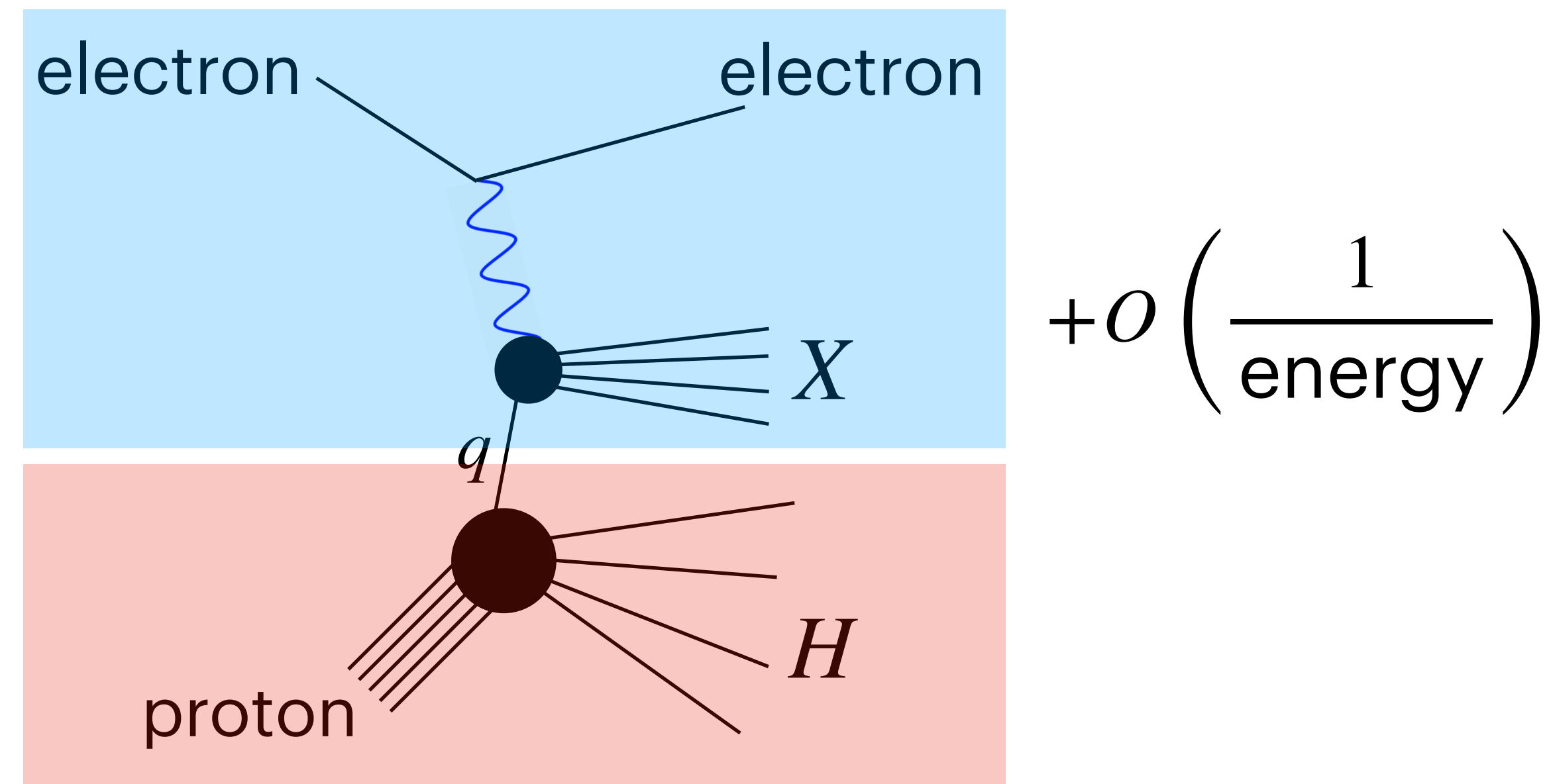
- The calculation is split into a **perturbative process-dependent part**, and a **non-perturbative, BUT universal, parton distribution function**.



# Factorisation theorems



$$= \sum_{\text{single quarks/gluons } q, \text{ quark/gluon states } X, \text{ hadron states } H}$$



In maths...  $\sigma(x, Q^2) = \sum_{\text{single quarks/gluons } q, \text{ quark/gluon states } X} \int_x^1 \frac{dy}{y} \hat{\sigma}_{eq \rightarrow eX} \left( \frac{x}{y}, Q^2 \right) f_q(y, Q^2) + O\left(\frac{1}{\text{energy}}\right)$

Mellin convolution

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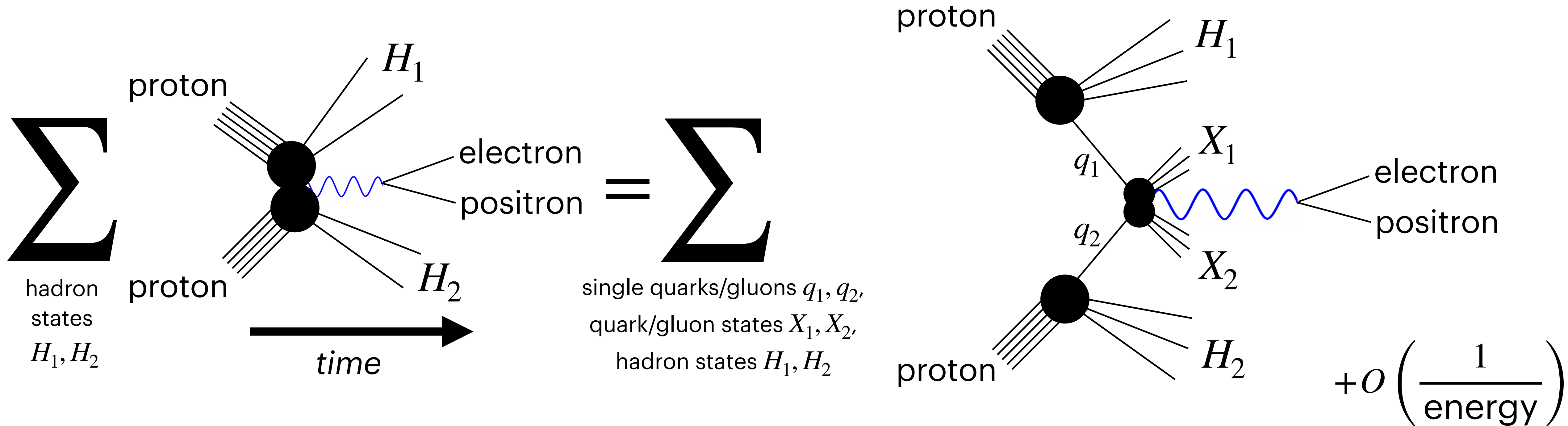
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  - An **energy scale**  $Q^2$  (comes from **absorbing collinear divergences**)
  - The fact we are colliding **protons** - if we started with a neutron, we would need different PDFs

# Universality of PDFs

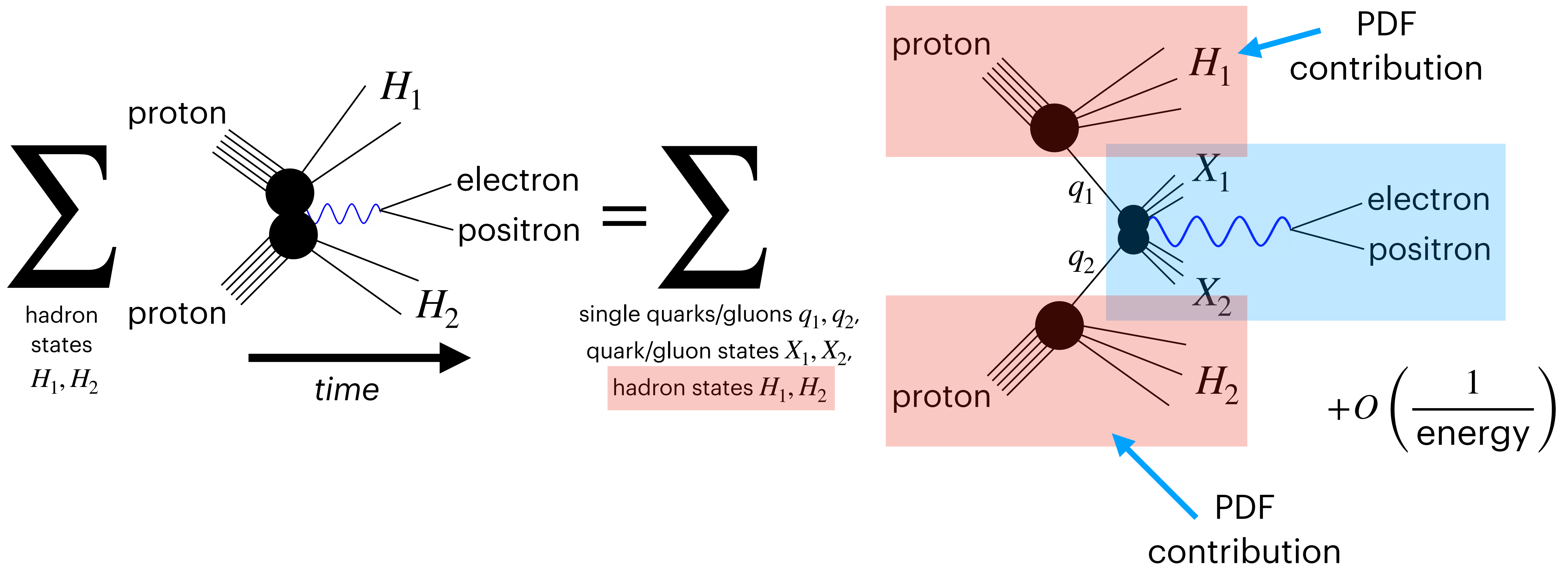
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# Scaling of PDFs

- Whilst the PDFs are non-perturbative, we can still say something about their  $Q^2$ -dependence, which enters the PDFs when we **absorb collinear IR divergences**.
- Just as in **standard UV renormalisation theory**, this leads to a Callan-Symanzik equation for the PDFs called the **DGLAP equation**:

$$Q^2 \frac{\partial f_q(x, Q^2)}{\partial Q^2} = \sum_{\text{quarks/gluons } q'} \int_x^1 \frac{dy}{y} P_{qq'}\left(\frac{x}{y}\right) f_{q'}(x, Q^2)$$

- The functions (technically distributions)  $P_{qq'}$  are called **splitting functions** and can be determined perturbatively.

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- This means if we know the PDFs at some **initial energy scale**  $Q_0$ , we can compute them at some energy scale  $Q > Q_0$  by solving DGLAP.
- In particular, only the  $x$ -dependence of the PDFs is truly **unknown**.
- We can obtain this  $x$ -dependence by **fits to collider data**, as we shall now describe...

# Summary of PDFs

- The **non-perturbative structure** of hadrons can be parametrised by **parton distribution functions**  $f_q(x, Q^2)$ , which depend only on the **type of hadron** being collided, **not** on the process.
- The PDFs have **known  $Q^2$ -dependence**, described by a linear system of **integro-differential equations** called the **DGLAP equations**.
- The PDFs have **unknown  $x$ -dependence**, which must be obtained through fits to experimental data.

# 2. - PDF fitting

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- Example functional form:

$$f(x, Q_0^2) = Ax^\alpha(1-x)^\beta(1 + ax^{1/2} + bx + cx^{3/2})$$

large and small  $x$  behaviour  
motivated by **Regge theory**

polynomial in  $\sqrt{x}$

# How to make PDFs...


- The best-fit parameters are found by **minimising the  $\chi^2$ -statistic**, which measures the **goodness of fit** of our model:

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- *General idea:* we want **theory to be close to data**, but if the data is **more uncertain**, we don't require such precise agreement.

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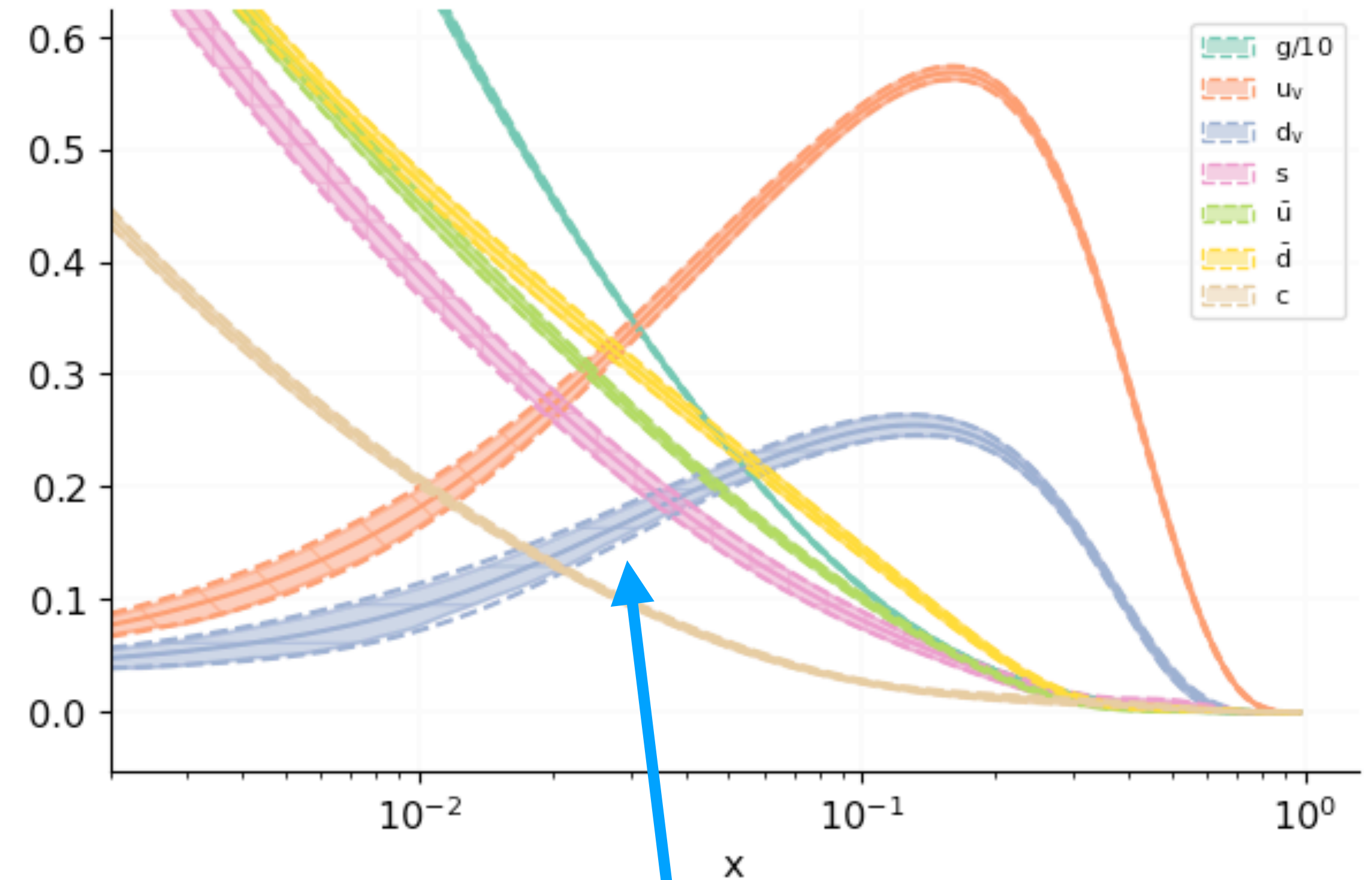
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PDFs with error bands



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- This seems a bit arbitrary though! To try to remove as much **bias** as possible, another possible choice is to parametrise the PDFs using a **neural network** instead:

$$f(x, Q_0^2) = Ax^\alpha(1-x)^\beta\text{NN}(x, \omega)$$

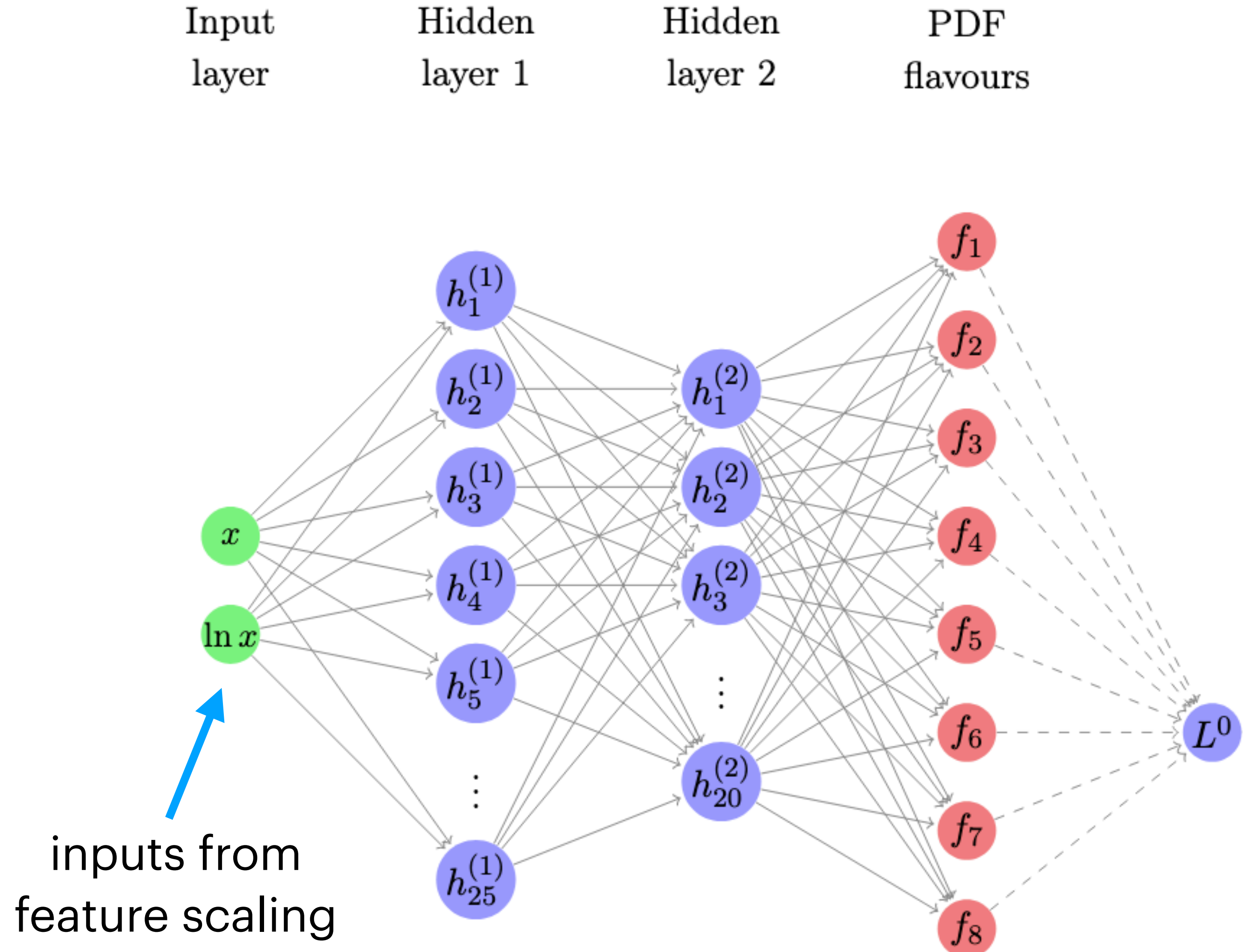
- Here,  $\text{NN}(x, \omega)$  is a **neural network** which takes in  $x$  as an argument, and has network parameters  $\omega$ .



# The choice of functional form

$$f(x, Q_0^2) = Ax^\alpha(1-x)^\beta \text{NN}(x, \omega)$$

- The neural network parametrisation is used by the **NNPDF collaboration**, whose fitting code is **publicly available**.
- See 2109.02653 and 2109.02671 for details.



# 3. - Joint PDF-SMEFT fits

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  - *Baryon number asymmetry*
  - *many more...*



# So how do we fix the Standard Model?

- For example, to **include dark matter** in the Standard Model, we might **hypothesise new particles** and add them in. The Standard Model Lagrangian density is augmented to:

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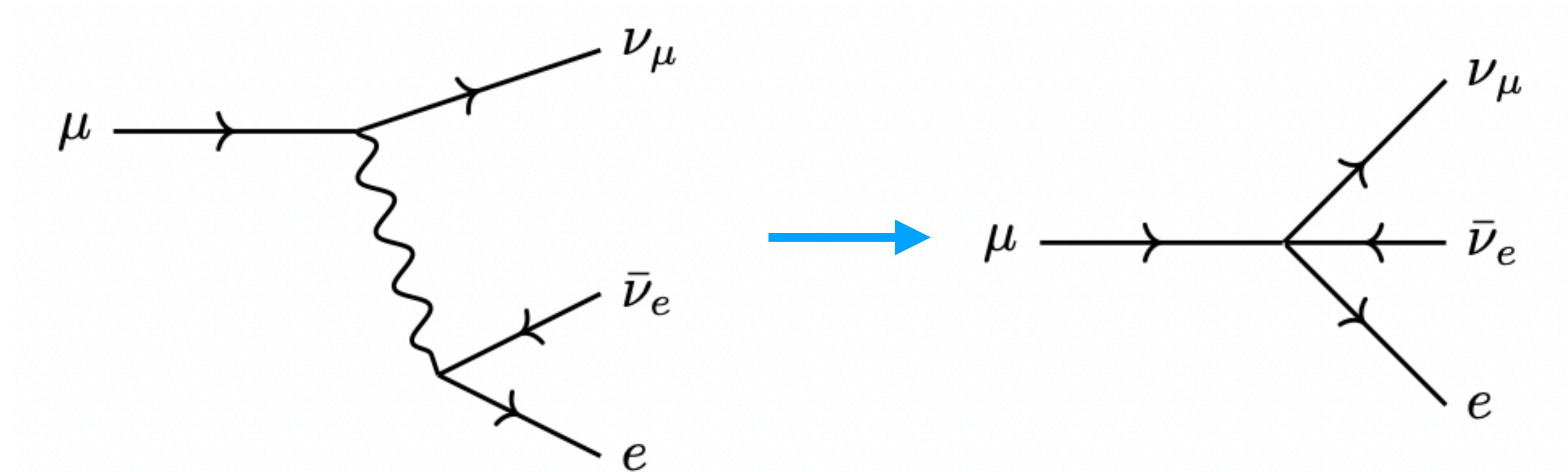
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- However, there are **thousands** of possibilities, so just guessing particles seems a bit like **stabbing in the dark!**
- Some models are **more motivated** than others, but it would be nice to have a more general approach...

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- *Idea:* at **low energies** we can **integrate out heavy particles from a theory**, giving **effective non-renormalisable interactions**:



- Integrating out particles can also yield **shifts in SM couplings**.



# Enter the SMEFT...

- Since **any**\* heavy particle manifests at low energies as non-renormalisable interactions, if we are hunting for **extensions of the SM**, we can simply **add on all non-renormalisable operators built from the SM fields** (and respecting the SM symmetries):

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- We can organise the additional non-renormalisable operators by their **mass dimension**, with higher-dimensional operators being **suppressed** by **powers of  $1/\Lambda$** , where  $\Lambda$  is a characteristic scale of the New Physics.

# SMEFT fits

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- However, the number of operators **decreases significantly** if we **assume additional symmetries**, e.g. **no baryon number violation**. There are only **59 operators** if we assume **flavour universality**.
- The main sectors studied so far are: **top, Higgs** and **electroweak** physics.

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- Finally, note that various fitting groups **just fit** the SMEFT couplings, for example the **SMEFiT collaboration**, and the **FitMaker collaboration**.
- In particular, SMEFiT and FitMaker both assume a **SM PDF input**. This could be **problematic** because the PDFs were fitted **assuming no New Physics...**

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- Optimal PDF parameters  $\theta^*$  then have an **implicit dependence** on initial SMEFT parameter choice:  $\text{PDF}(\theta^*) \equiv \text{PDF}(\theta^*(\bar{c}))$ .

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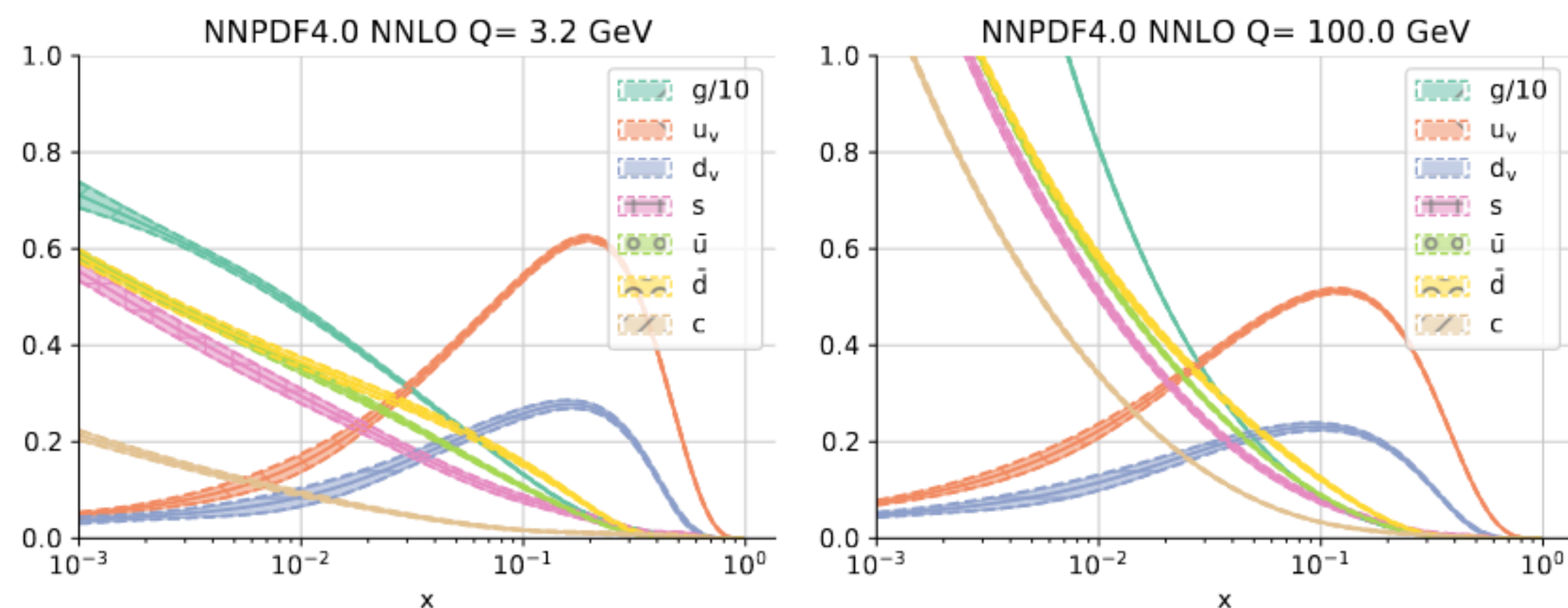
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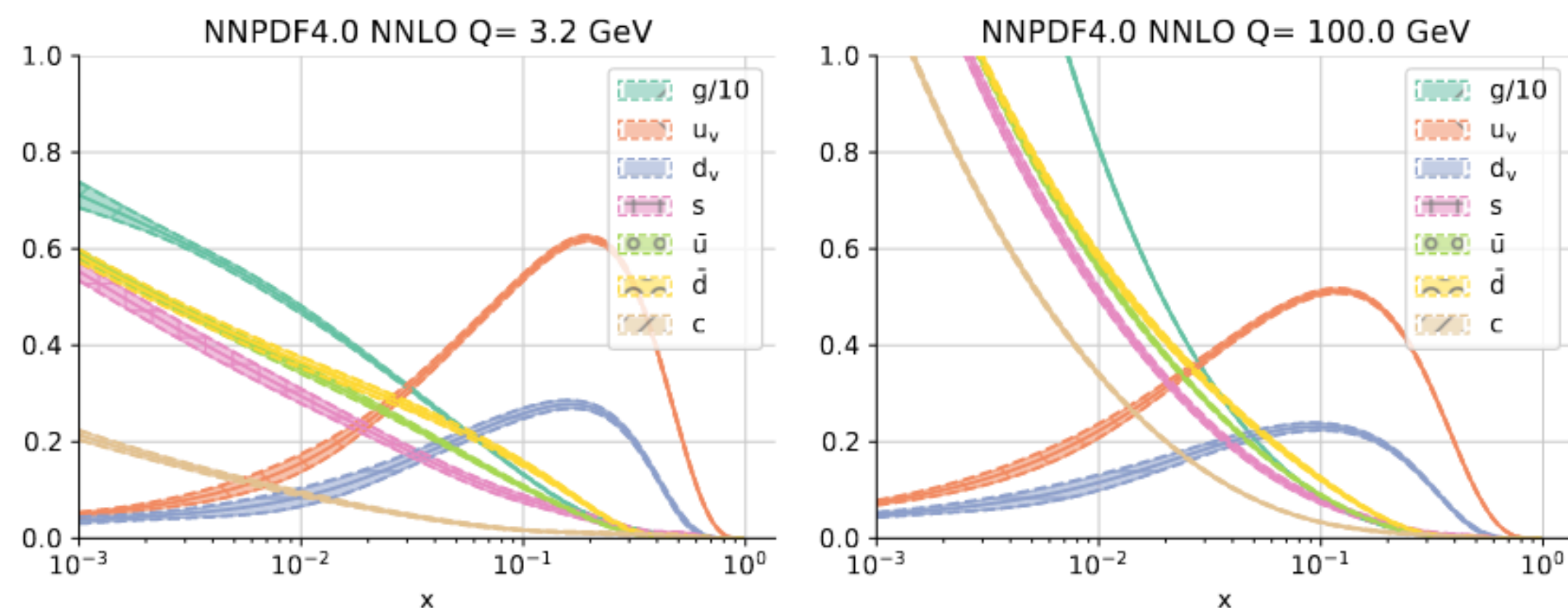
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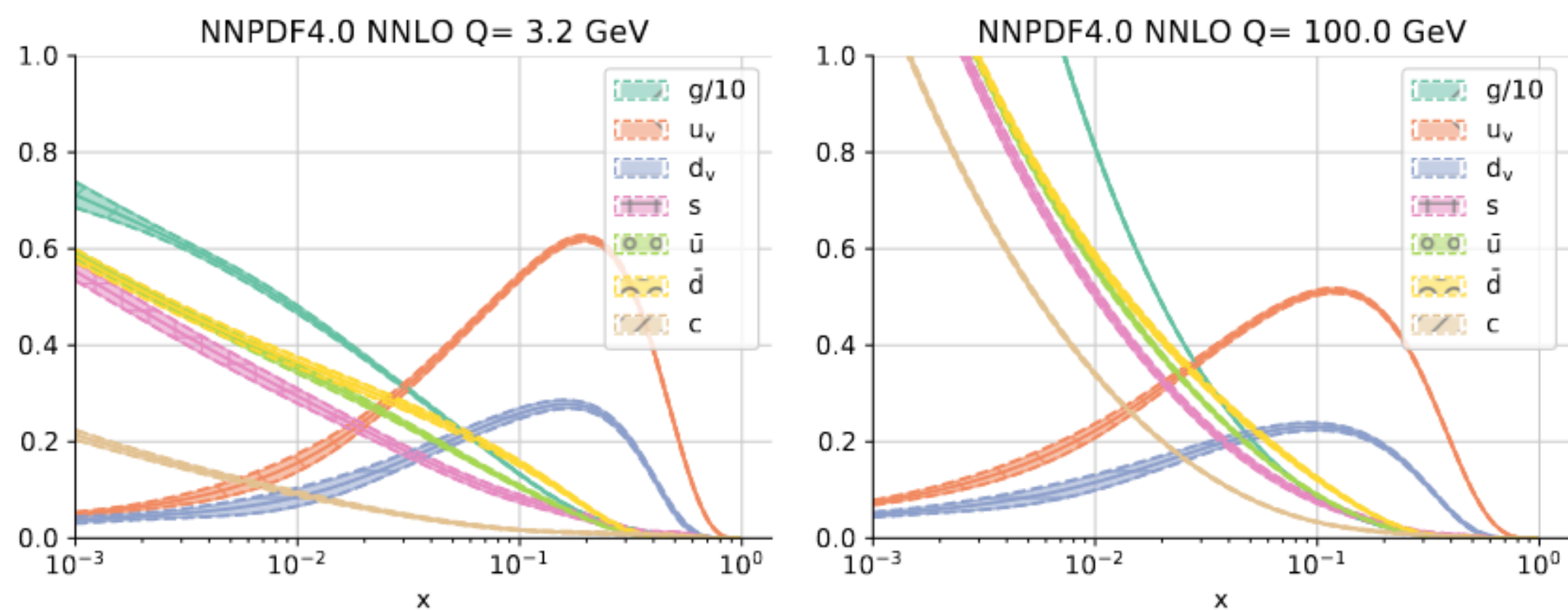
- In more detail ( $\otimes$  is shorthand for the **Mellin convolution**)...

## PDF parameter fits

- Fix SMEFT parameters (usually to zero),  $c = \bar{c}$ :

$$\sigma(\bar{c}, \theta) = \hat{\sigma}(\bar{c}) \otimes \text{PDF}(\theta)$$

- Optimal PDF parameters  $\theta^*$  then have an **implicit dependence** on initial SMEFT parameter choice:  $\text{PDF}(\theta^*) \equiv \text{PDF}(\theta^*(\bar{c}))$ .
- E.g. NNPDF4.0 fit, Ball et al., 2109.02653.

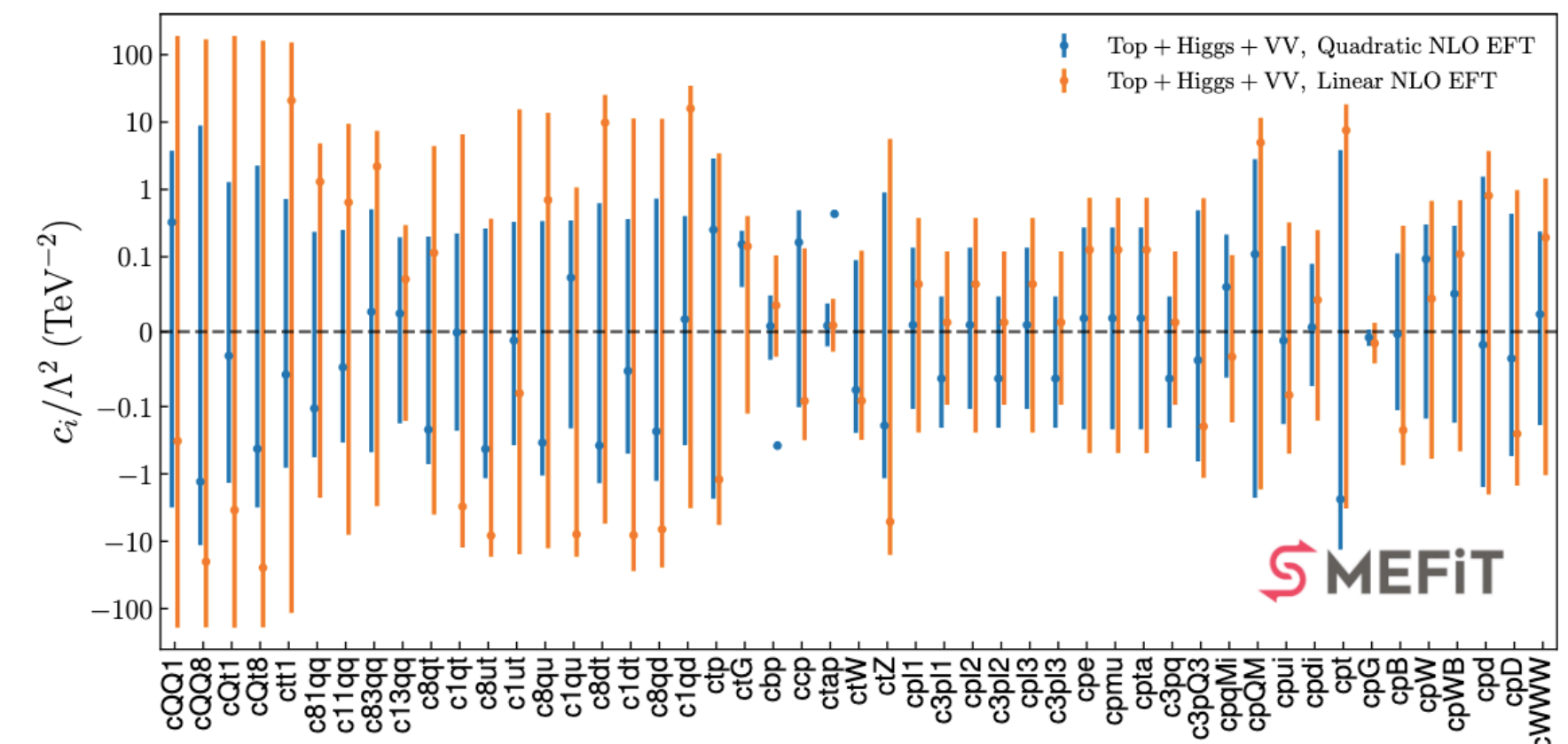


## SMEFT parameter fits

- Fix PDF parameters  $\theta = \bar{\theta}$ :

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# Joint PDF-SMEFT fits?

- **This could lead to inconsistencies.**

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- In particular, if we fit PDFs **assuming all SMEFT couplings are zero**, but then **use those PDFs in a fit of SMEFT couplings**, our resulting bounds **could be misleading**. The same applies to SM parameters.
- We could even **miss New Physics**, or **see New Physics that isn't really there!**

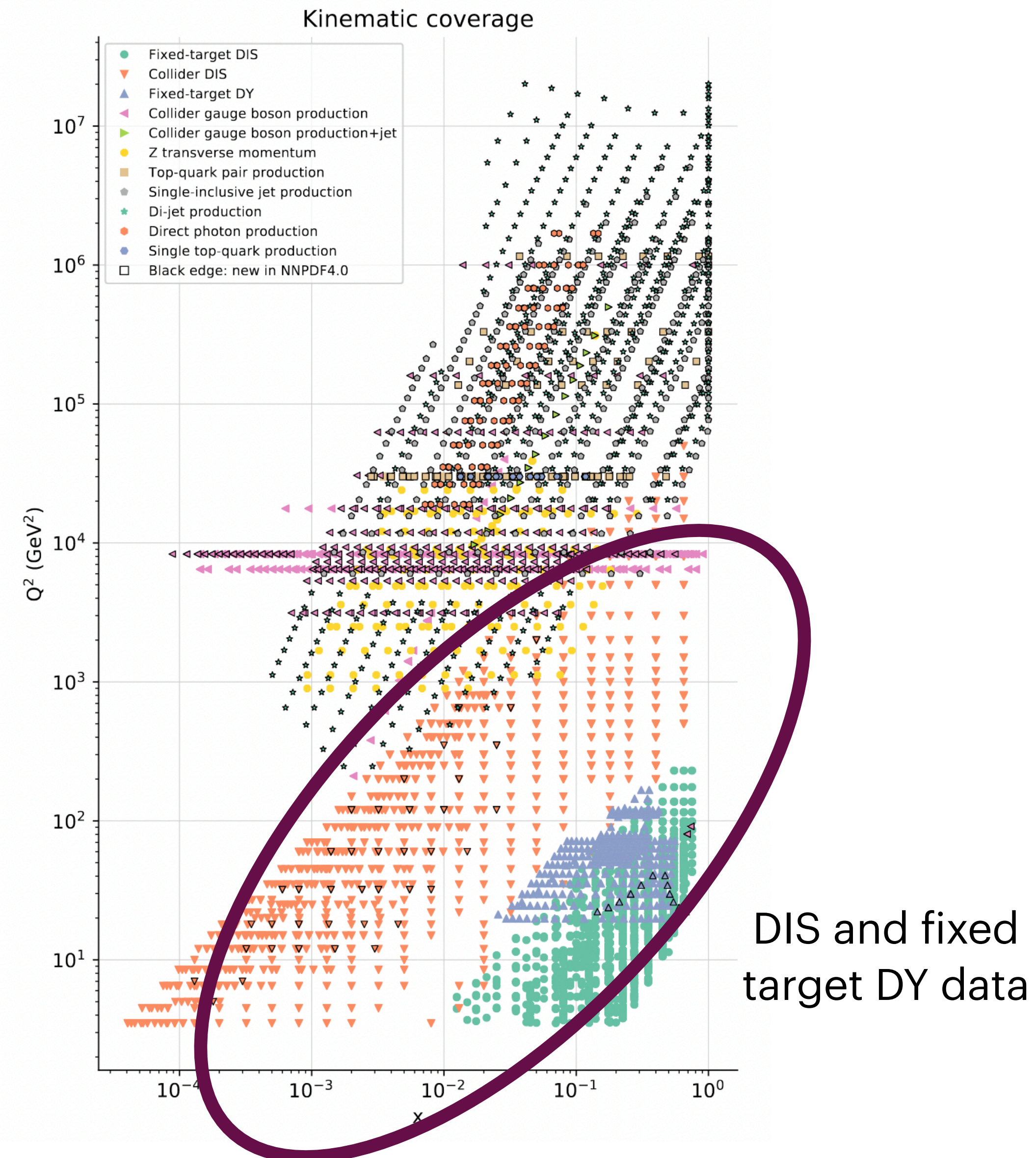
# PDF-SMEFT interplay: natural questions

- *Question 1:* **Can't I just use PDF sets which are fitted using data that is not affected by SMEFT operators?**



# PDF-SMEFT interplay: natural questions

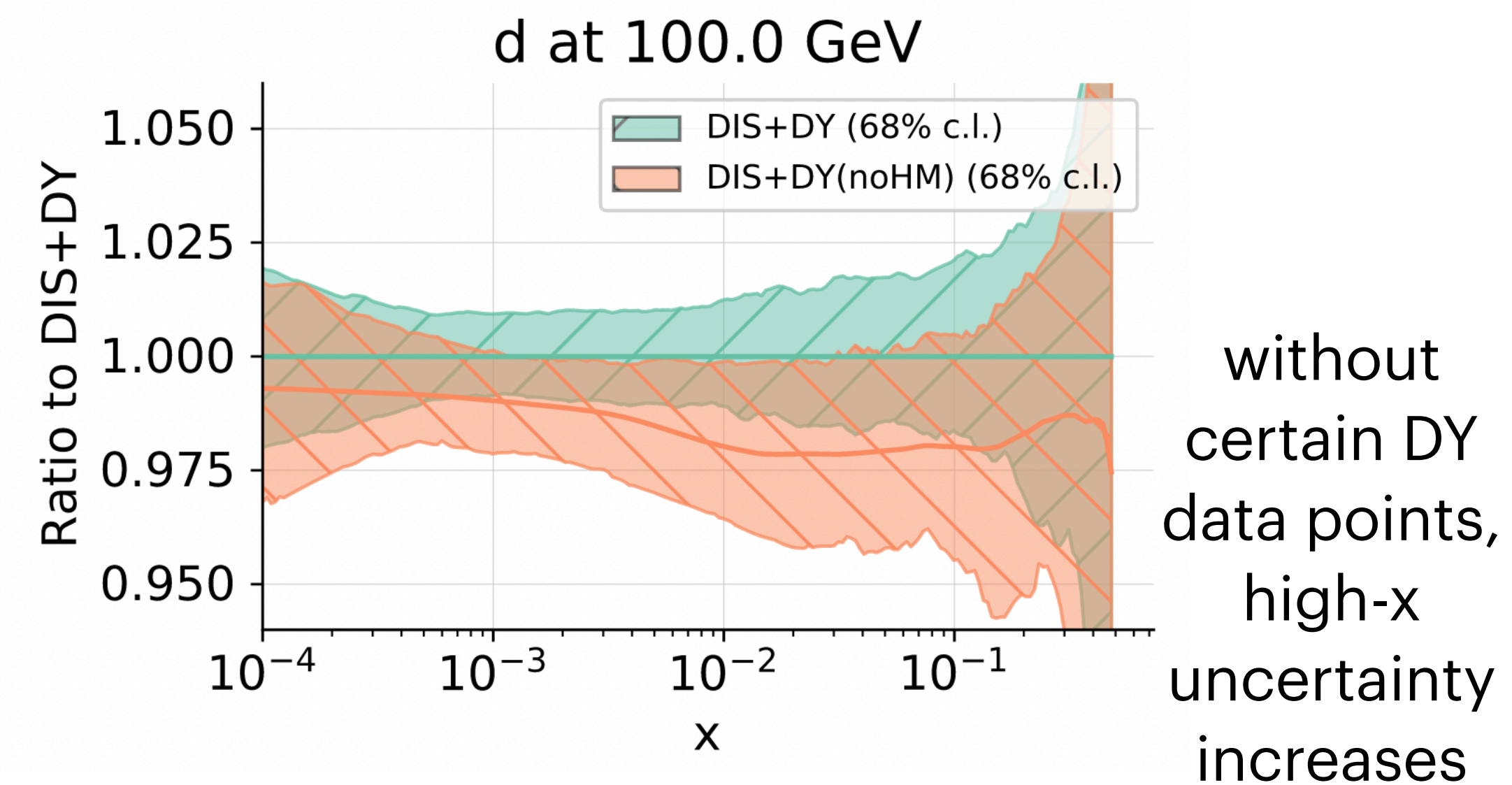
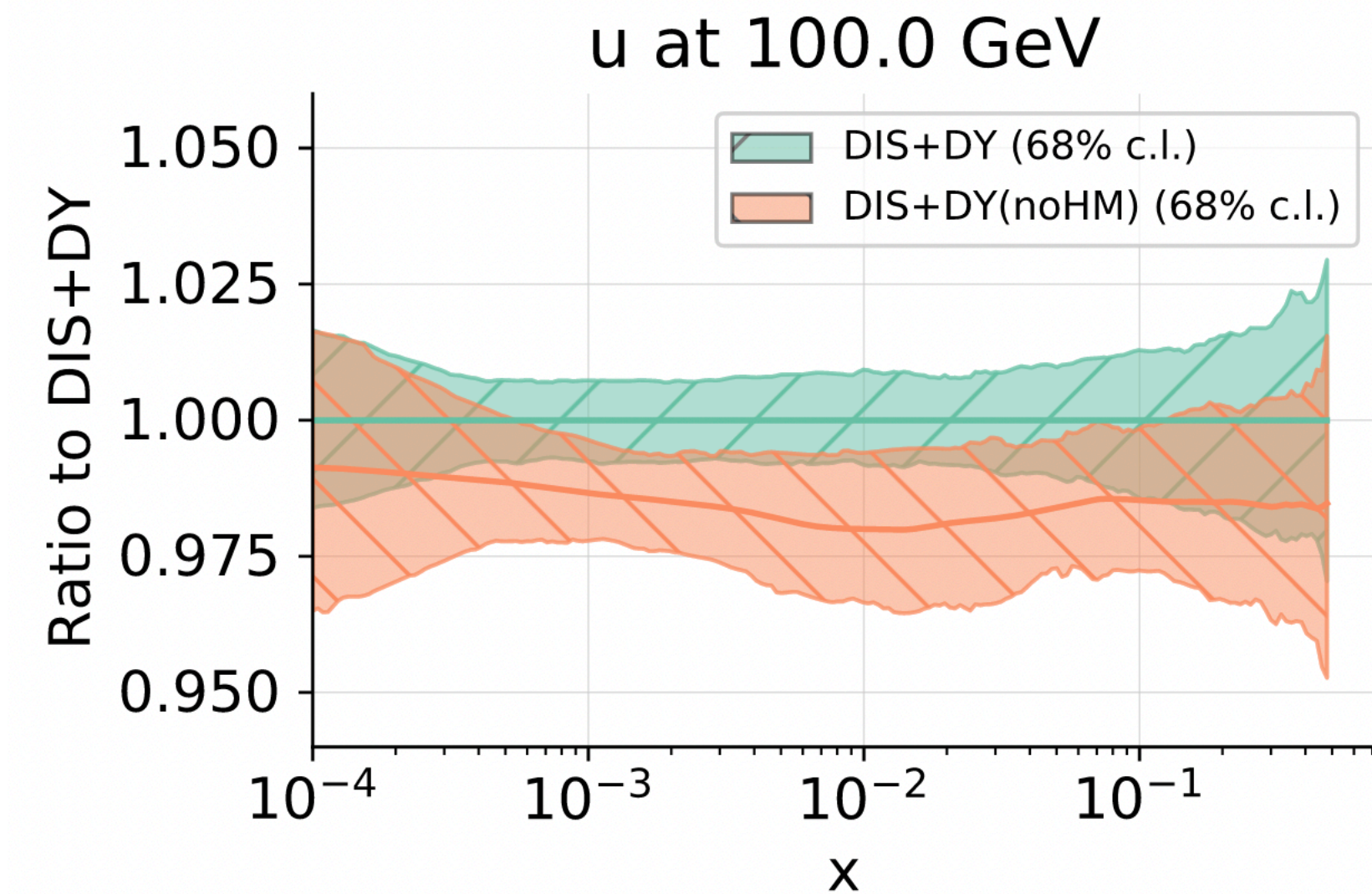
- **Question 1: Can't I just use PDF sets which are fitted using data that is not affected by SMEFT operators?**
  - It depends on the SMEFT operators. Some operators (e.g. four-fermion operators) will **contaminate DIS and DY data**, which comprise the majority of the data going into PDF fits. So often '*uncontaminated PDFs*' don't exist!
  - Right: kinematic coverage of NNPDF4.0 by dataset.





# PDF-SMEFT interplay: natural questions

- **Question 1: Can't I just use PDF sets which are fitted using data that is not affected by SMEFT operators?**
  - Furthermore, if we include more data in a PDF fit, we obtain **better quality fits**. Therefore, we expect that using 'uncontaminated PDFs' will result in **poorer quality SMEFT fits**; we won't be using the 'best quality' PDFs that are available - this is shown explicitly in *Greljo et al., 2104.02723*, where PDF sets including and excluding high-mass DY data are compared.



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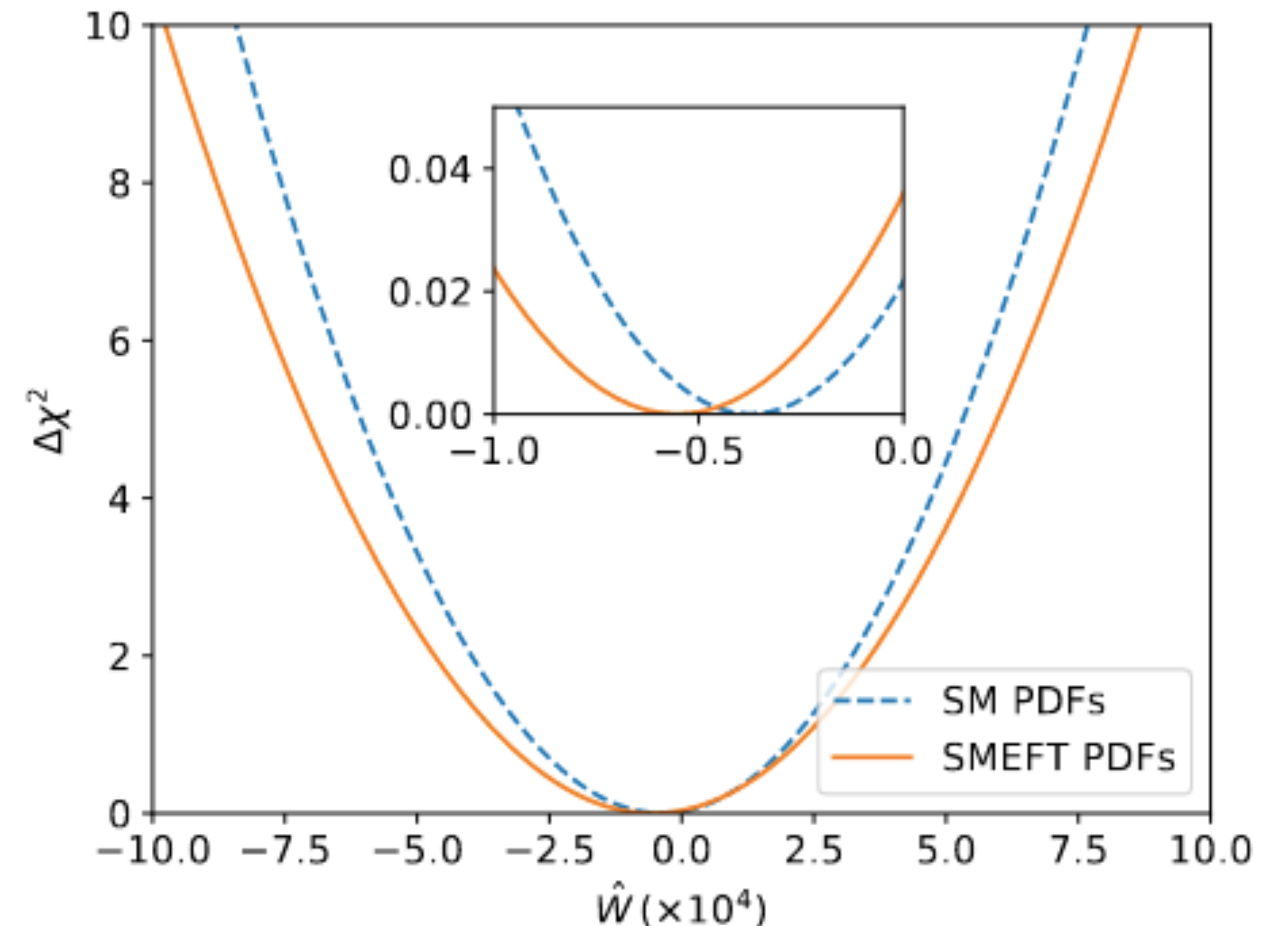
# PDF-SMEFT interplay: natural questions

- *Question 2: **Won't the PDF-SMEFT interplay be negligible?***
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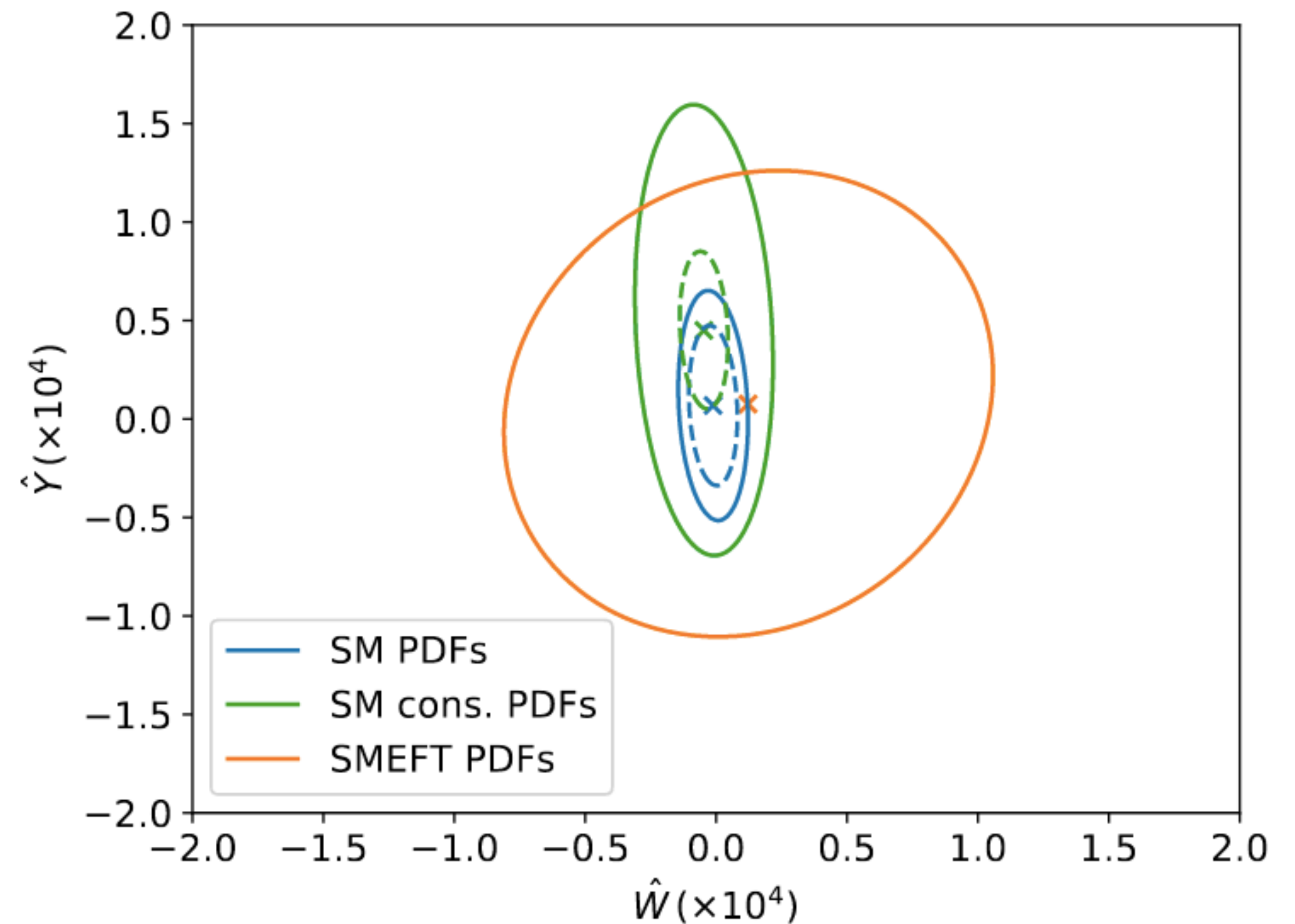
- It depends on the scenario!
- It was shown in *Carrazza et al., 1905.05215*, that interplay is very mild in the case of simultaneous extractions of four-fermion operators and PDFs using DIS-only data.
- Similarly, it was shown in the PBSP team's earlier study, *Greljo et al., 2104.02723*, that interplay is mild between the  $\hat{W}$ ,  $\hat{Y}$  operators and PDFs using current DIS and DY data.



# PDF-SMEFT interplay: natural questions

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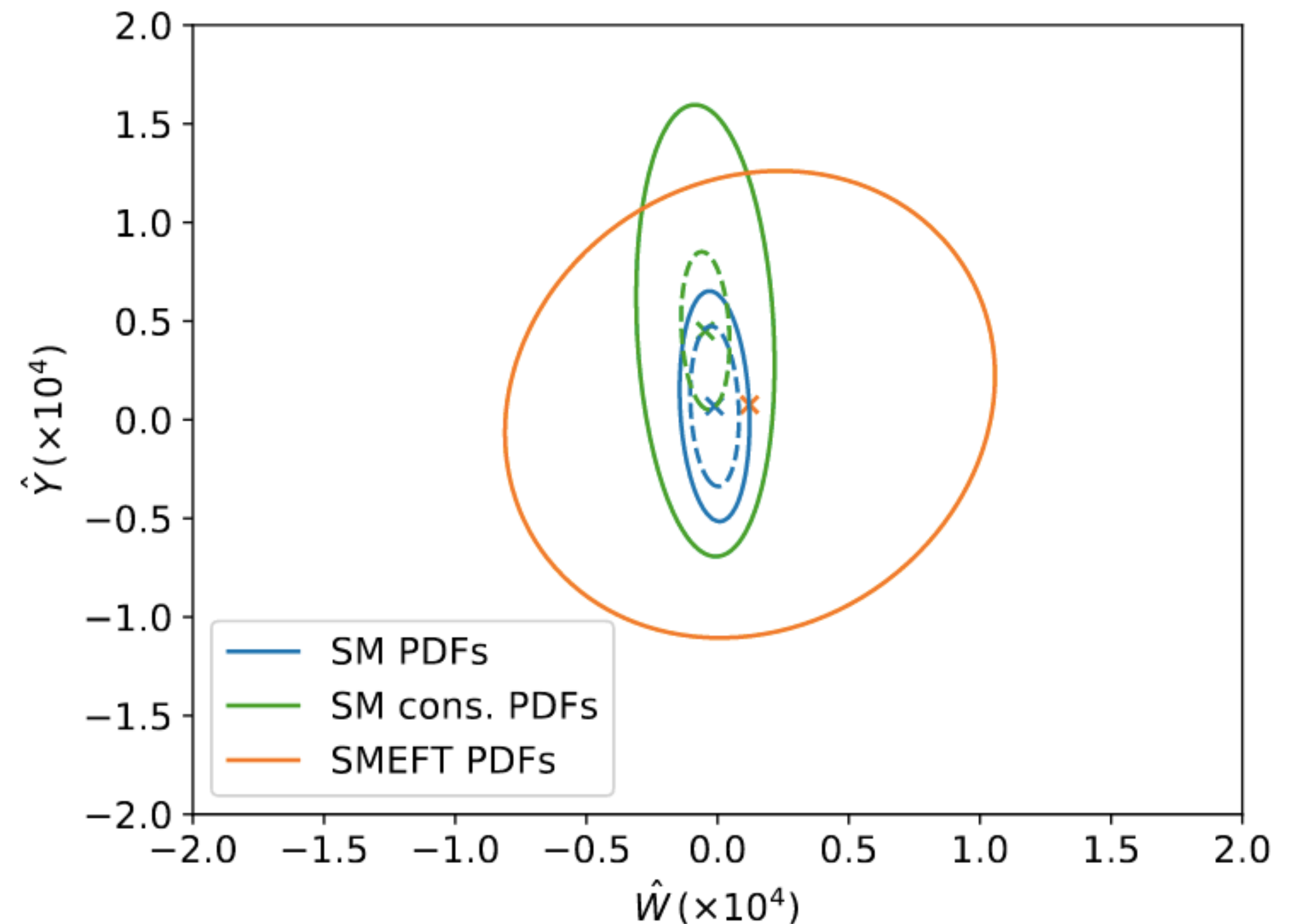
- However, it was also shown in *Greljo et al., 2104.02723*, that interplay is **very significant** between the  $\hat{W}$ ,  $\hat{Y}$  operators and PDFs using **projected high-luminosity DY data**.



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- However, it was also shown in *Greljo et al., 2104.02723*, that interplay is **very significant** between the  $\hat{W}$ ,  $\hat{Y}$  operators and PDFs using **projected high-luminosity DY data**.
- We see that using fixed PDFs results in a **significant underestimation** of uncertainties on the WCs - we might wrongly conclude **New Physics!**



# 4. - The SIMUnet methodology for joint PDF-SMEFT fits

# PDF-SMEFT interplay: methodology

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## 1. 'Scan' methodology

- Select a grid of benchmark SMEFT points.
- Perform PDF fits at each benchmark point.
- Construct a  $\chi^2$ -surface and obtain bounds.

See **1905.05215** and  
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## 2. CTEQ-TEA methodology

- Model the  $\chi^2$ -surface as a neural network, with inputs given by PDF parameters and WCs.
- After training the network, use Lagrange multiplier scans to minimise  $\chi^2$ .

See **2201.06586** and  
**2211.01094**

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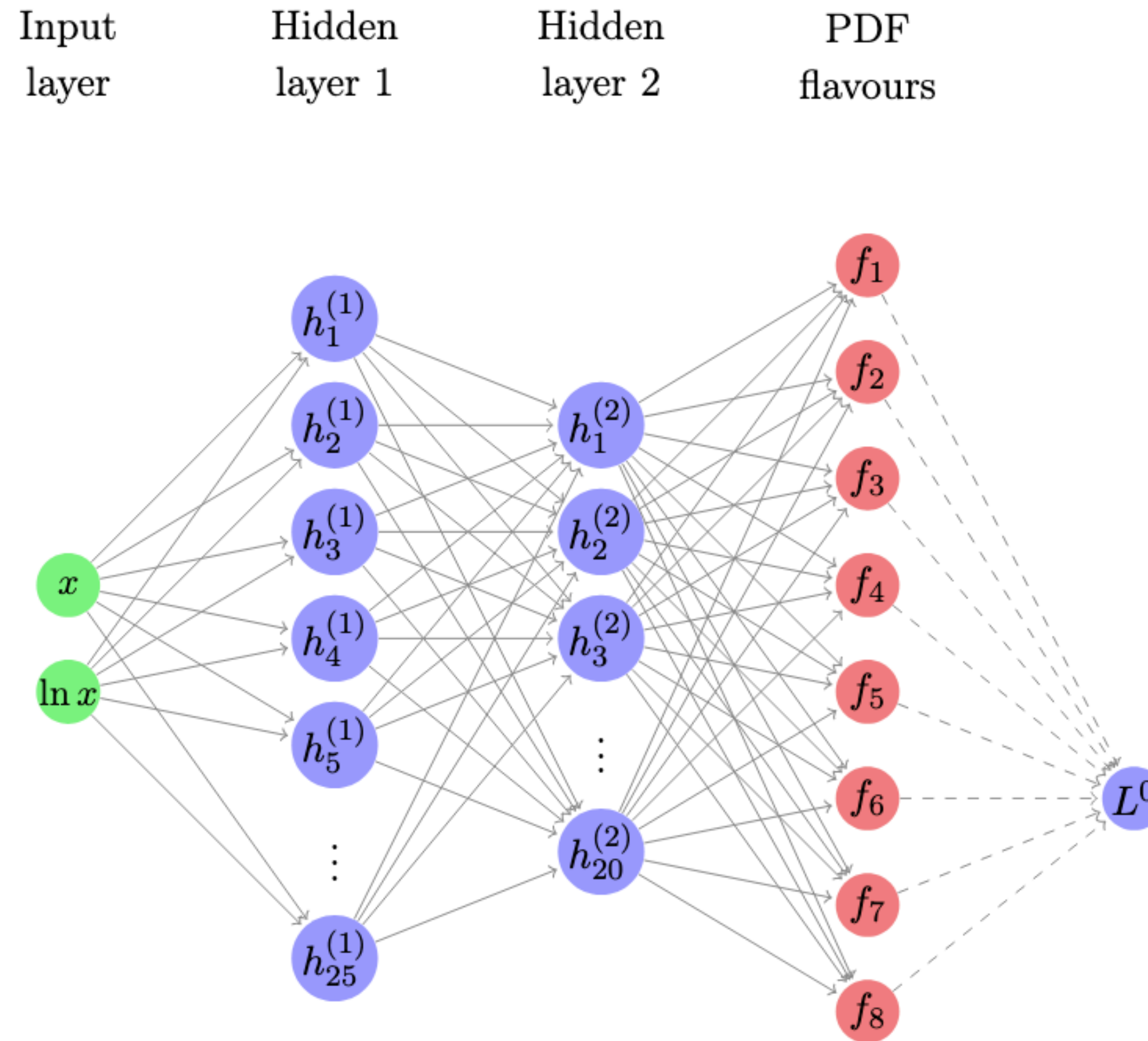
## 3. SIMUnet methodology

- Extend the NNPDF replica networks with a new layer with edges corresponding to the WCs.
- Train the network as per an NNPDF fit, but also learning the WCs.

See **2201.07240**

# The SIMUnet methodology: details

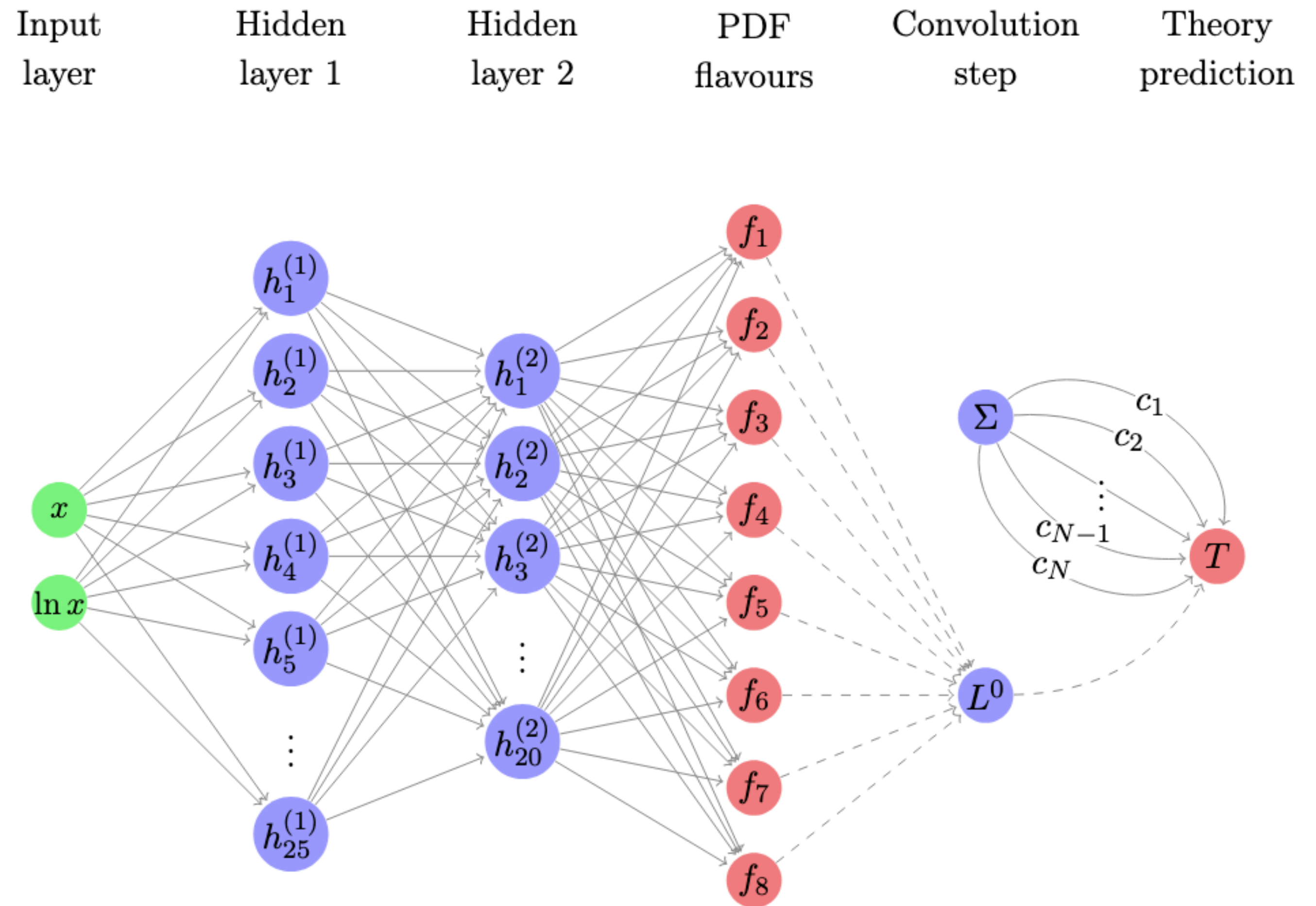
- The SIMUnet methodology **extends the existing NNPDF neural network** with an additional **convolution layer**.





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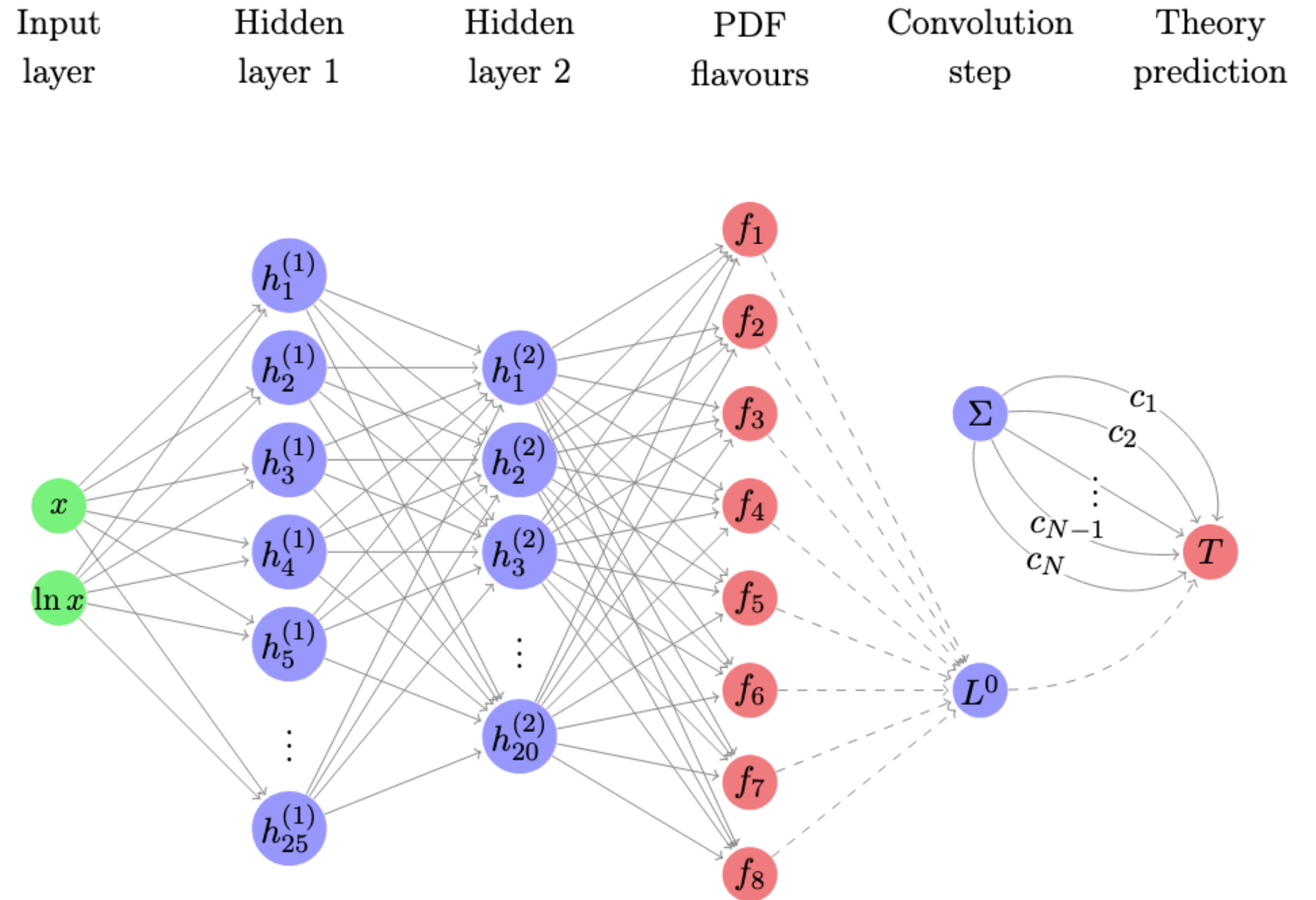
- The SIMUnet methodology **extends the existing NNPDF neural network** with an additional **convolution layer**.
- The SMEFT couplings are added as **weights of neural network edges**, and are **trained alongside the PDFs**.





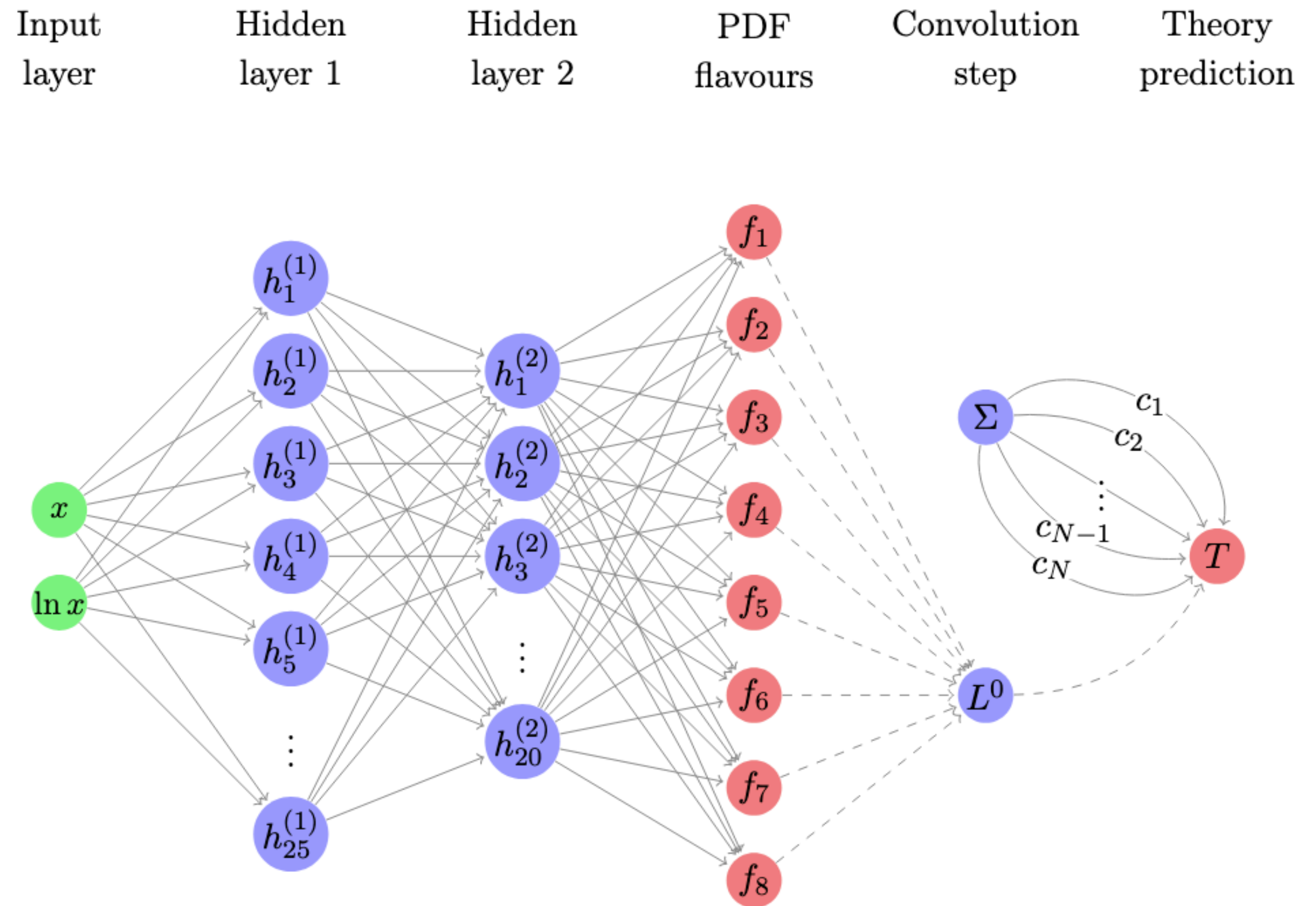
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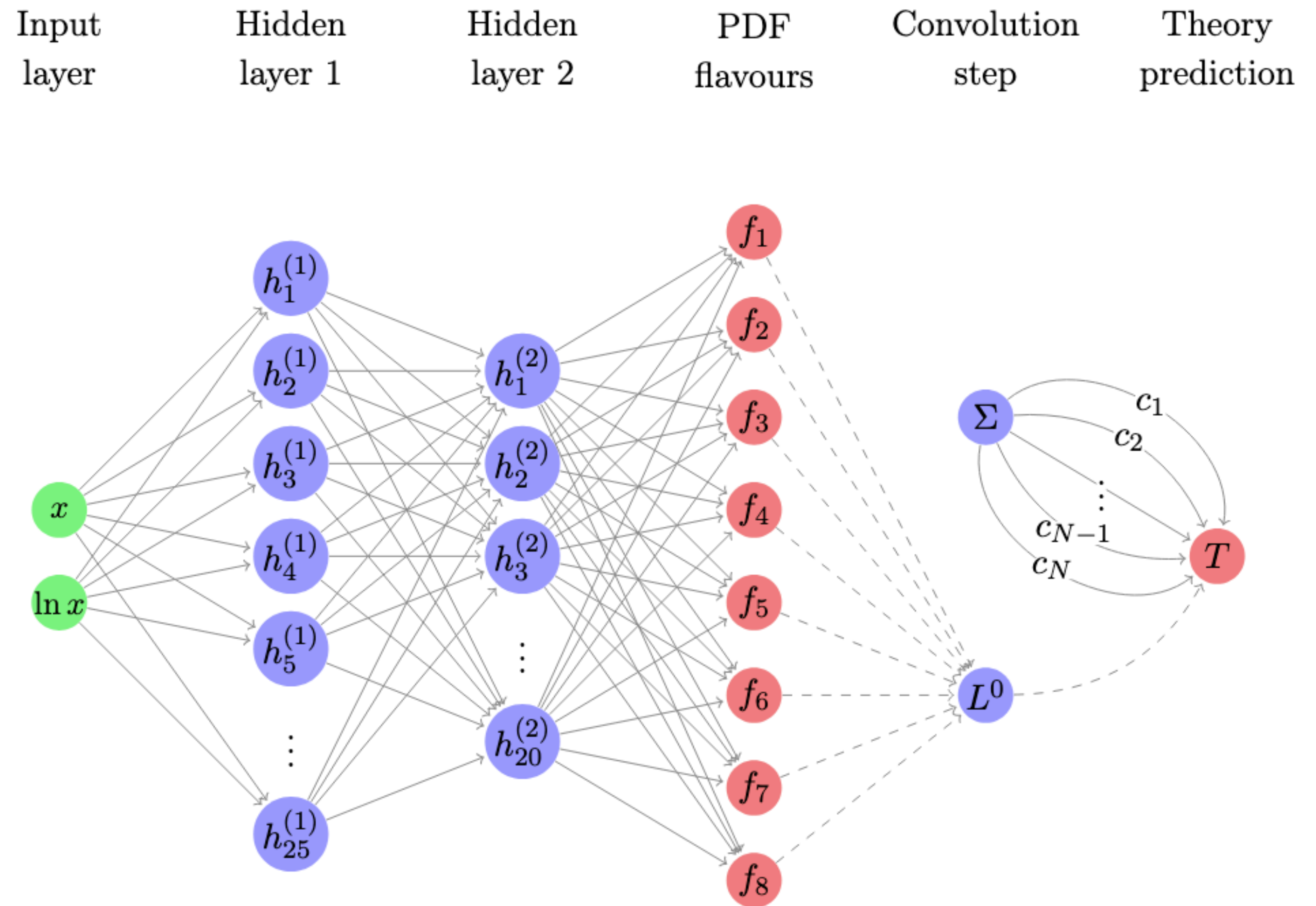
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- Can easily include **PDF-independent observables**.

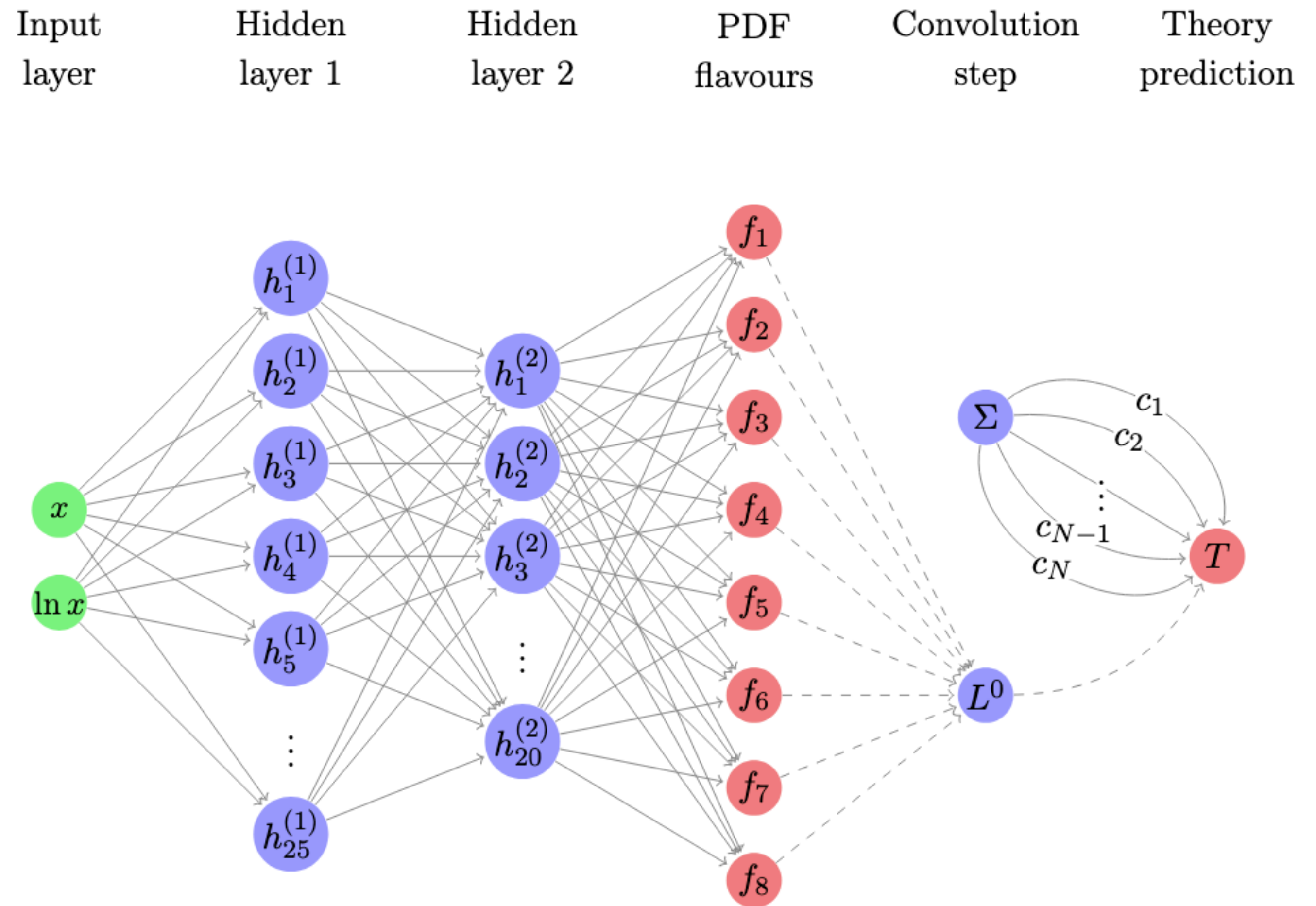




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- Can include **quadratic\*** SMEFT corrections through **non-trainable edges**.
- Can easily include **PDF-independent observables**.
- Can perform **fixed PDF fits** by **freezing the PDF part of the network**.



# 5. - The top quark legacy of the LHC Run II for PDF and SMEFT analyses

***Based on 2303.06159***

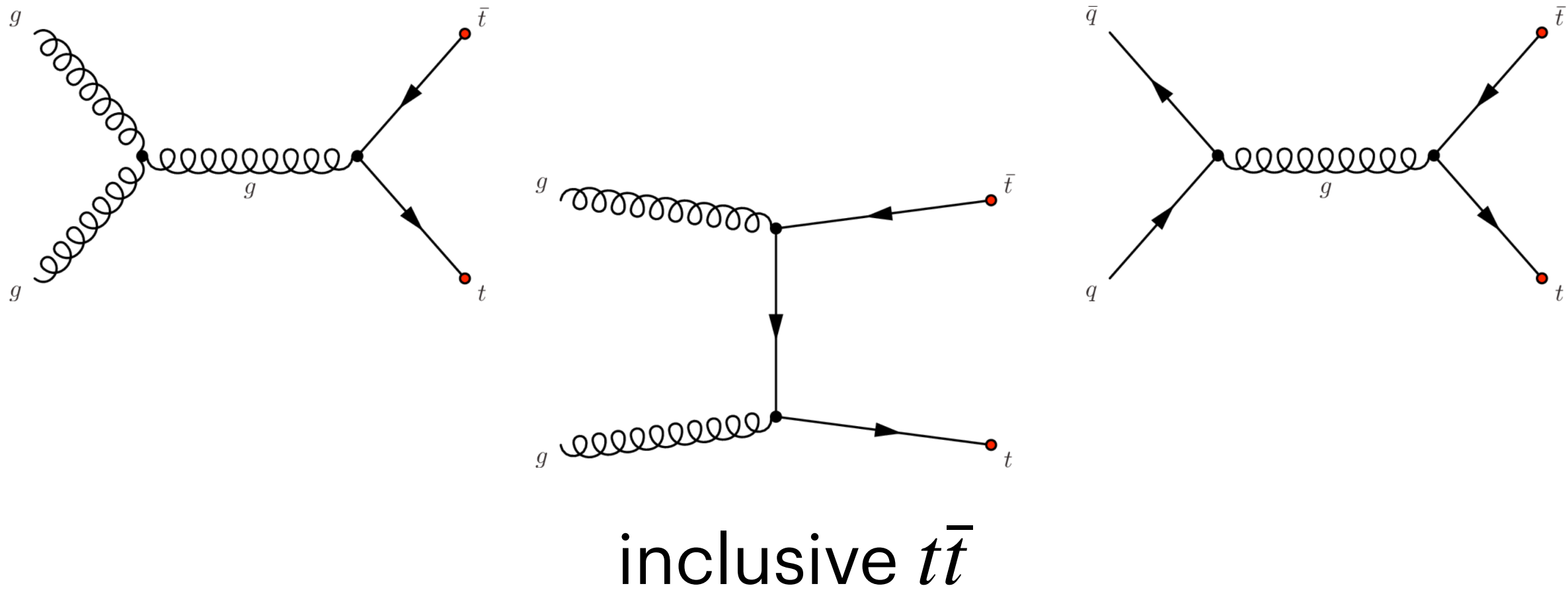
# Run II top quark data

- **Huge amount of Run II top quark data** from ATLAS and CMS. Four basic processes:



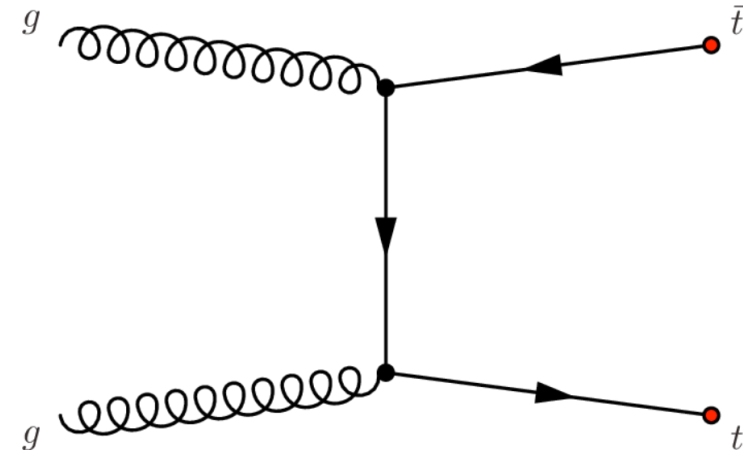
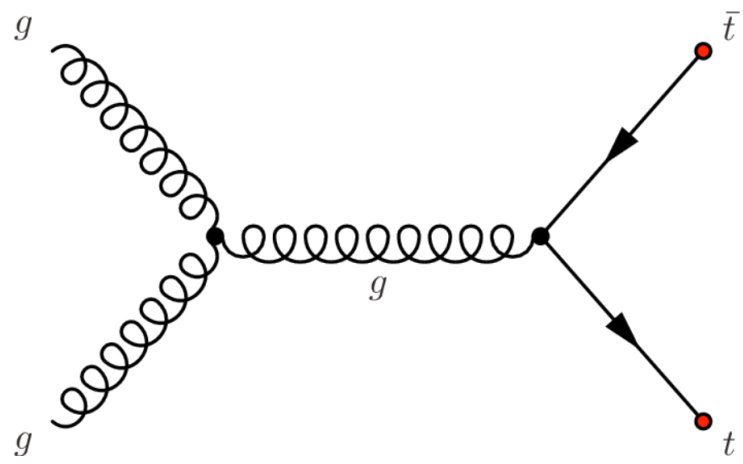
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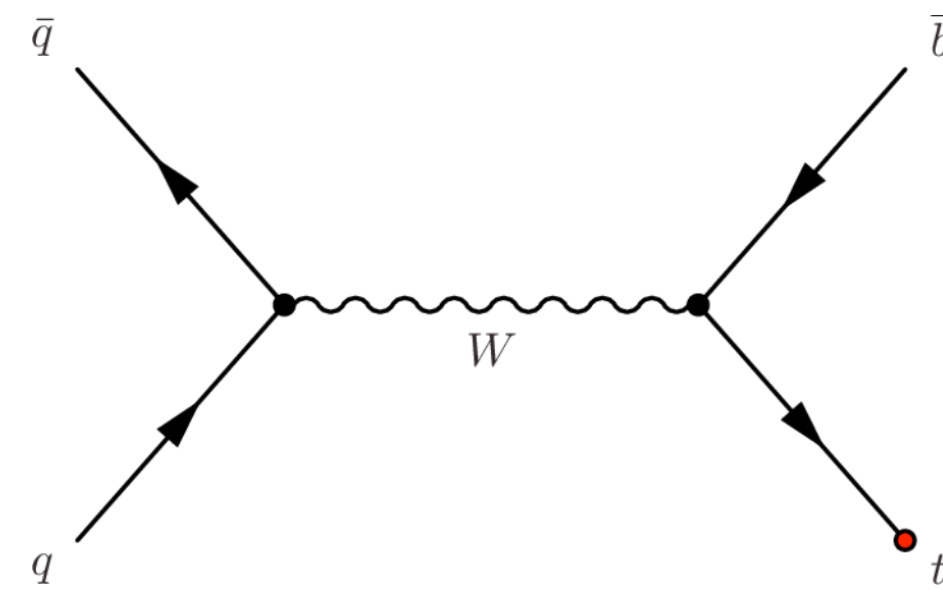
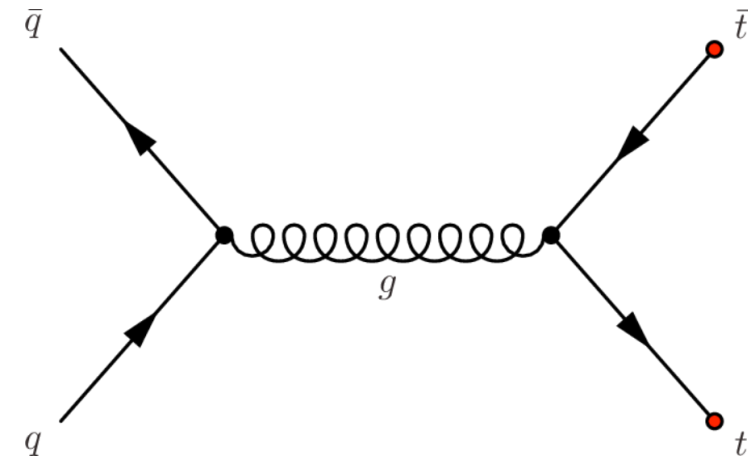


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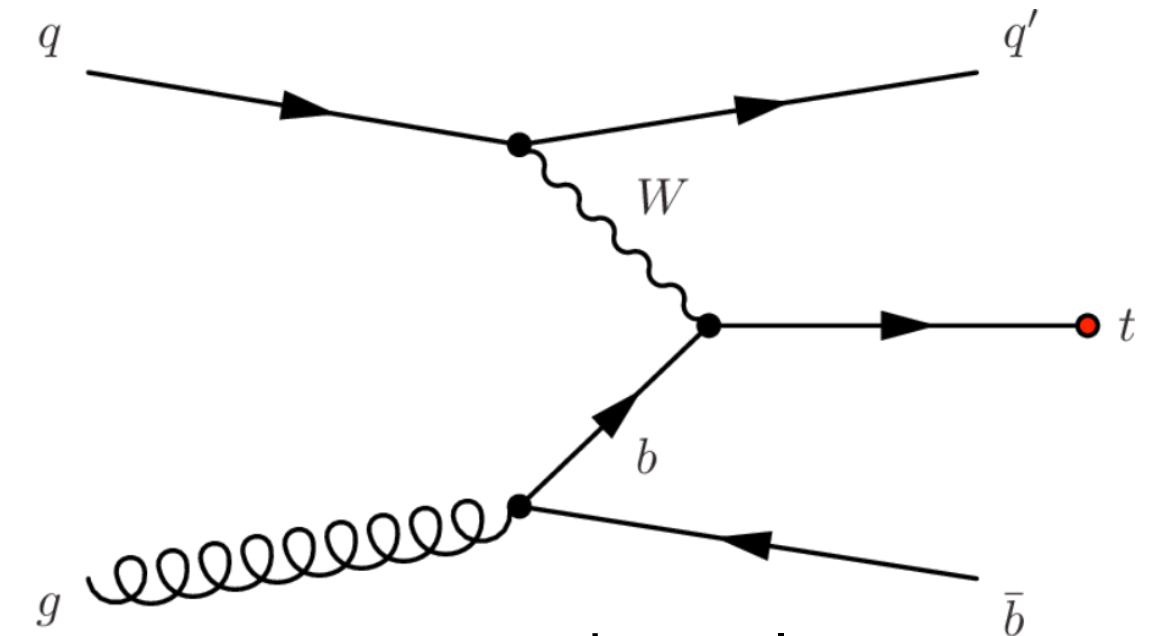
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inclusive  $t\bar{t}$



s-channel

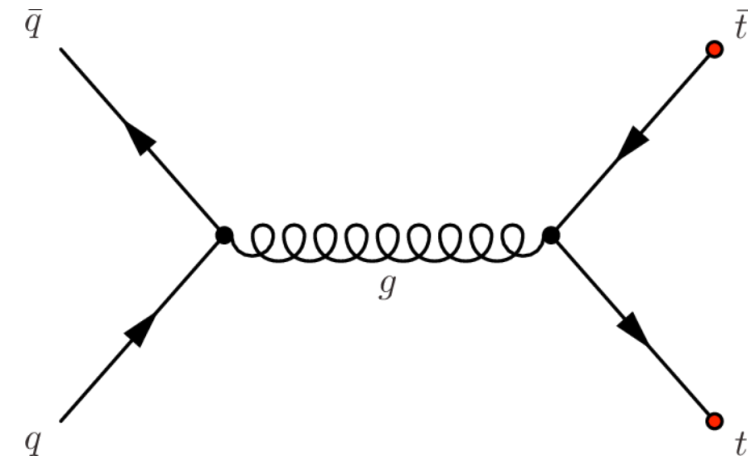
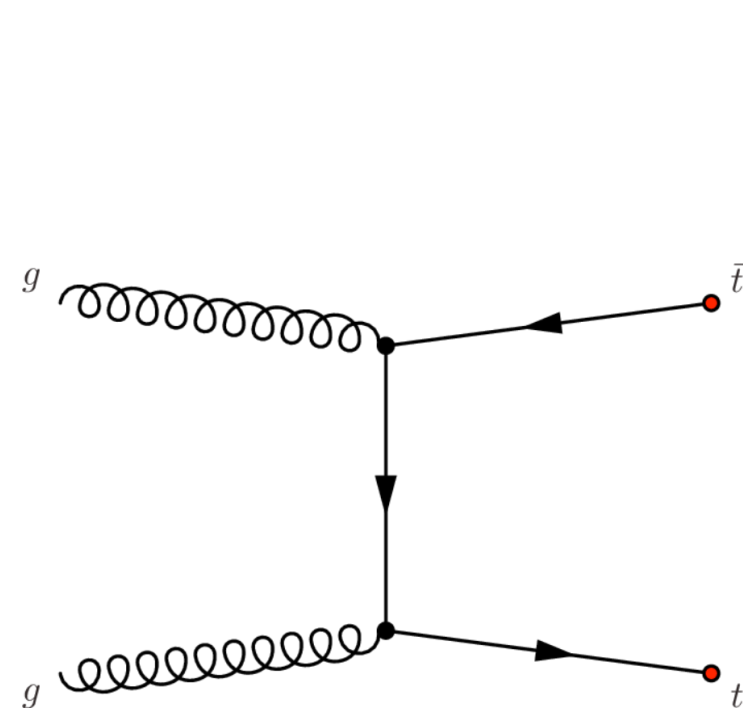
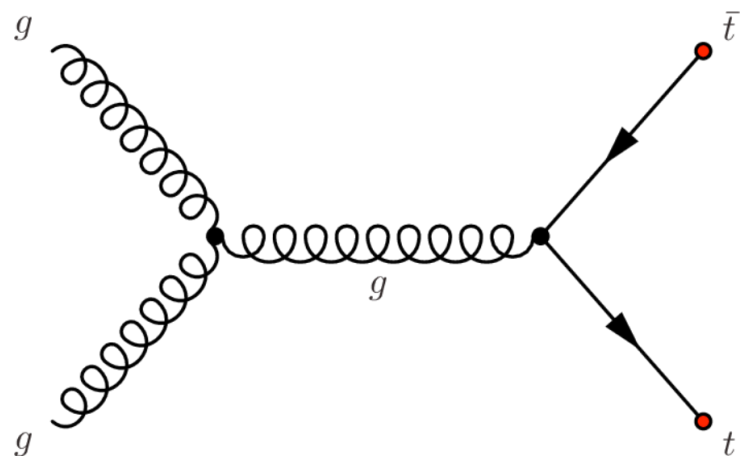


t-channel

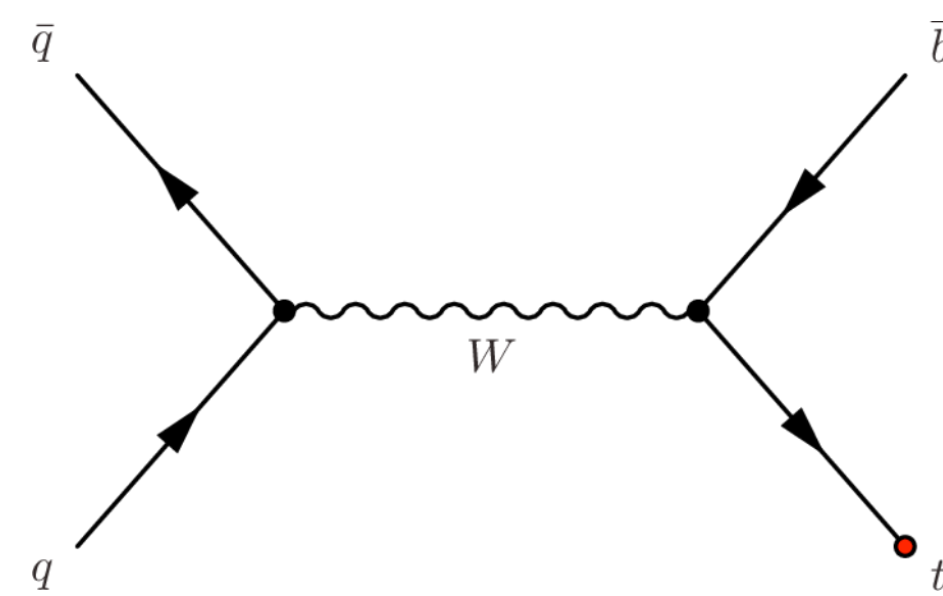
single top

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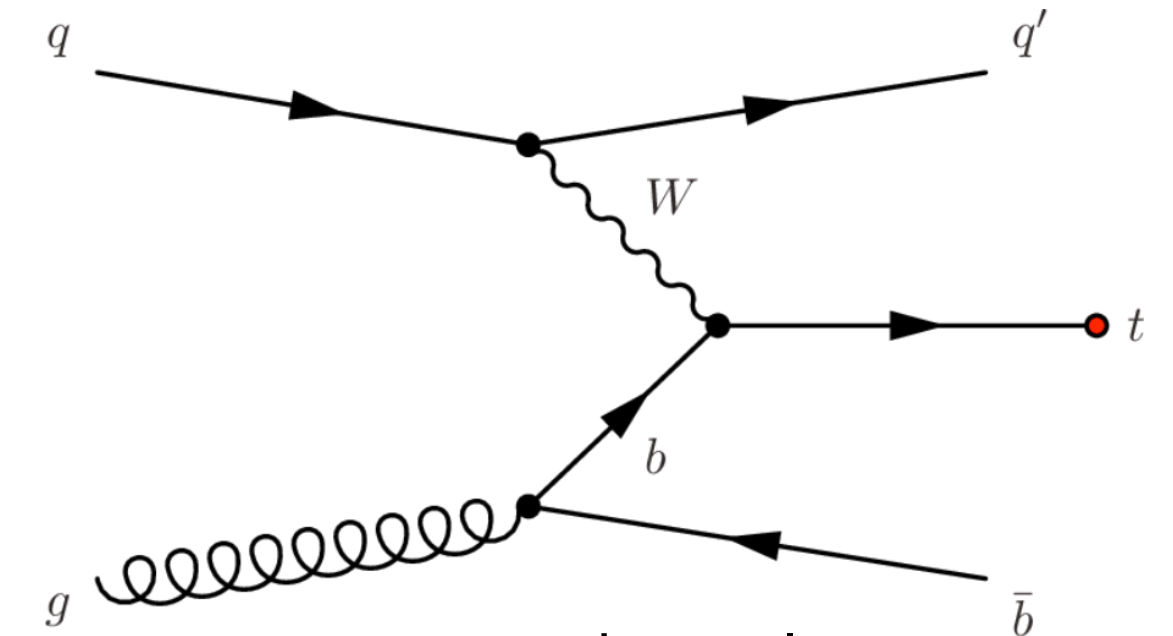
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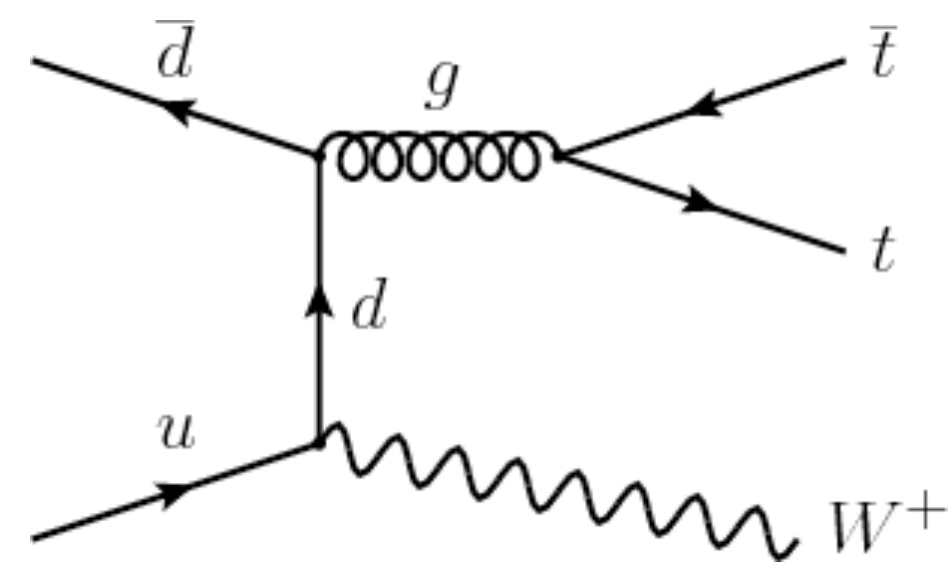
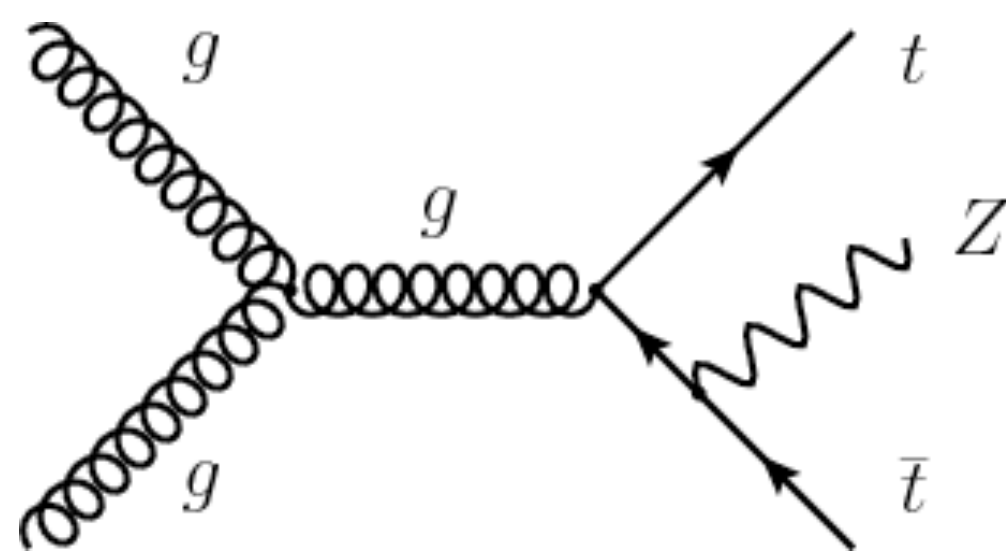


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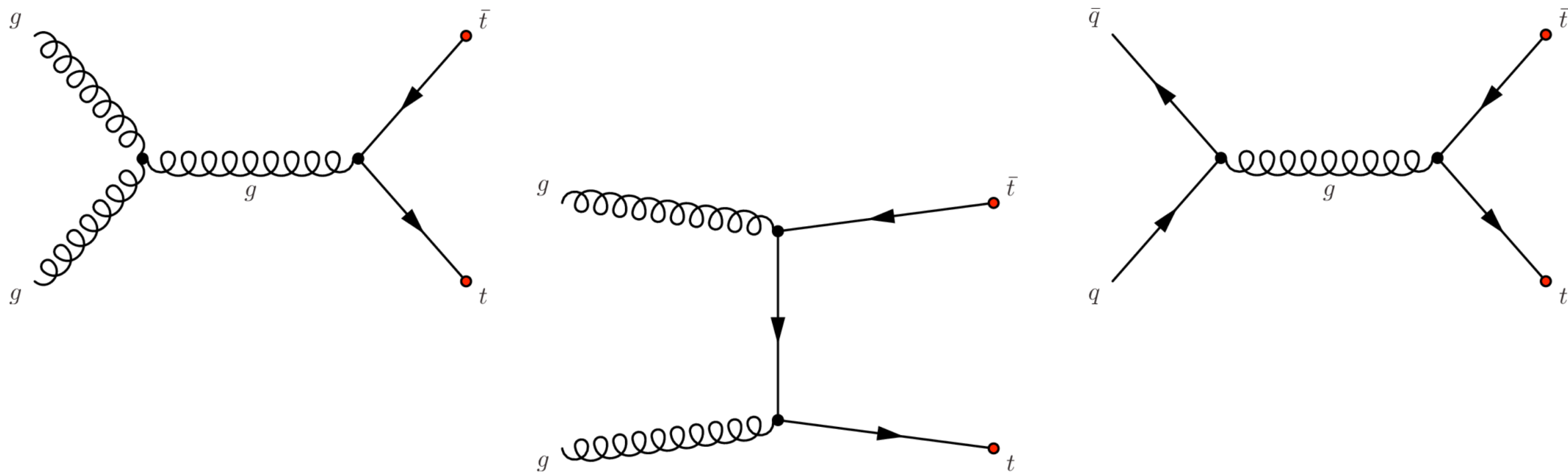
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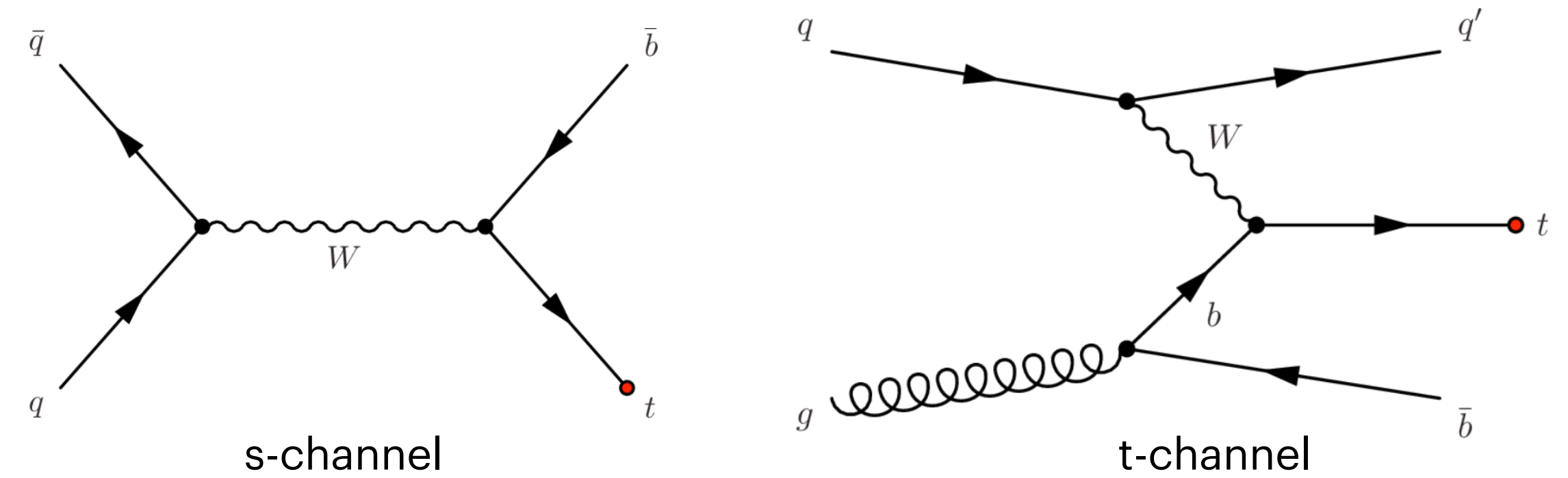
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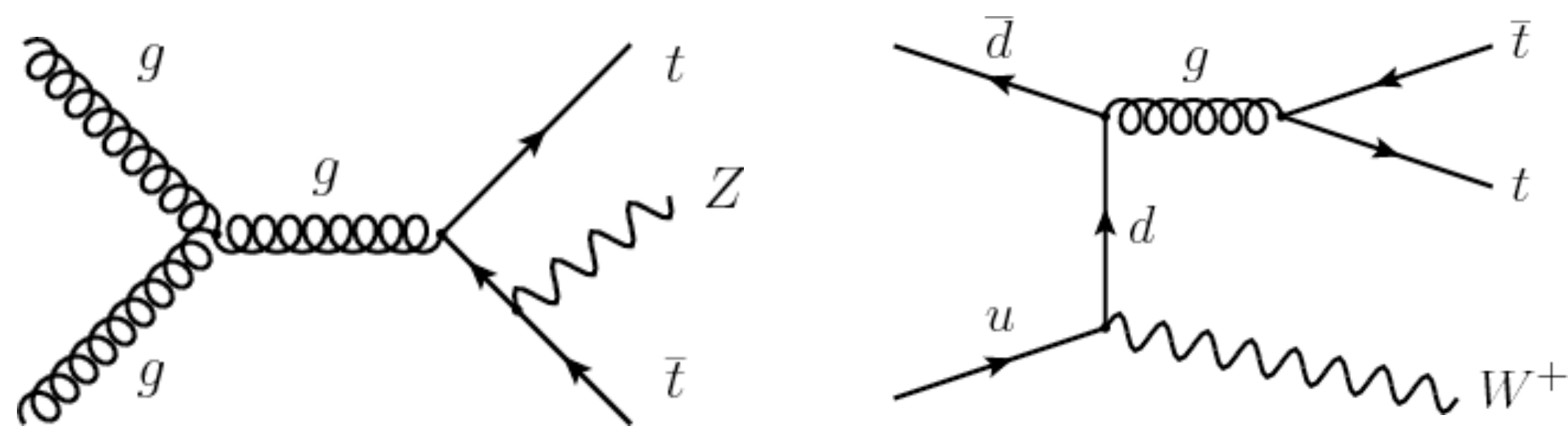
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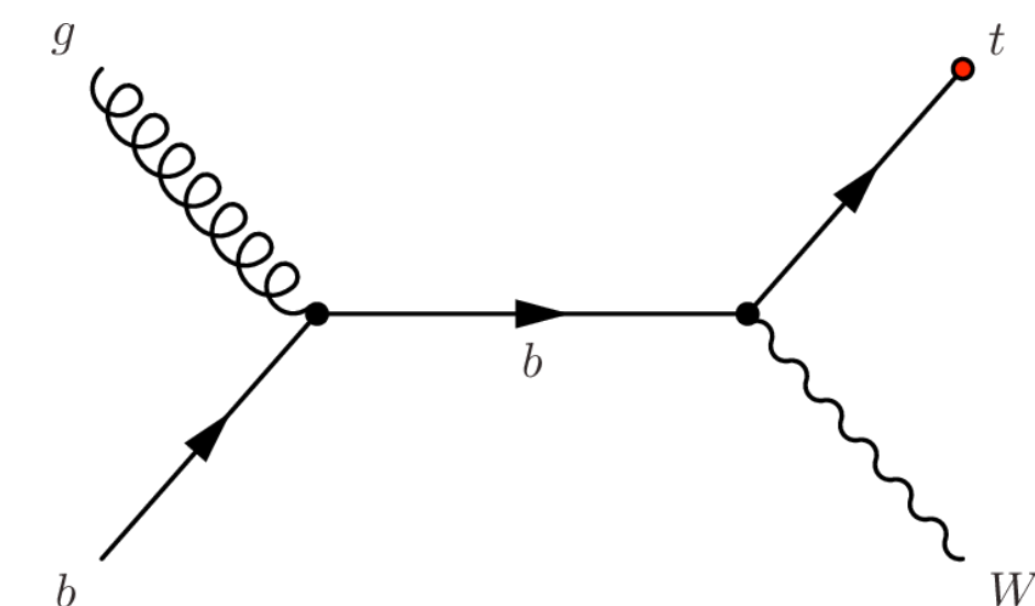
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four-fermion singlets

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four-fermion octets

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- 1. How do WC bounds compare between fixed PDF EFT-fits and simultaneous fits?**
- 2. How do PDFs compare between SM PDF fits and simultaneous PDF-EFT fits?**



# Fit settings

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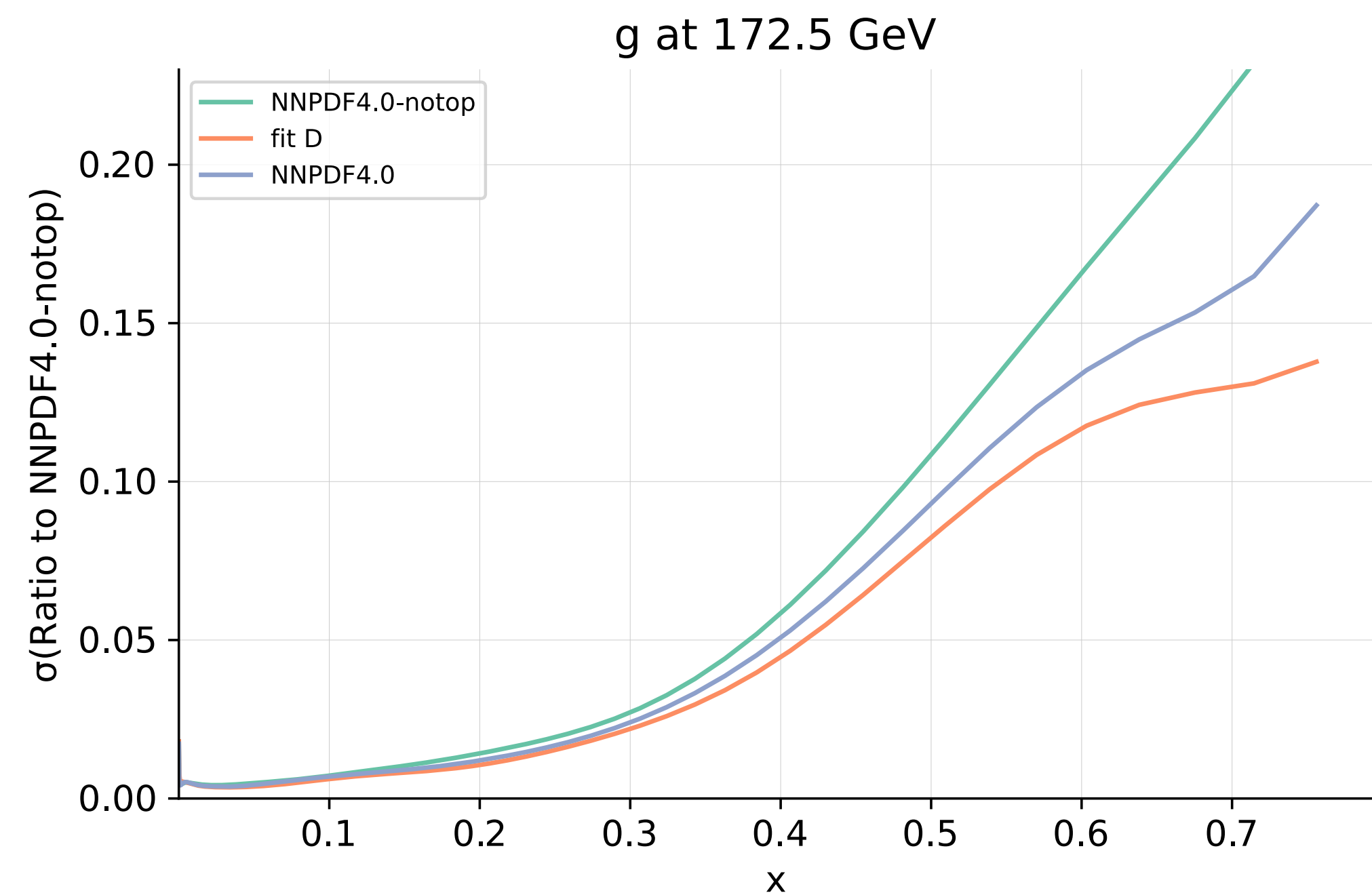
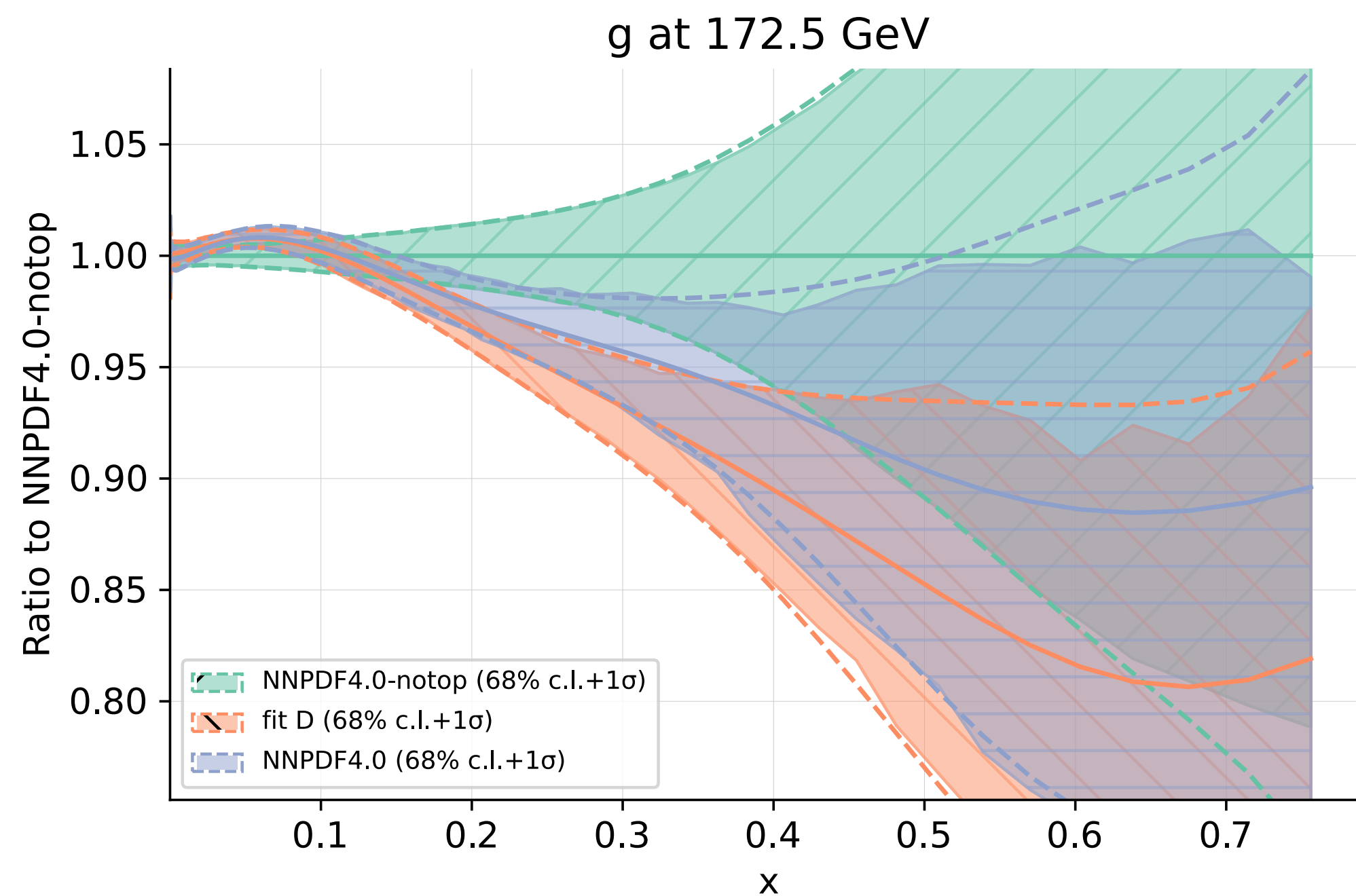


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- We work with theory predictions accurate to **NNLO in QCD in the SM**, and include **NLO QCD in the SMEFT**. Some fits are **linear in the SMEFT**, some are **quadratic** - a point we will return to.

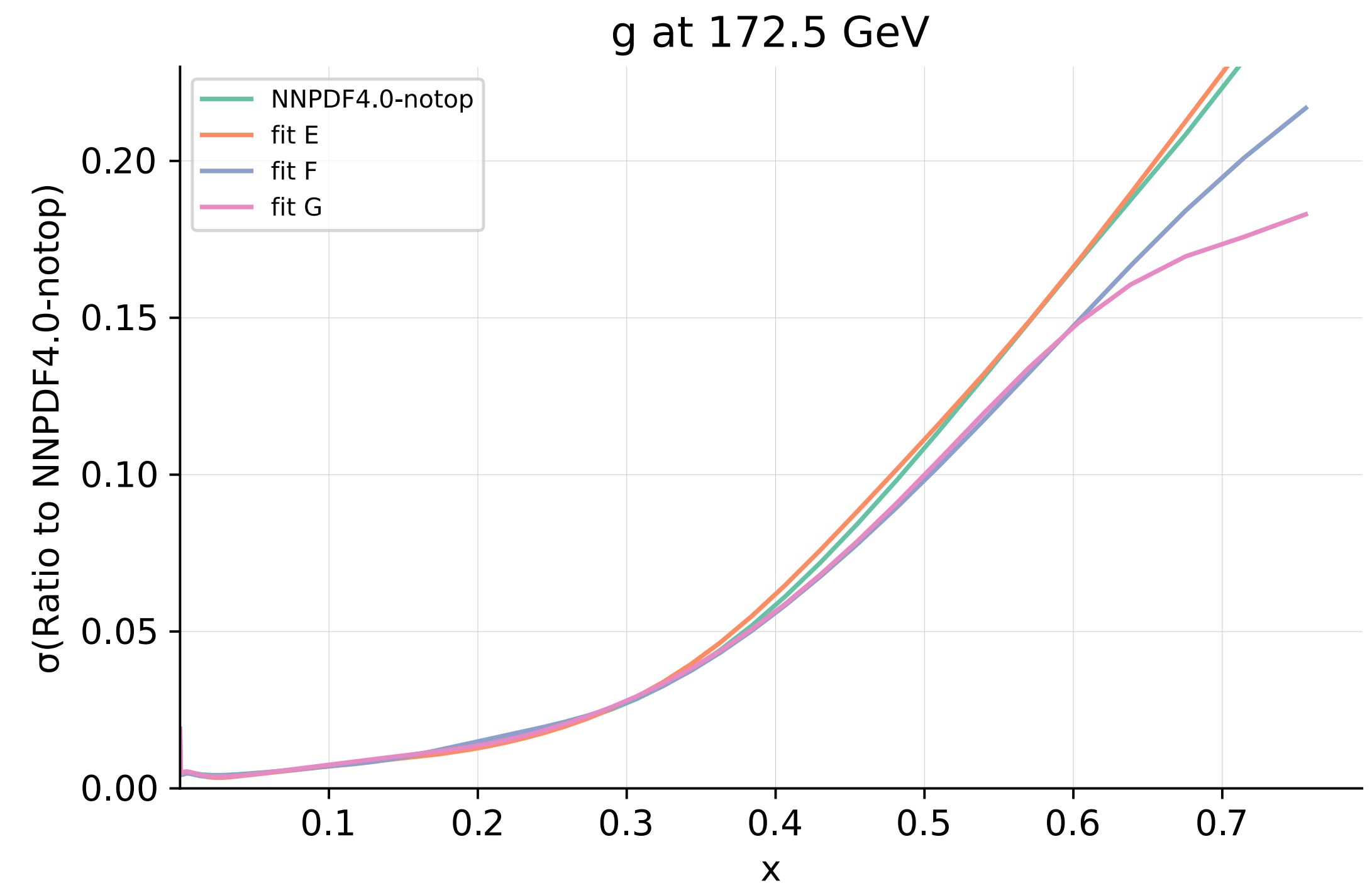
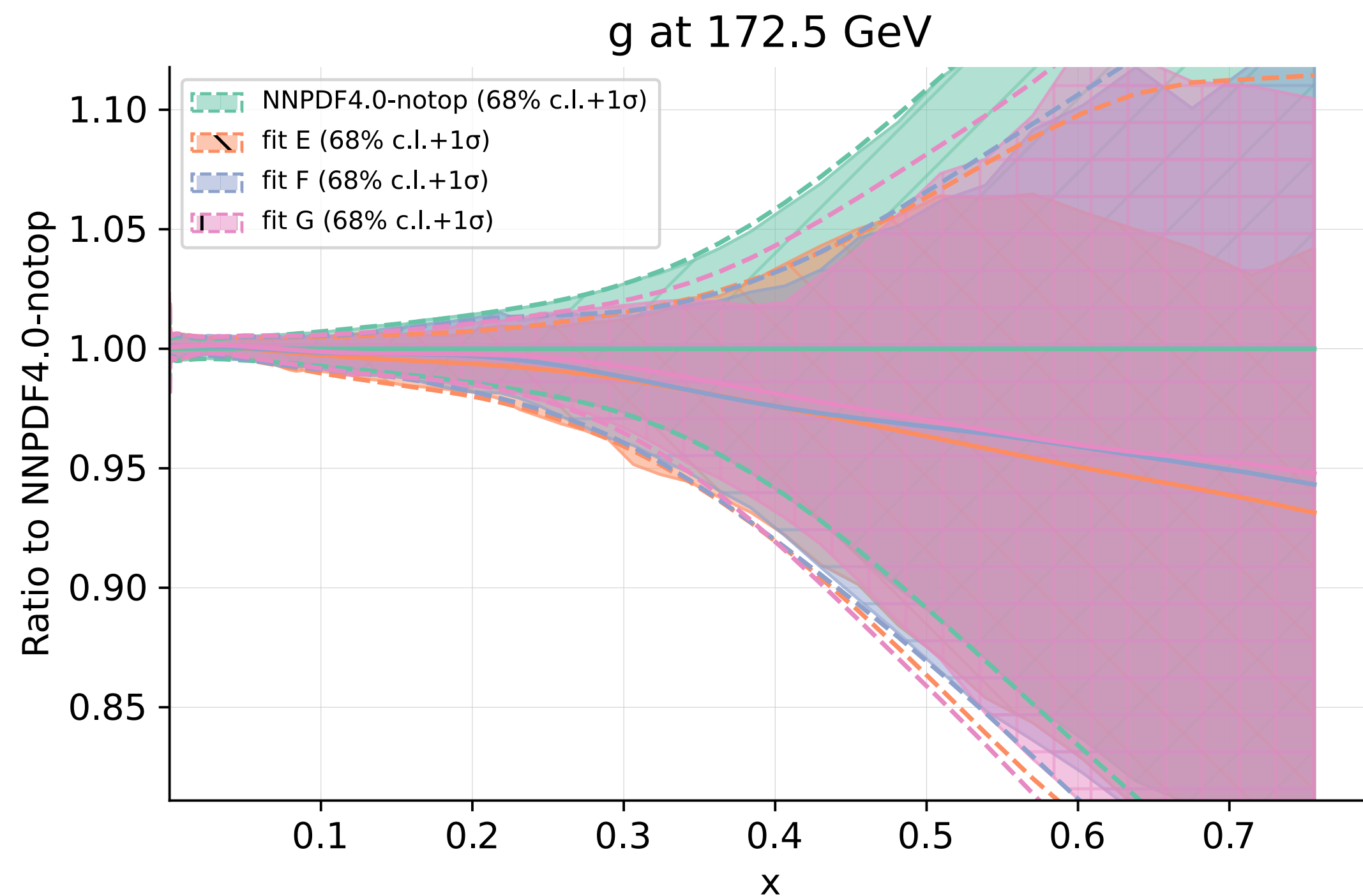
# PDFs in the SM - impact of inclusive $t\bar{t}$ and single-top

- First, we consider the impact of our dataset on PDFs **in the SM**.
- Begin by considering the updates to the **inclusive  $t\bar{t}$**  and **single-top** dataset relative to NNPDF4.0. If we perform a SM PDF fit using only our new inclusive  $t\bar{t}$  and single-top data, we see a more pronounced effect on the **large- $x$  gluon** relative to NNPDF4.0. The **uncertainty** is also **further reduced**.



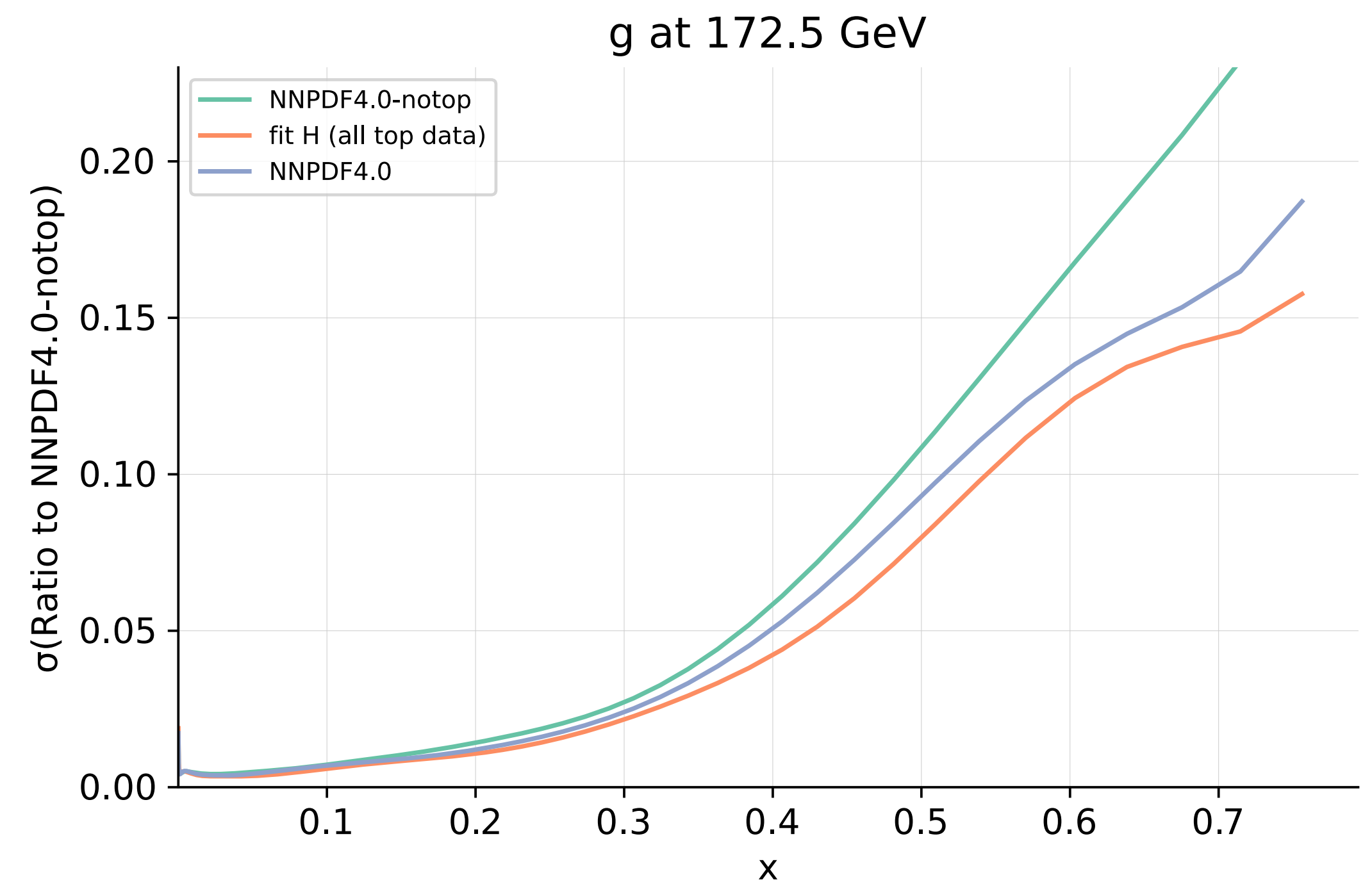
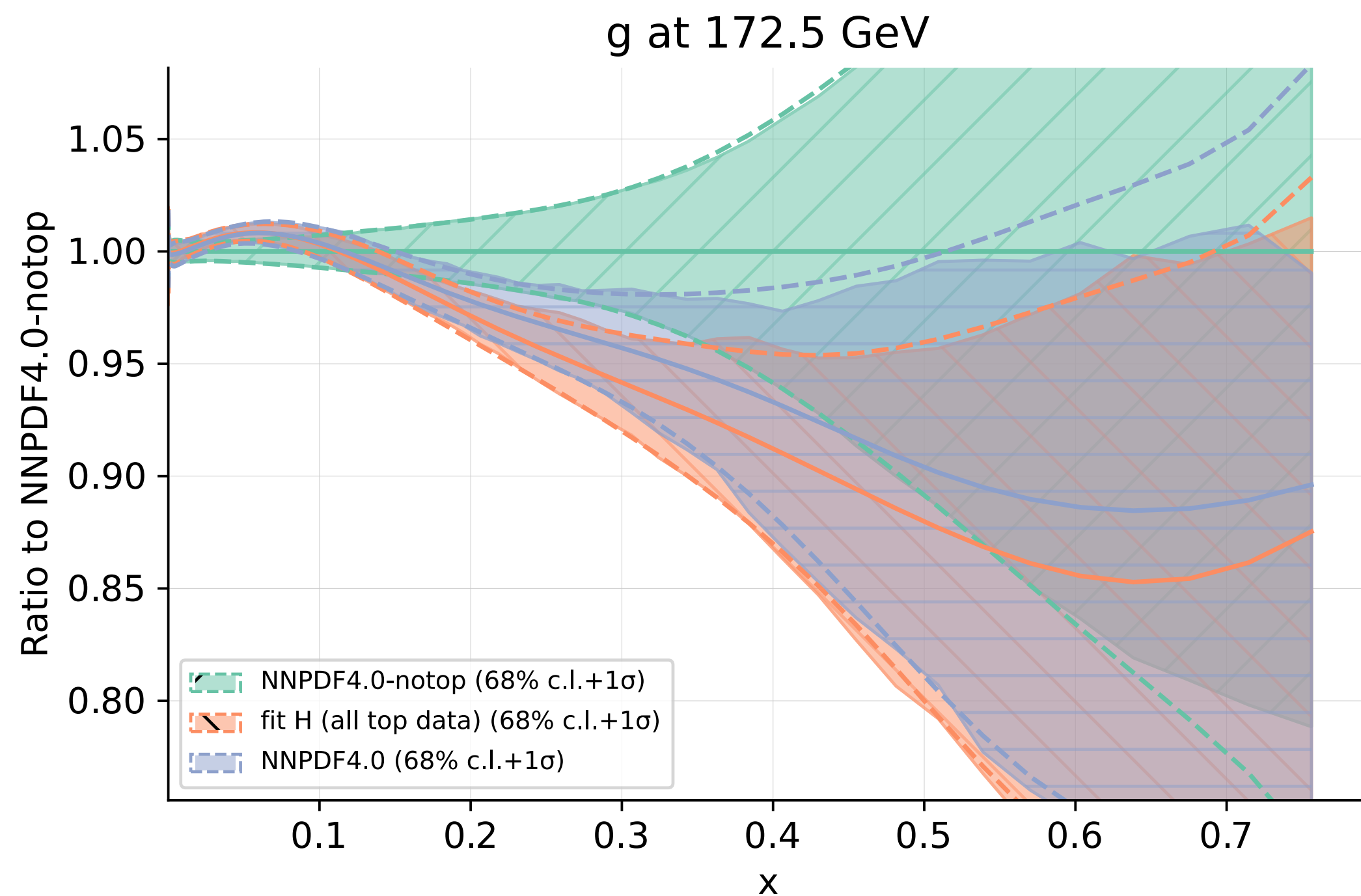
# PDFs in the SM - impact of associated top

- Next, for the first time we consider the impact of **associated top data** in a PDF fit. There is only a very mild effect on the central value of the gluon, reducing it at large- $x$ , and fractionally reducing uncertainty.



# PDFs in the SM - impact of all new top data

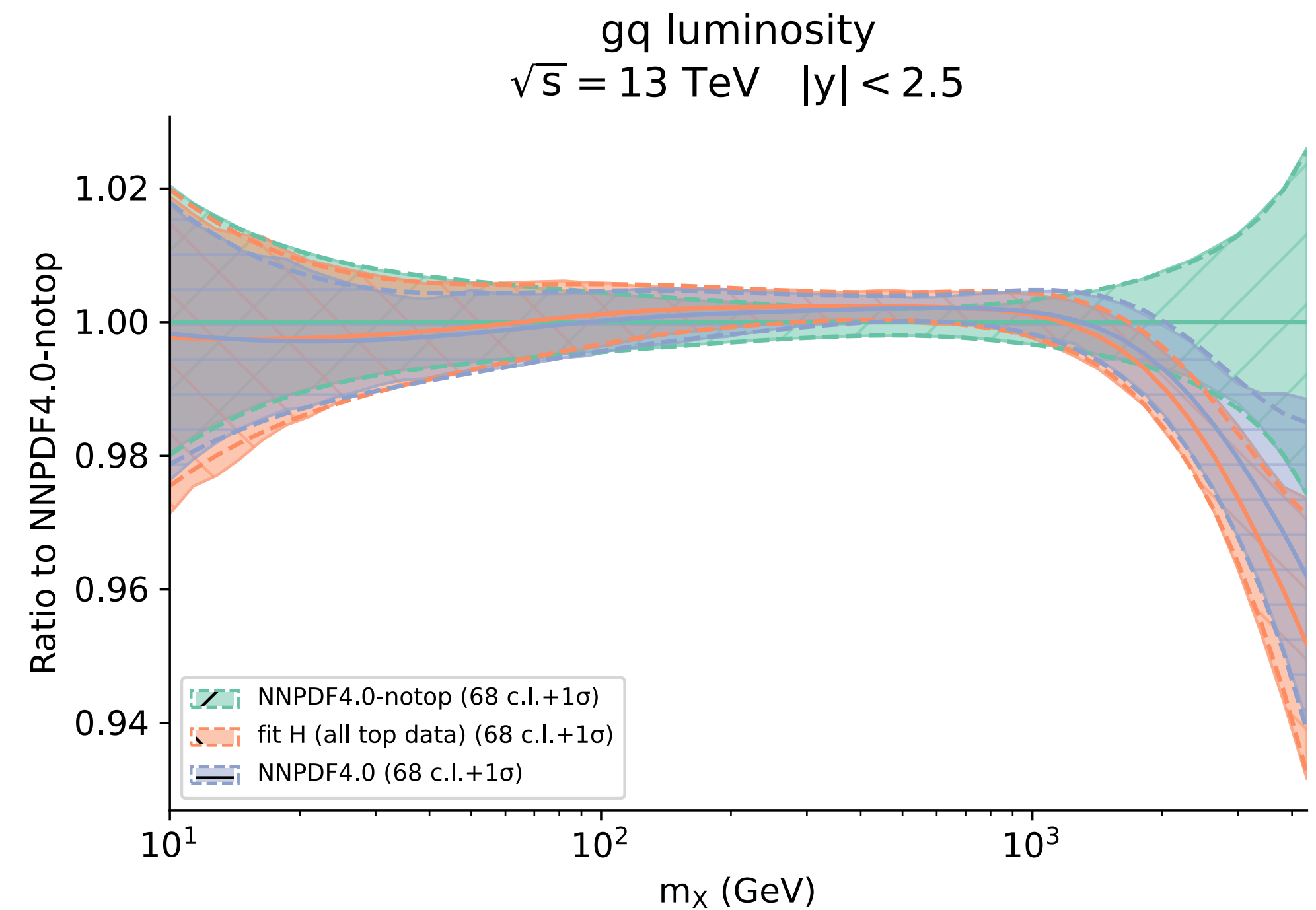
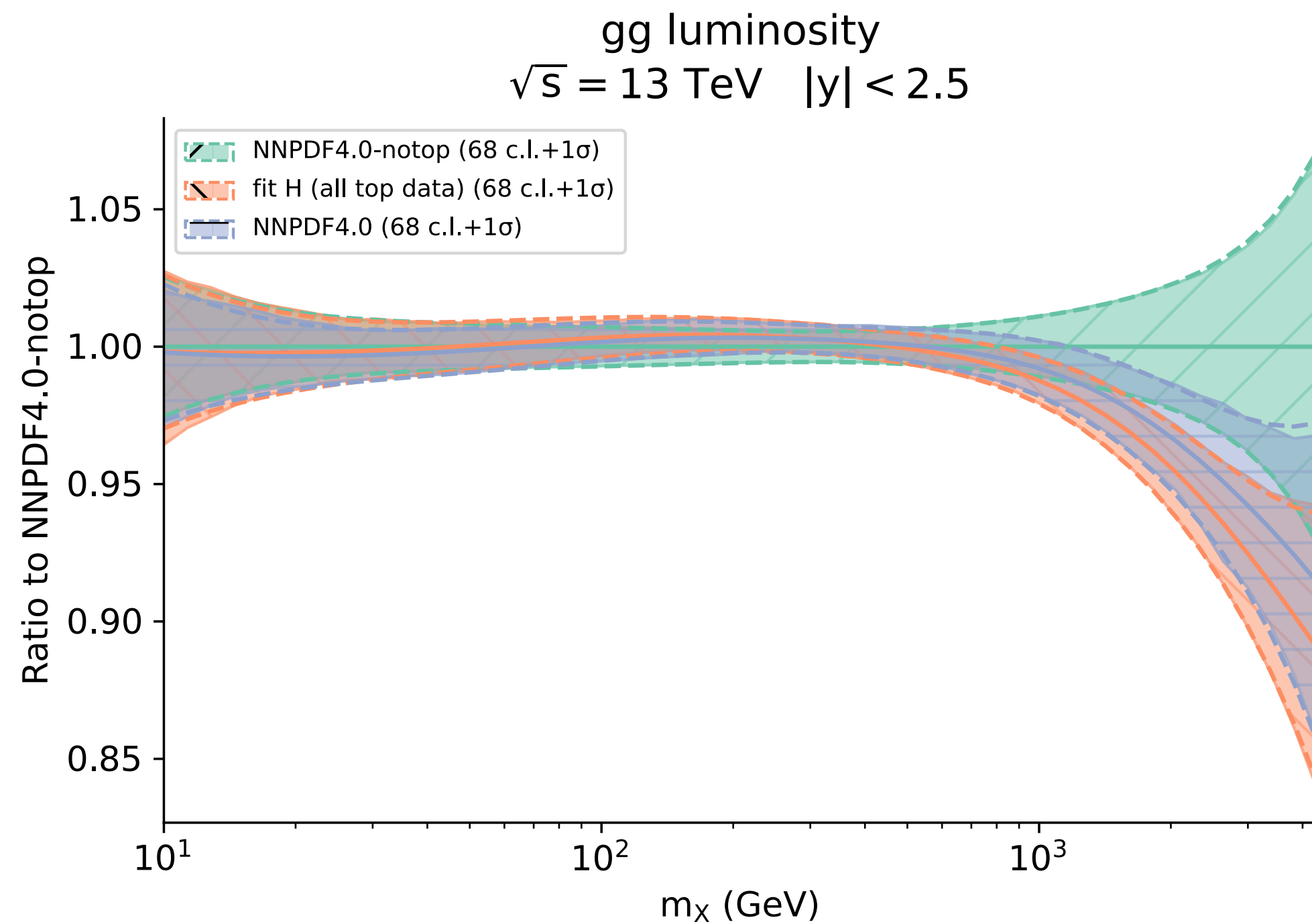
- Finally, we present the results of a **complete PDF fit** including **all our new top data**. As expected, the effect on the large- $x$  gluon is broadly the same as the effect of just including the inclusive  $t\bar{t}$  and single-top data, but is mildly tempered by the associated top data.





# PDFs in the SM - impact of all new top data

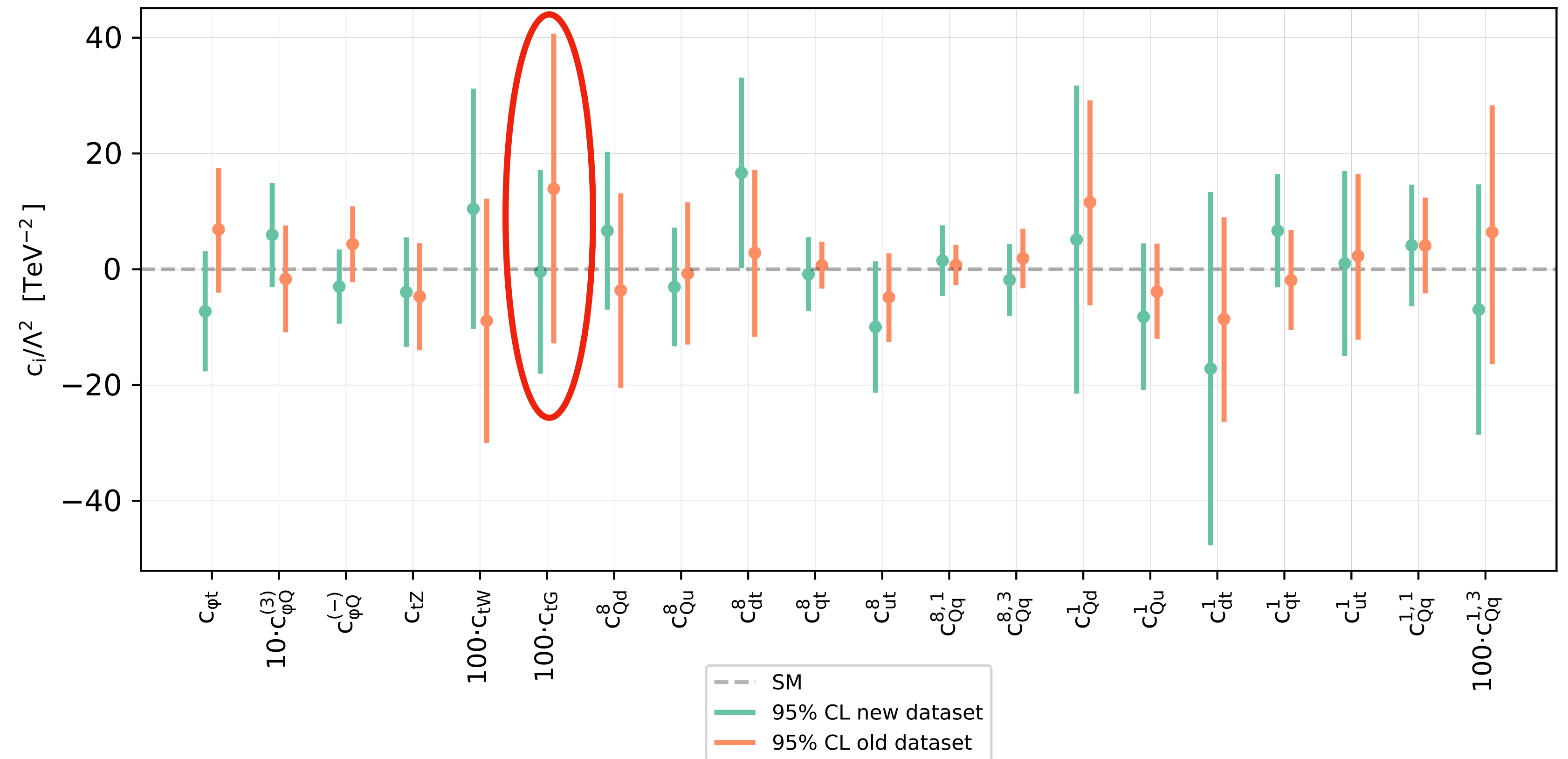
- A similar trend holds for the **PDF luminosities**, with our new updated fit compatible with NNPDF4.0, but with the central luminosity reduced relative to NNPDF4.0 at very large invariant mass.





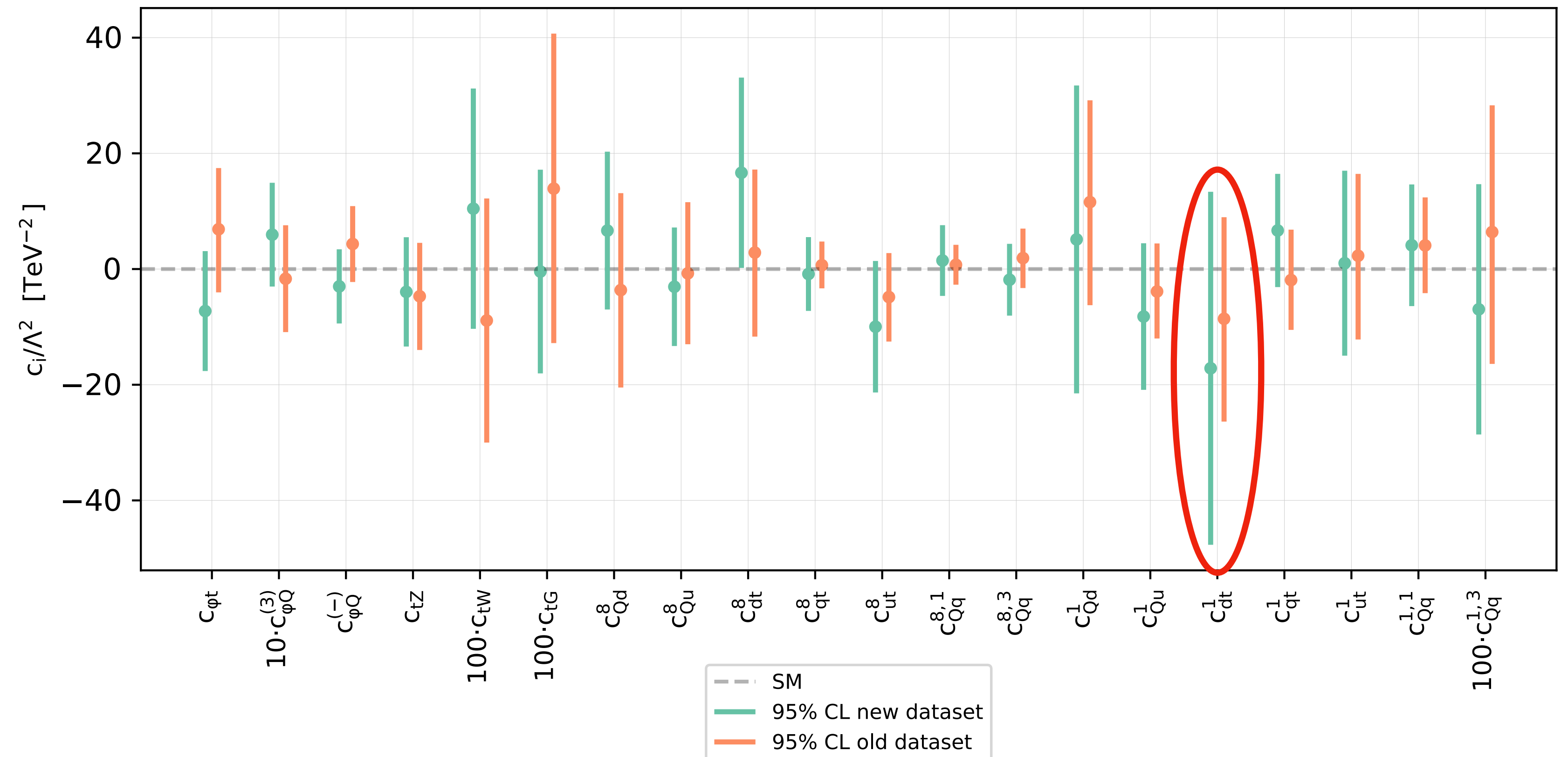
# SMEFT-only fits: linear SMEFT

- We have also performed SMEFT-only fits to see the impact of our new dataset relative to previous SMEFT-fits, namely **SMEFiT**.
- At the **linear level** in the SMEFT, best improvement is seen in  $c_{tG}$ , whose bound undergoes a 35% tightening - this is traced to more precise total  $t\bar{t}$  measurements.



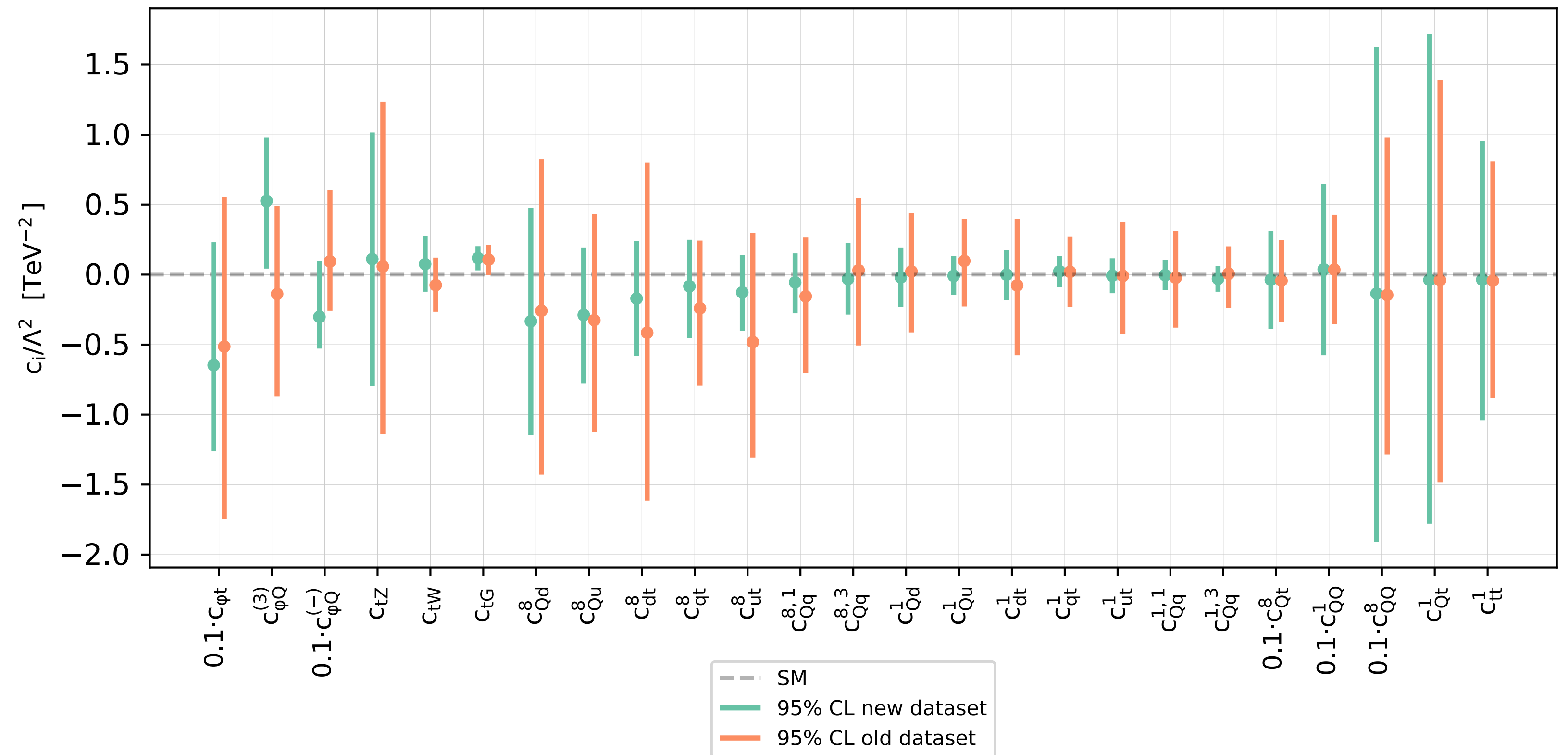
# SMEFT-only fits: linear SMEFT

- Some other coefficients undergo a **shift in the central value**, but no tightening or broadening of the constraint.
- Some coefficients have **broader bounds** than previously obtained, in particular some of the four-fermion operators.
- However, bounds are very weak here anyway, and likely challenge EFT validity.



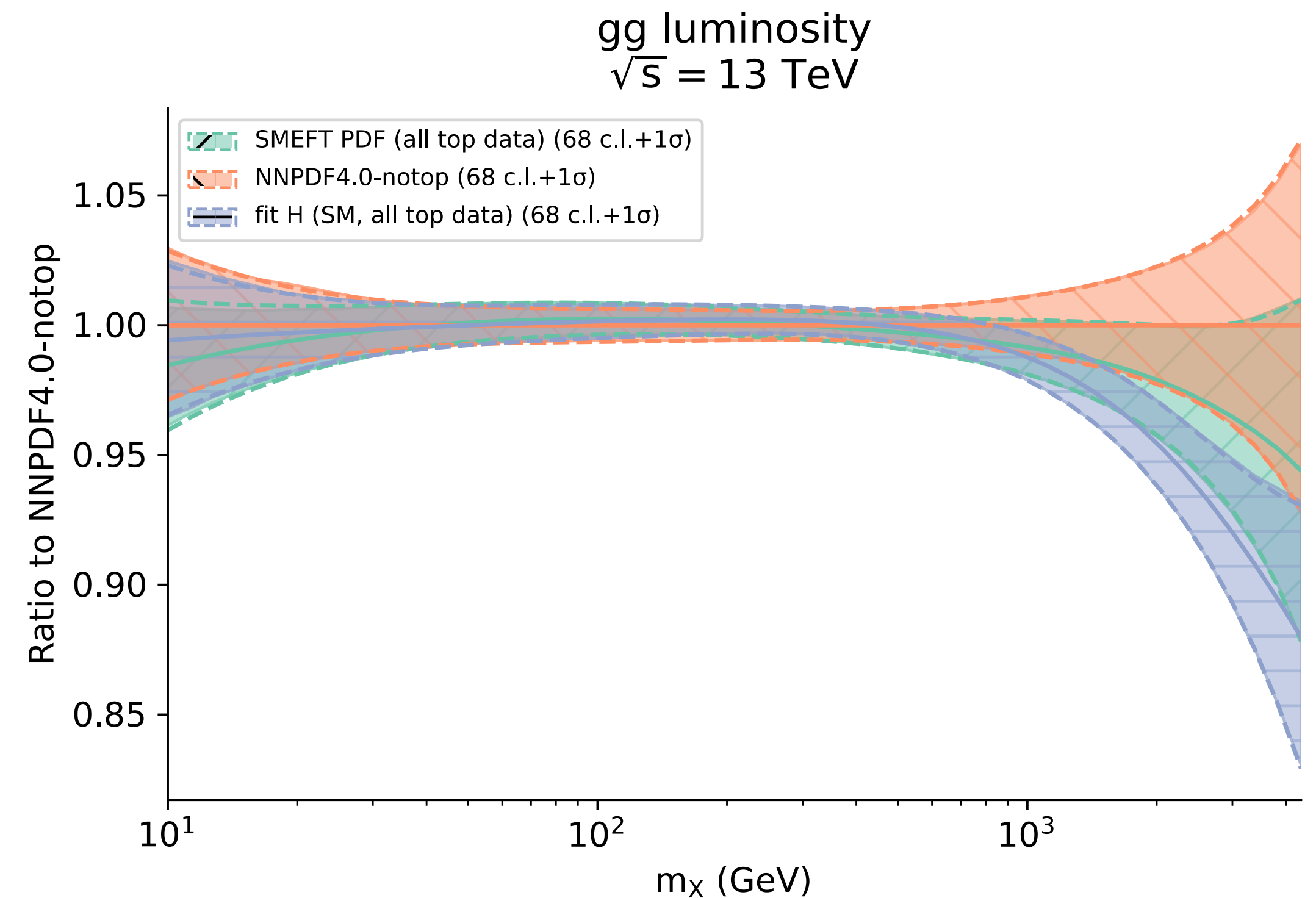
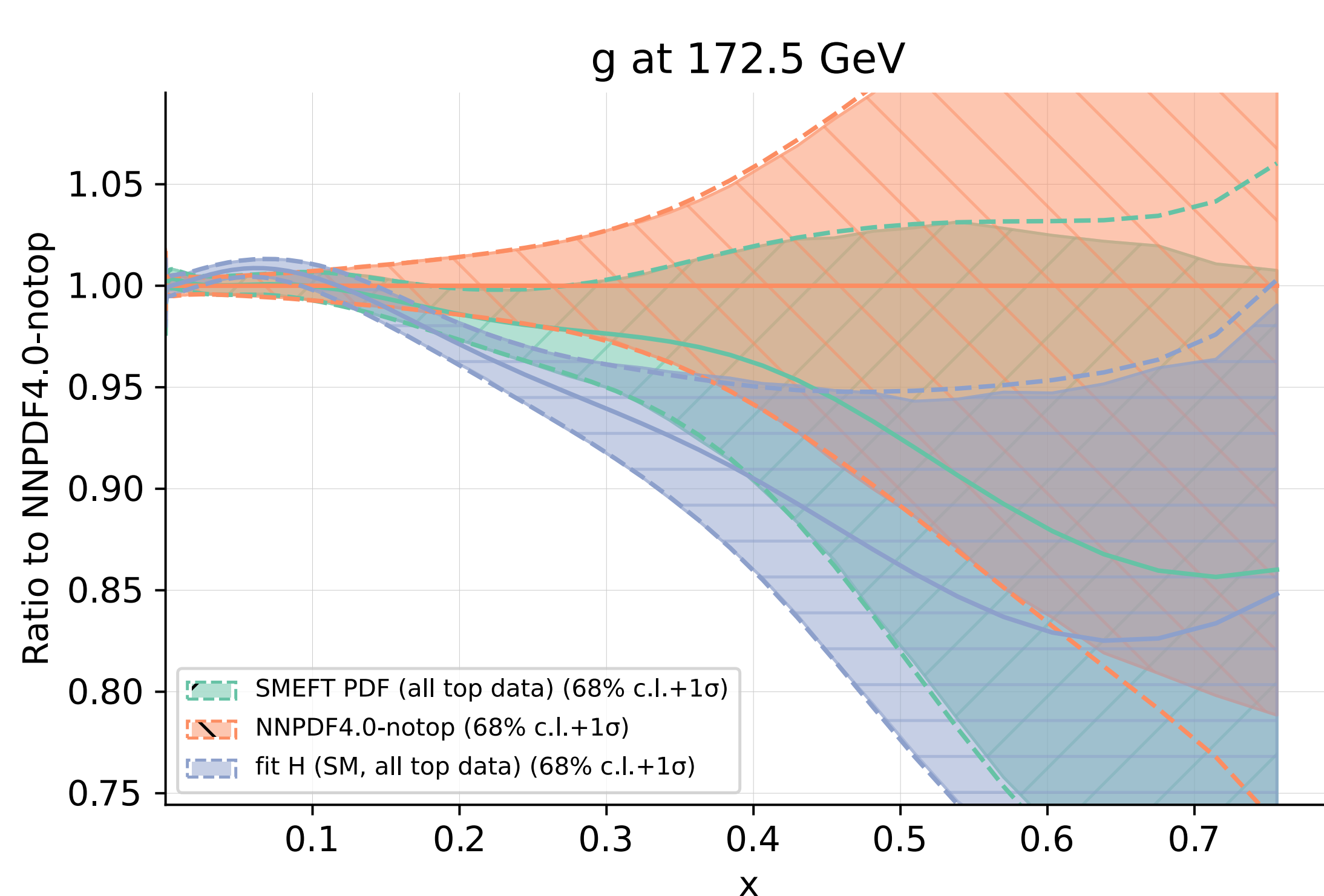
# SMEFT-only fits: quadratic SMEFT

- Results are **much more promising** when **quadratic SMEFT effects** are included. A **significant tightening** of bounds is seen for most operators.
- Only the five **four-heavy operators** experience broadening relative to the old dataset. This could point to some inconsistency in the  $t\bar{t}t\bar{t}$  and  $t\bar{t}b\bar{b}$  data, but with such large uncertainties, it is difficult to be precise.



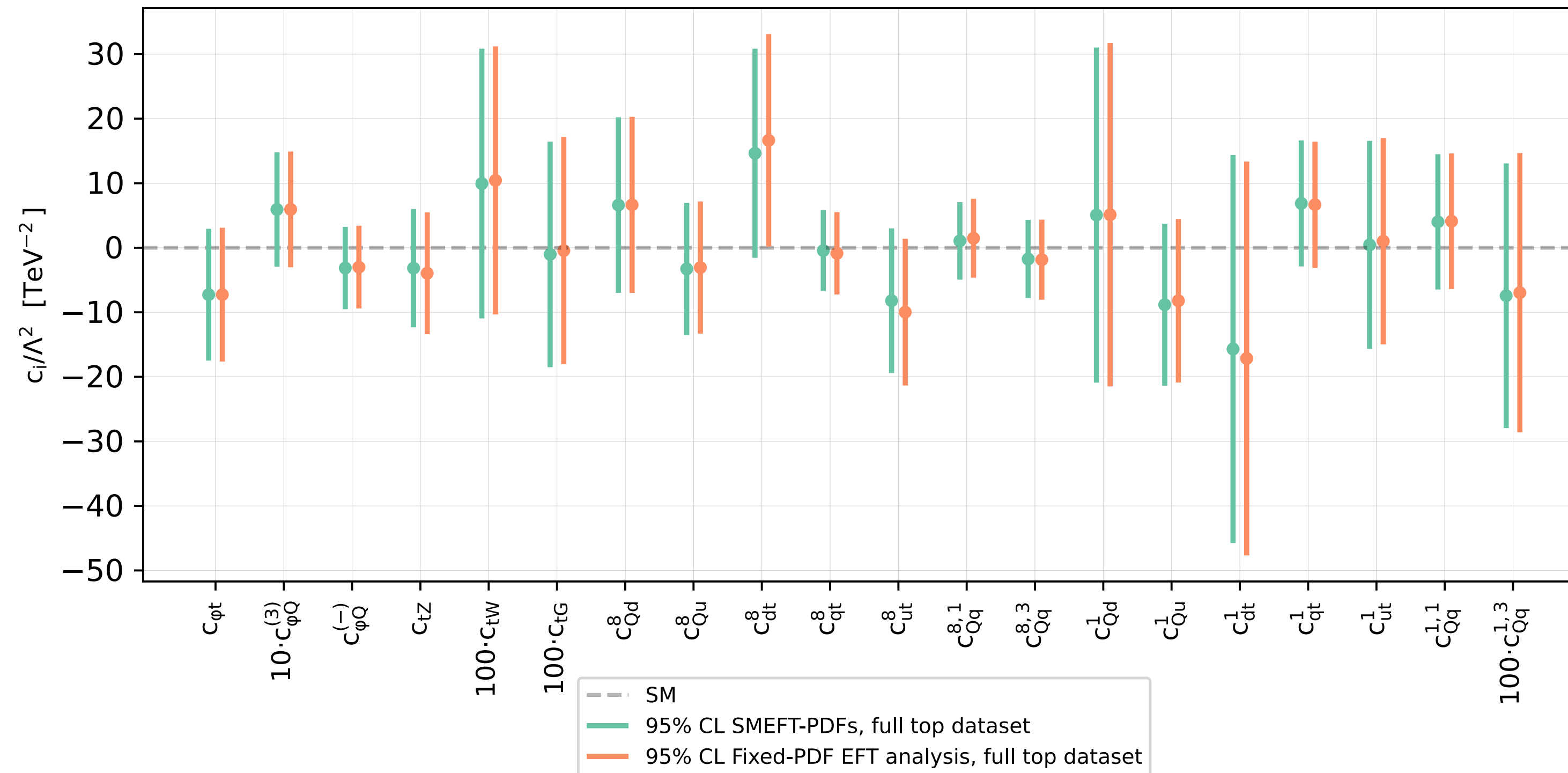
# Joint PDF-SMEFT fits: linear SMEFT

- Finally, we present the key result of the work: a **simultaneous** determination of PDFs and SMEFT Wilson coefficients. We start assuming **linear SMEFT**.
- In terms of the gluon PDFs and luminosities, we find that a simultaneous determination **reduces the pull** of the top data from the **non-top baseline**.



# Joint PDF-SMEFT fits: linear SMEFT

- On the other hand, we find that the bounds on the Wilson coefficients are **very stable** between a simultaneous PDF-SMEFT fit and a SMEFT-only fit.



- This indicates that within a **linear EFT interpretation** of the top data, the PDF effects are **currently subdominant**.



# Joint PDF-SMEFT fits: quadratic SMEFT

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- The issue is such that quadratic results with the SIMUnet methodology (and indeed with any methodology that uses the Monte Carlo replica method) are **currently unreliable**.
- An **upcoming publication** will describe the issue in more detail; for now, here's the basics...

# Pitfalls of the Monte-Carlo replica method

- For simplicity, consider a single data point  $d$  with experimental variance  $\sigma^2$ , which we attempt to describe using the **quadratic** theory, involving a single theory parameter  $c$ :

$$t(c) = t^{\text{SM}} + t^{\text{lin}}_c + t^{\text{quad}}_c c^2$$

- The Monte-Carlo replica method propagates the uncertainty from the data to the theory parameter by fitting to **pseudodata**. We sample lots of pseudodata replicas from a normal distribution based on the data,  $d_p \sim N(d, \sigma^2)$ , and define the corresponding **parameter replicas** to be a random function of the pseudodata given by minimising the  $\chi^2$ -statistic:

$$c_p(d_p) = \arg \min_c \left( \frac{(t(c) - d_p)^2}{\sigma^2} \right)$$



# Pitfalls of the Monte-Carlo replica method

- In this very simple example, one can compute the distribution function of the parameter replicas analytically; it is given by:

$$P_{c^{(i)}}(c) \propto \delta\left(c + \frac{t^{\text{lin}}}{2t^{\text{quad}}}\right) \int_{-\infty}^{t_{\text{min}}} dx \exp\left(-\frac{1}{2\sigma^2}(x-d)^2\right) + \frac{2}{|2ct^{\text{quad}} + t^{\text{lin}}|} \exp\left(-\frac{1}{2\sigma^2}(d-t(c))^2\right)$$

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- **Key features to note:**
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  - There is also a **delta function spike** in the distribution - interesting to ask: why...?

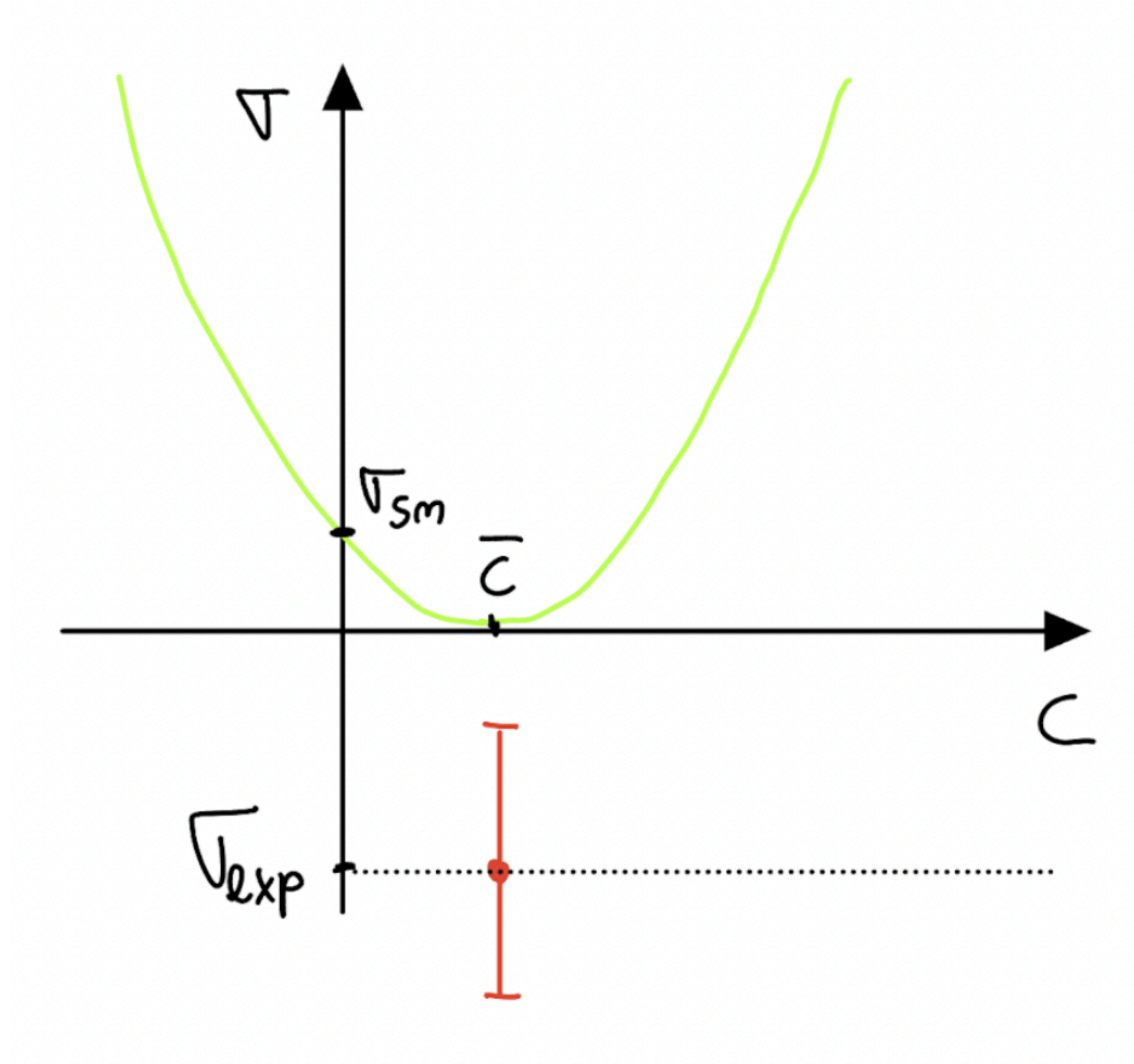
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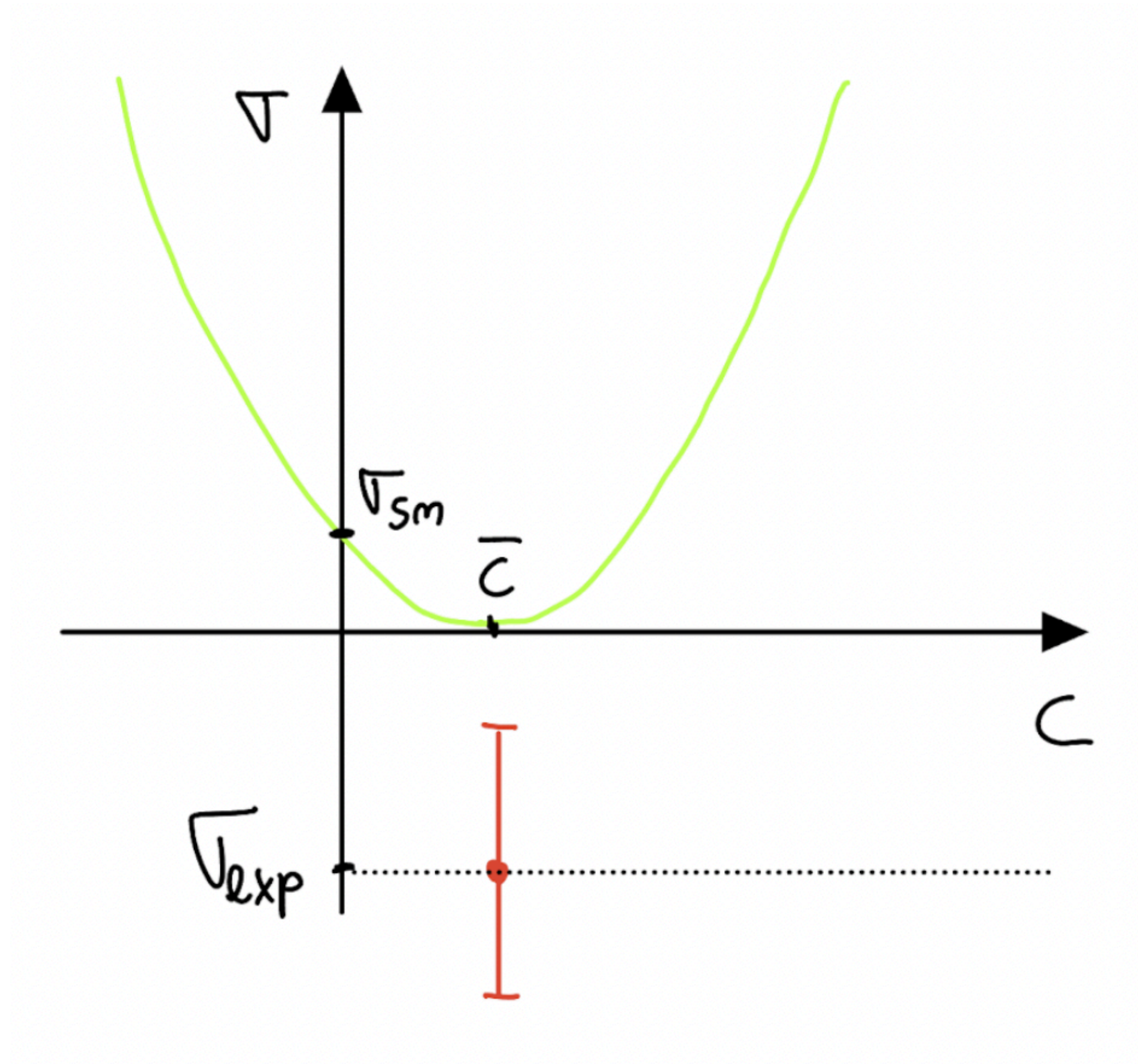
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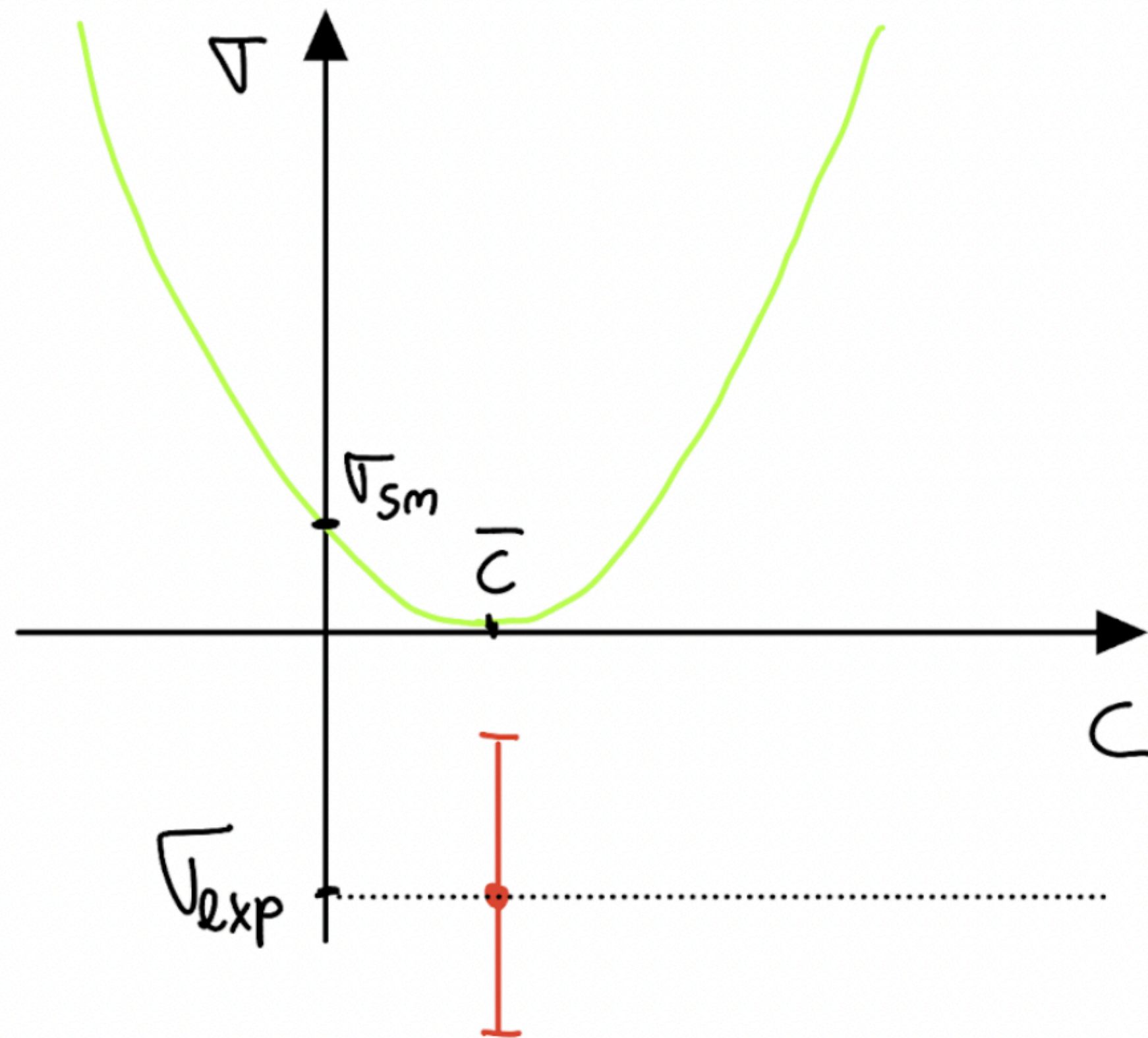
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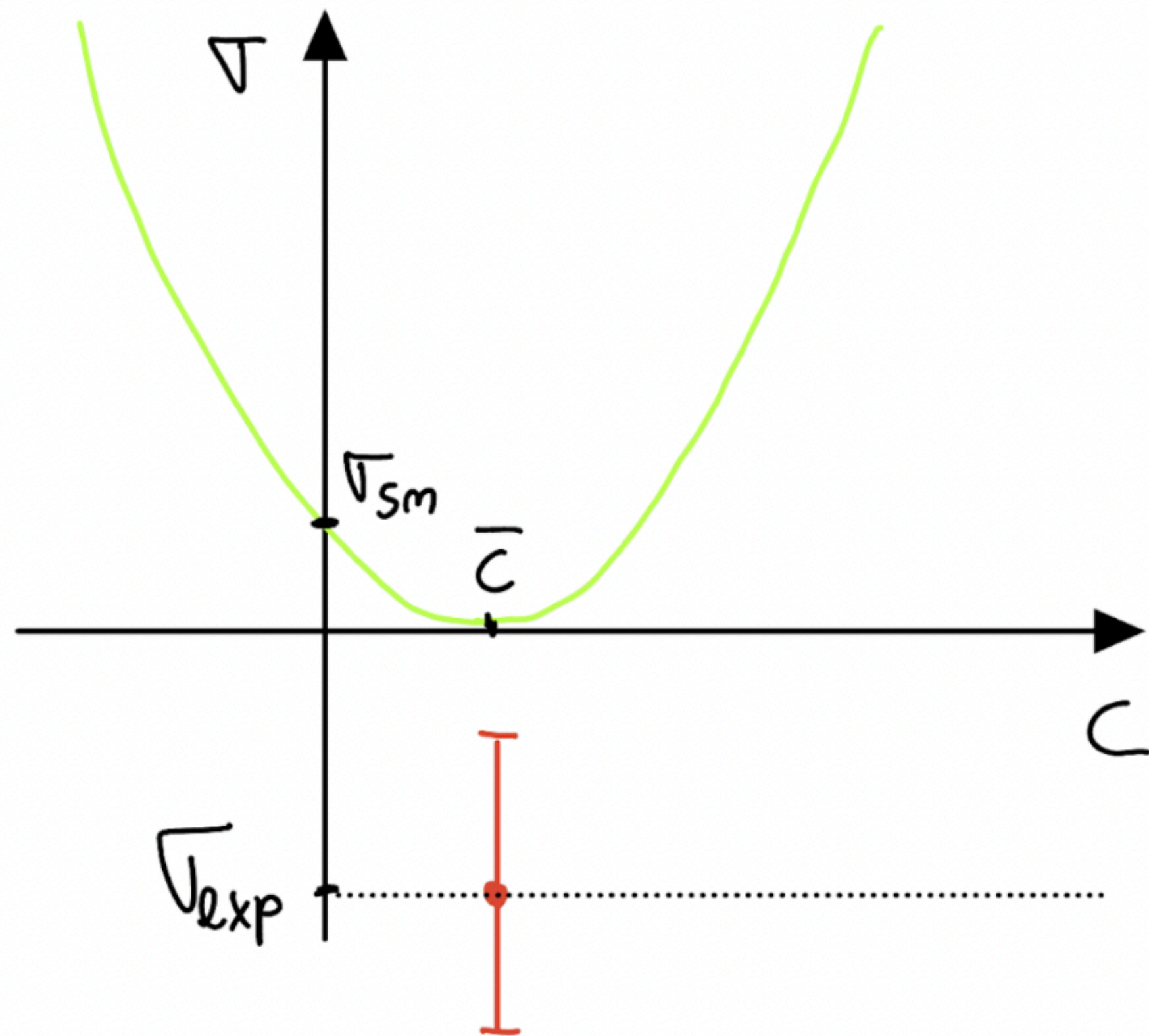


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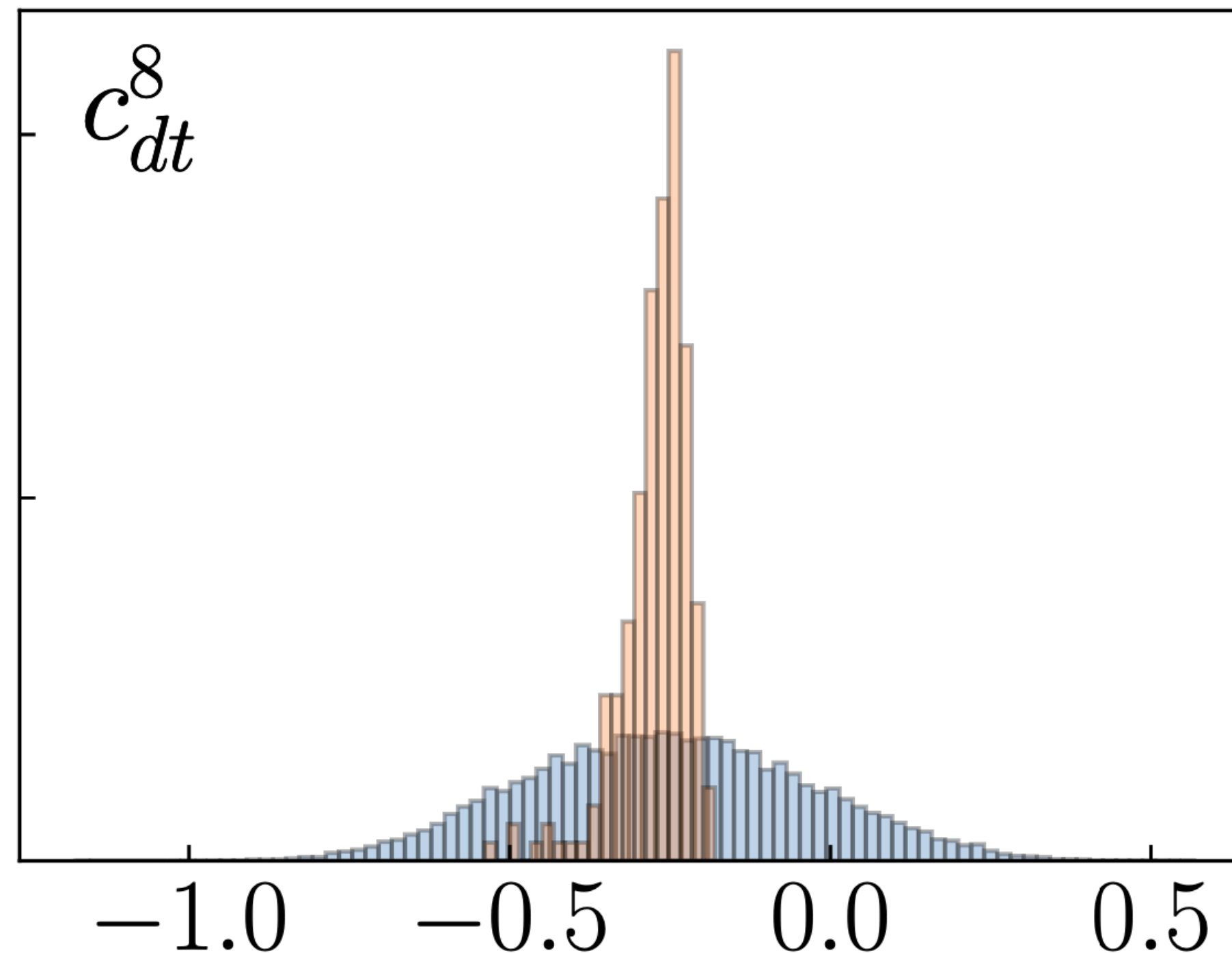
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- Any pseudodata replica that falls below the minimum results in the **same parameter replica**, corresponding to the parameter value that gives the minimum.
- This gives rise to the spike in the distribution at  $c = -t^{\text{lin}}/2t^{\text{quad}}$ .

# Pitfalls of the Monte-Carlo replica method

- These problems extend to our top fit... for example in a **realistic quadratic fit** of one operator  $c_{dt}^8$ , we get the following comparison between the Monte-Carlo method (**orange**) and a Bayesian method with uniform prior (**blue**).
- We see that **Monte-Carlo massively underestimates uncertainties.**





## **Key questions for the future:**

**Can the MC replica method be modified to agree with Bayesian methods?**

**To what extent do existing fits (in the SMEFT world, PDF world, and beyond) that use the MC replica method underestimate uncertainties?**

# 6. - The dark side of the proton

***Based on 2203.12628***

# Light new physics and PDFs

- So far, we've focussed on **joint PDF-SMEFT determinations**. However, whilst the SMEFT is a great tool in searching for New Physics, it does not capture **new weakly-coupled, light particles**. Proton structure could also be affected by these new degrees of freedom!

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- In this case, we could **still see the impact on proton structure** by including the new particles as **constituents of the proton**.
- The idea is not too far-fetched! The inclusion of new **coloured** particles, e.g. **gluinos**, has already been studied by Berger et al. in 0406143 (from 2005) and 1010.4315 (from 2010). **Strong constraints** can be derived assuming that new coloured particles alter our SM view of proton structure.



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- *Idea:* now PDFs are known **very precisely**, and their uncertainties **will continue to reduce in the near future with the HL-LHC**, could we do the same for a **colourless** particle too?

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- **Low-energy experimental probes** already strongly constrain  $m_B < 2$  GeV.
- We also treat this as an effective theory, valid up to the mass of the  $Z$ , where **kinetic mixing** effects become important; so for us:  $m_B \in [2, 80]$  GeV.

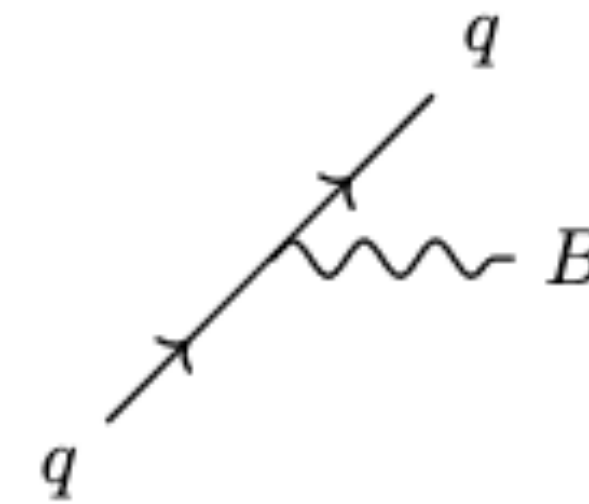
# DGLAP in the presence of dark photons

- Now, to include the dark photon as a constituent of the proton, we mimic the earliest studies into **photon PDFs** (namely MRST 0411040, from 2004), using the following procedure:

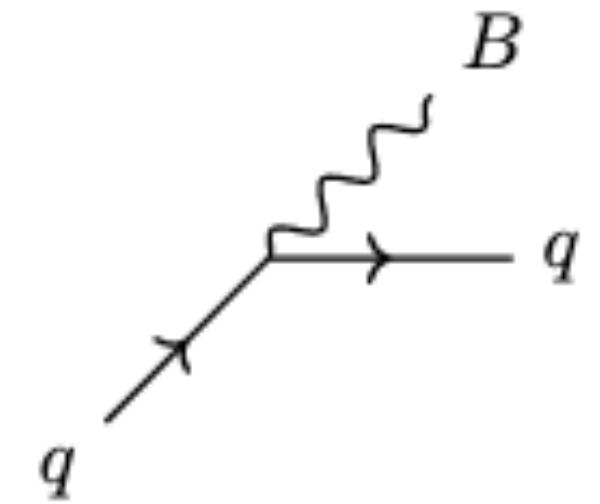


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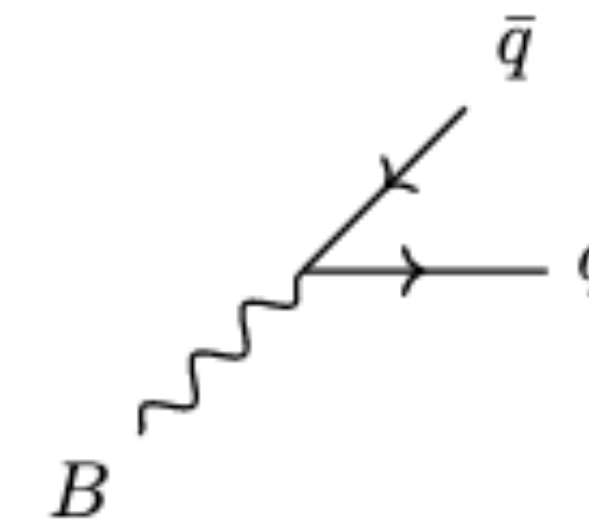
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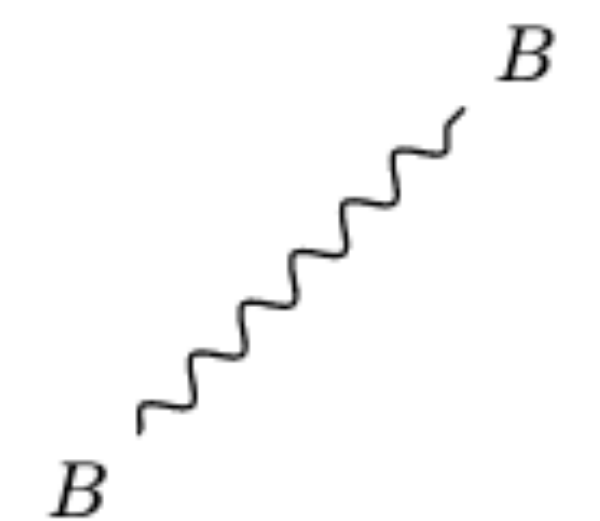
$$P_{qq}(x) = \frac{1+x^2}{9(1-x)_+} + \frac{1}{6}\delta(1-x)$$



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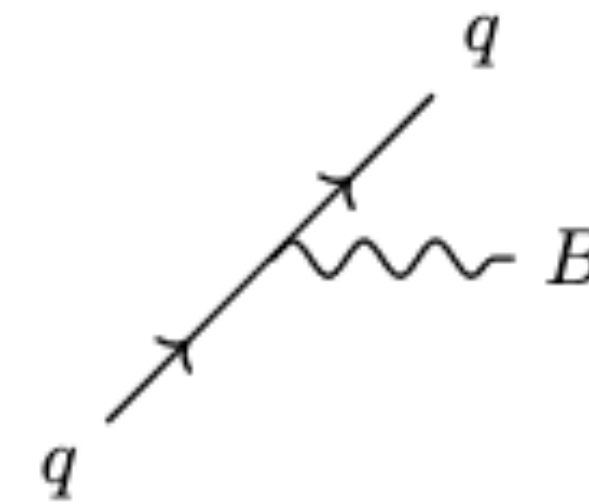
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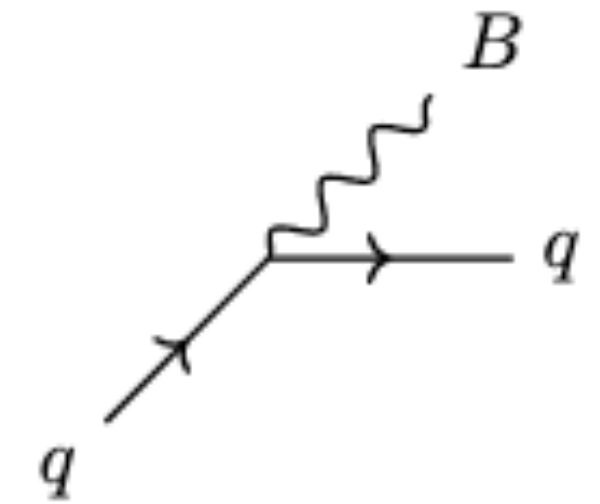
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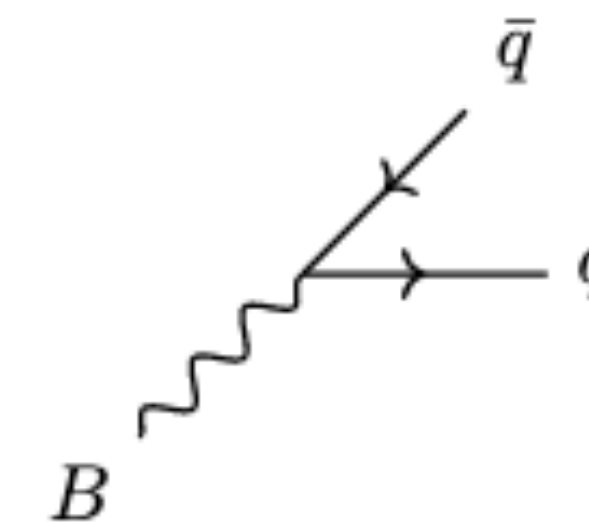
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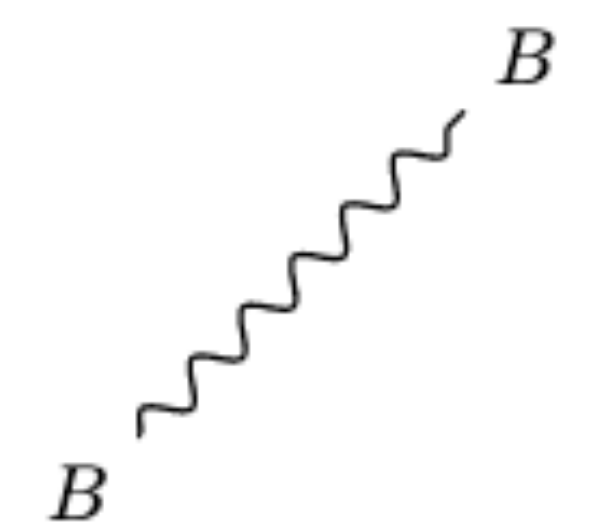
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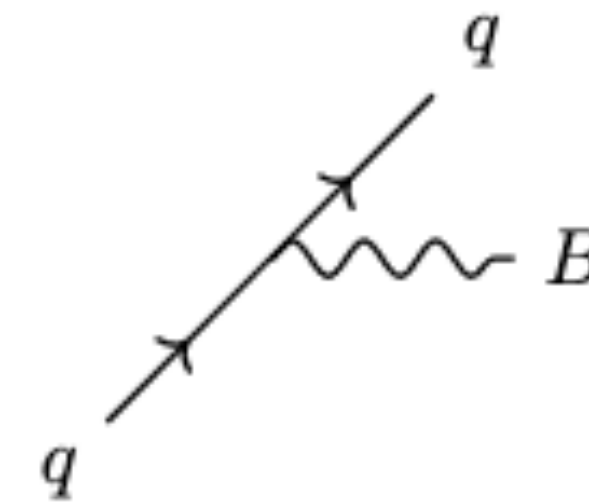
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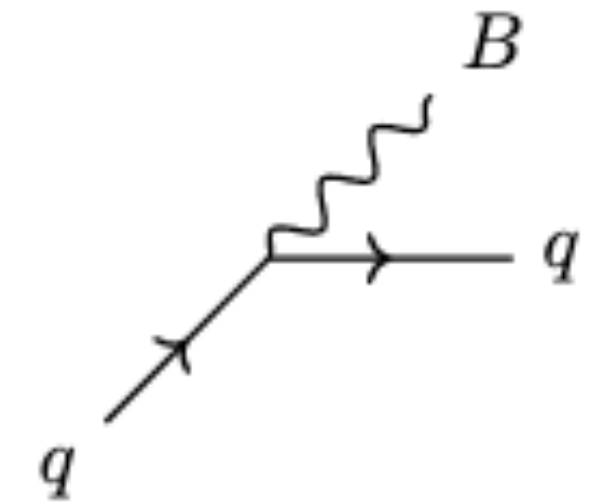
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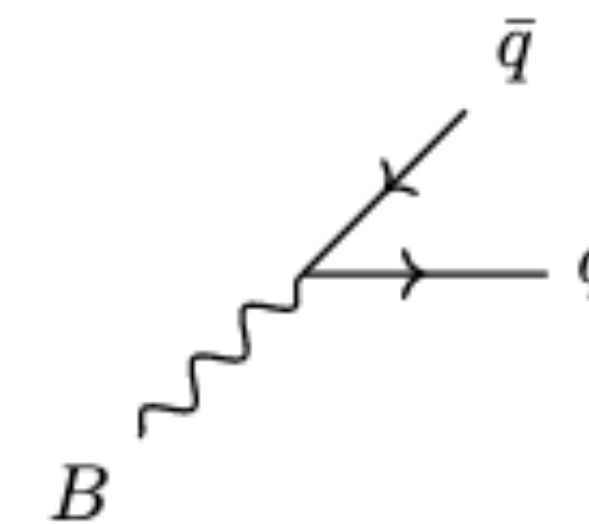
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  3. Compare resulting PDF set predictions with reference SM predictions to see **impact of inclusion of a dark photon**.



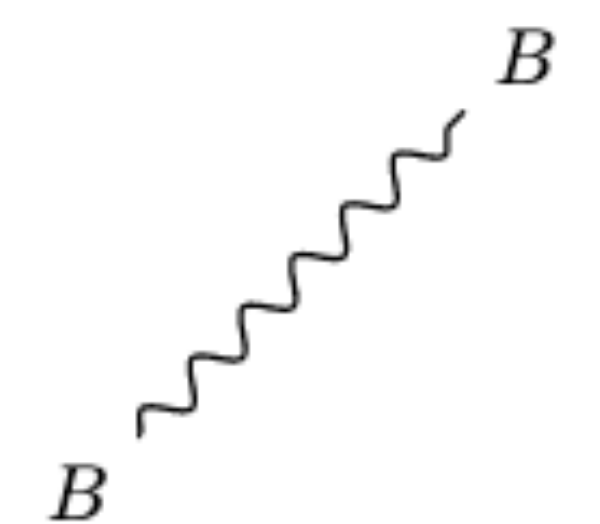
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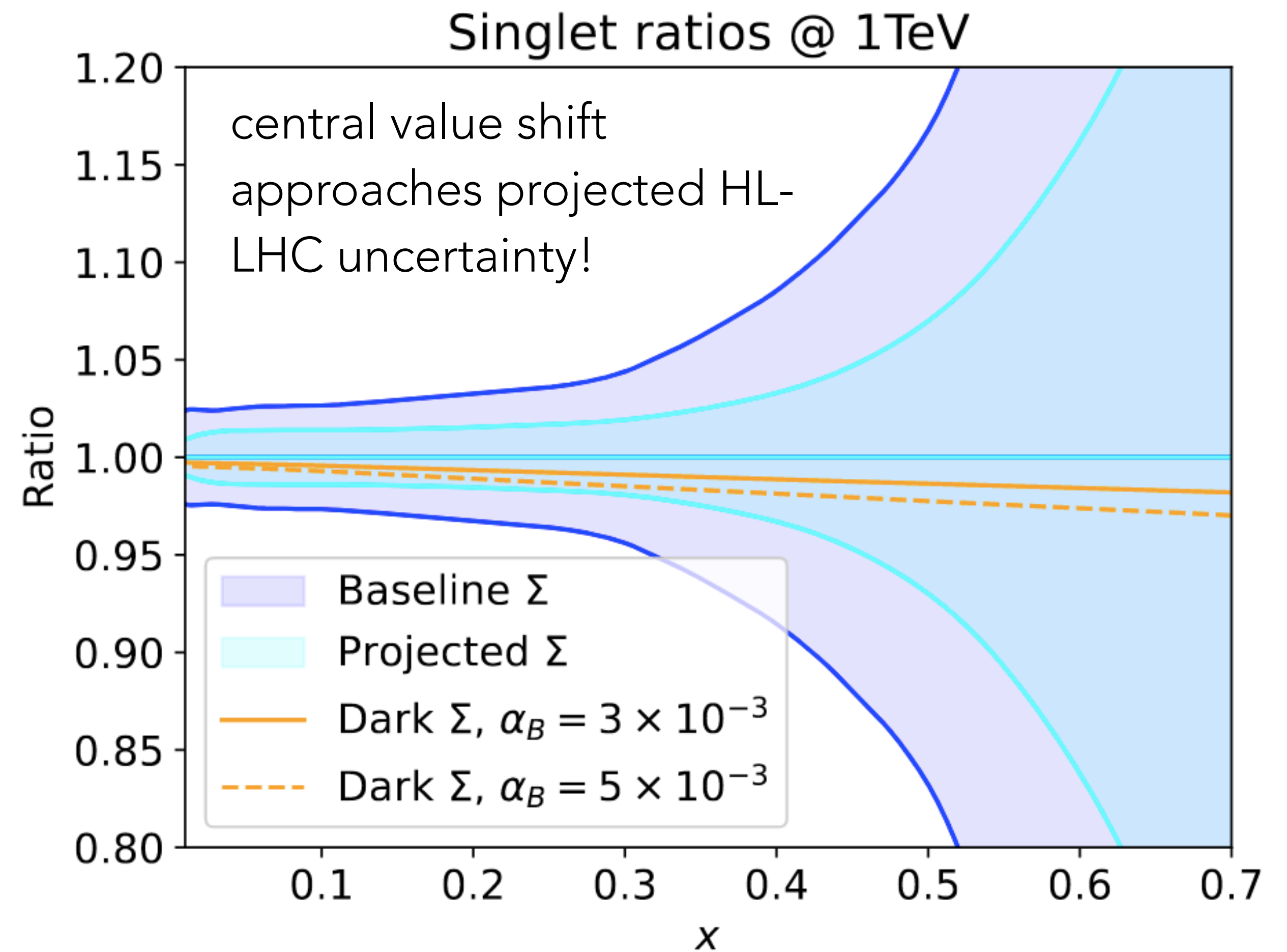
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- These contributions are well-known and already implemented in the **APFEL public evolution code**, which we modify in our work.

# Impact on PDFs and parton luminosities

- We can now study the impact of including a dark photon in DGLAP evolution on **PDFs** and **parton luminosities**, and hence on **theoretical predictions for collider processes**.

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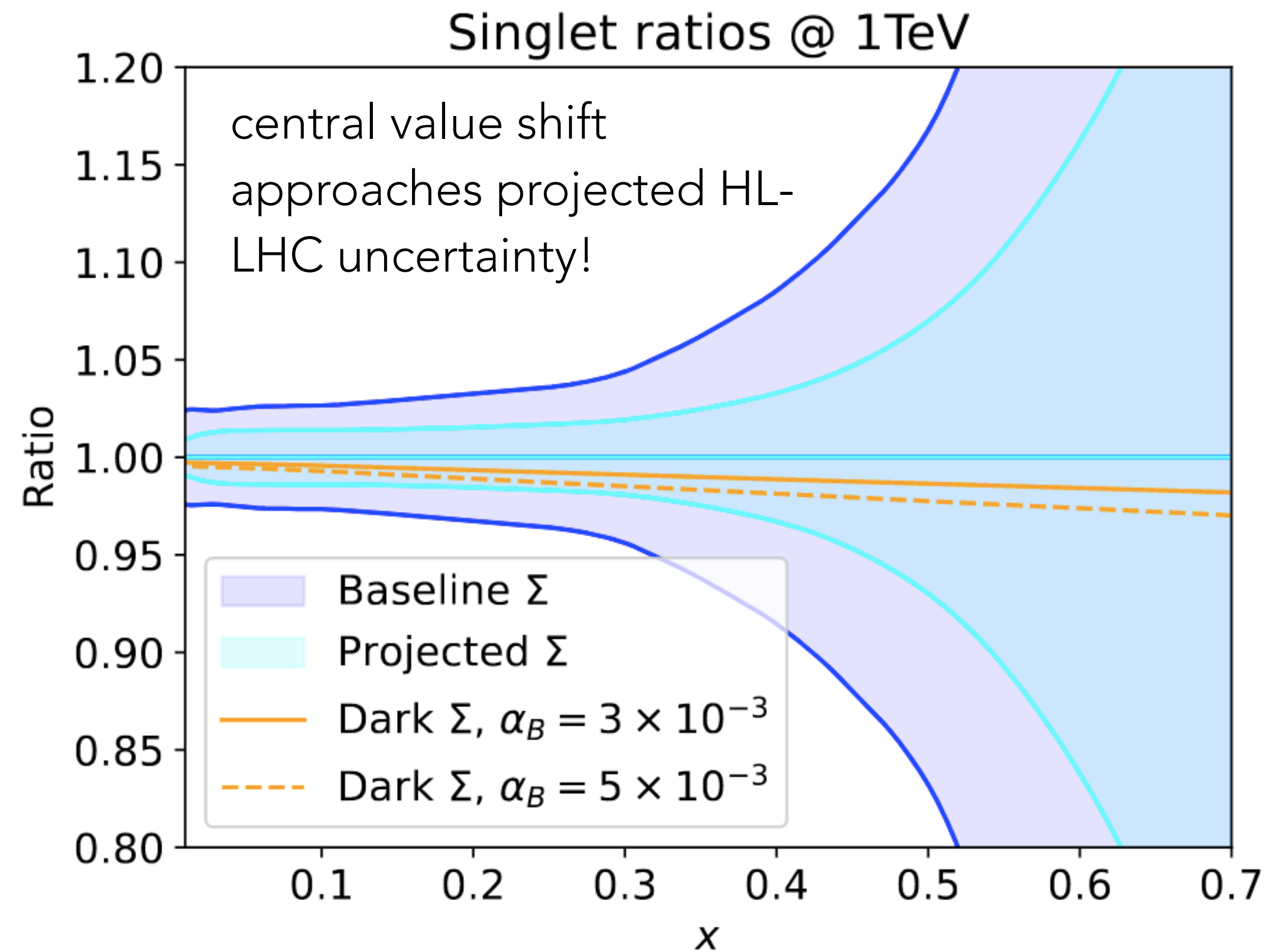
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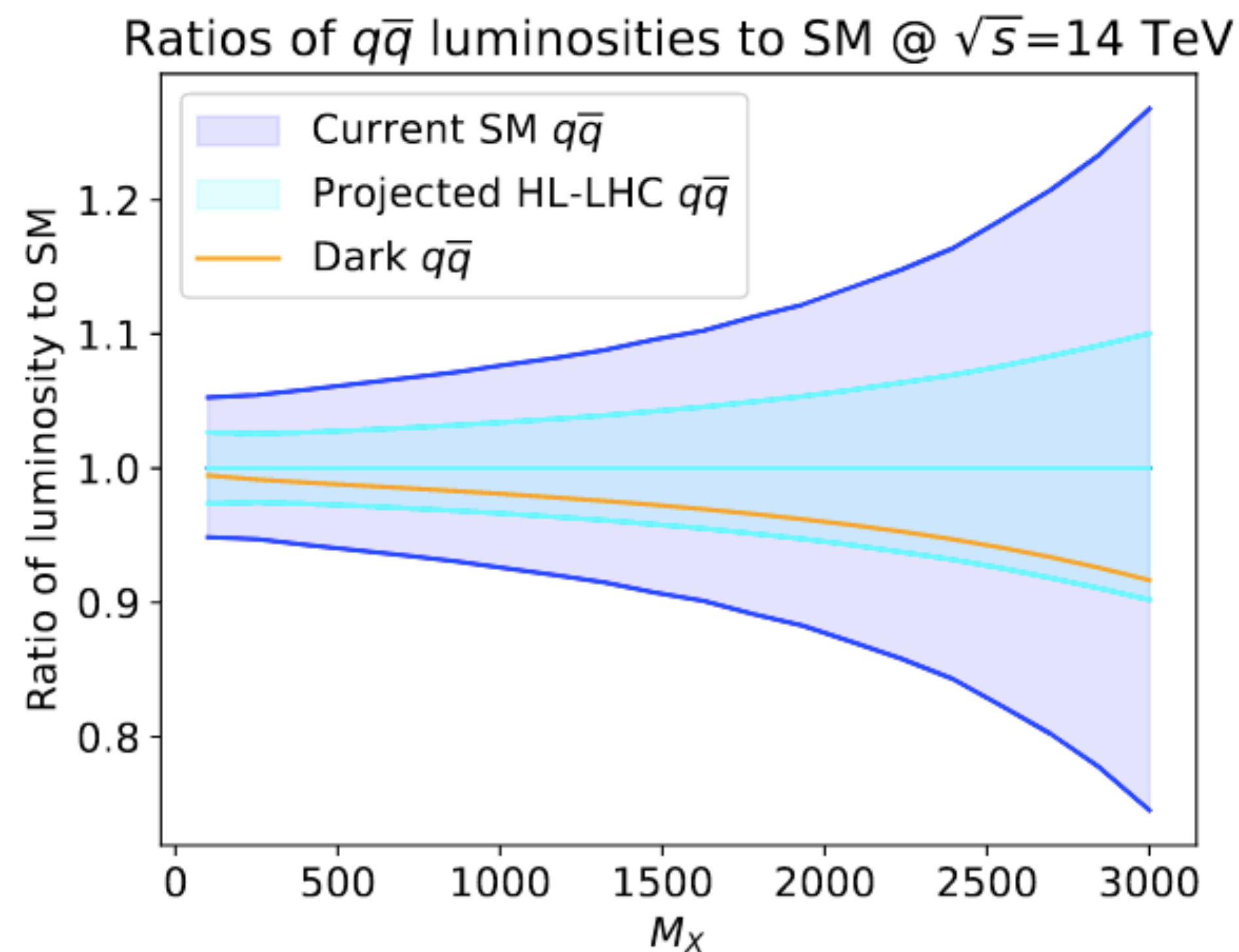
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- The region that is most modified suggests that some values of the dark mass and coupling might lead to PDF sets which **perform too poorly on Drell-Yan sets**, relative to the baseline.

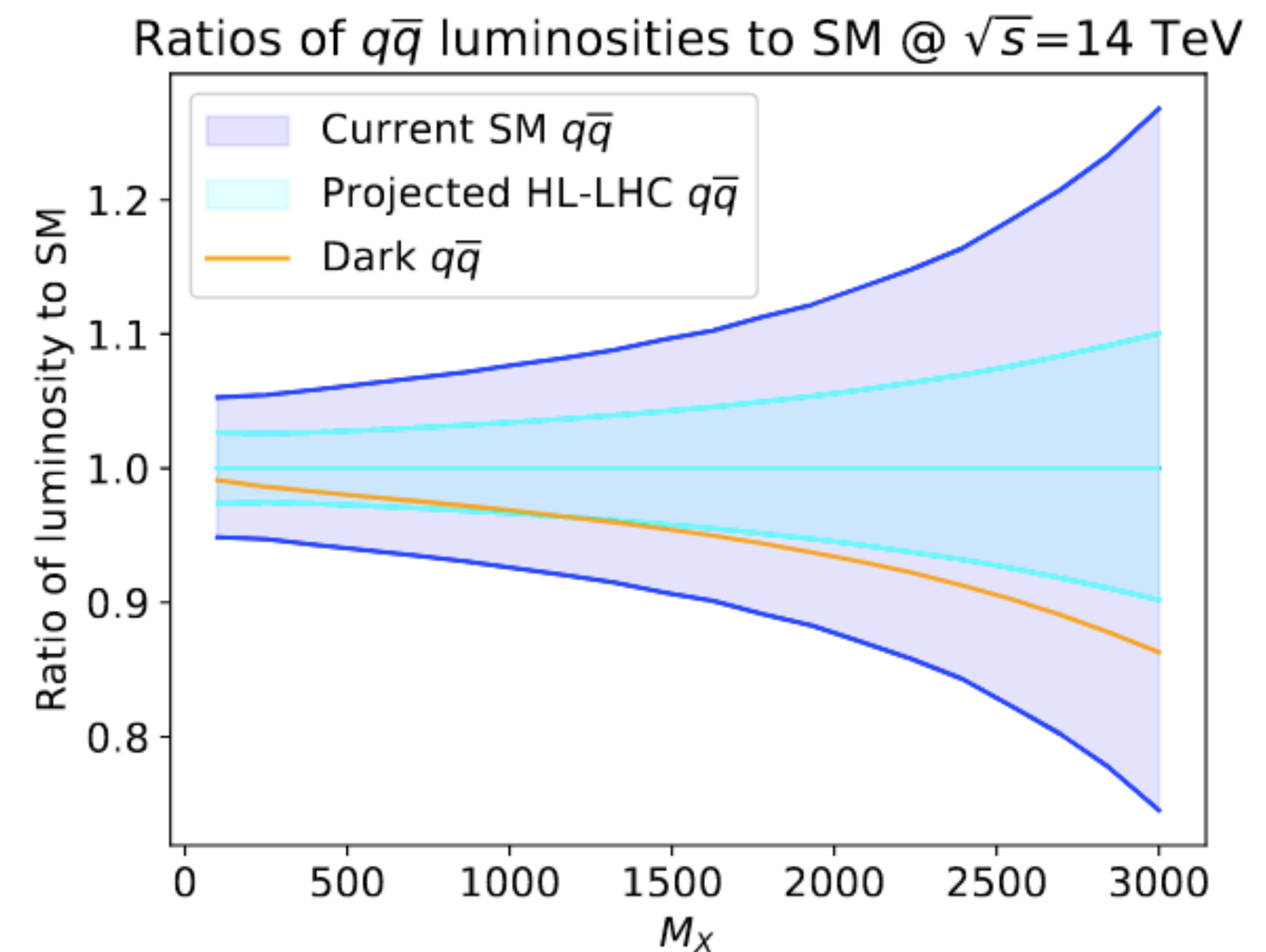


# Impact on PDFs and parton luminosities

- The most important luminosity channel for DY is  $q\bar{q}$ ; here, there is **tension with projected HL-LHC uncertainties** for some values of the mass and couplings!



(c)  $m_B = 5$  GeV,  $\alpha_B = 3 \times 10^{-3}$



(d)  $m_B = 5$  GeV,  $\alpha_B = 5 \times 10^{-3}$

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- We obtain **projected bounds** as follows:
  1. Construct a large ensemble of 'dark' PDF sets, one for each point for a grid in dark parameter space (we use 32 points, so 32 PDF sets).

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# Impact on PDFs and parton luminosities

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  3. Compare to the reference fit's  $\chi^2$ -statistic, and hence obtain projected bounds.

# Impact on PDFs and parton luminosities

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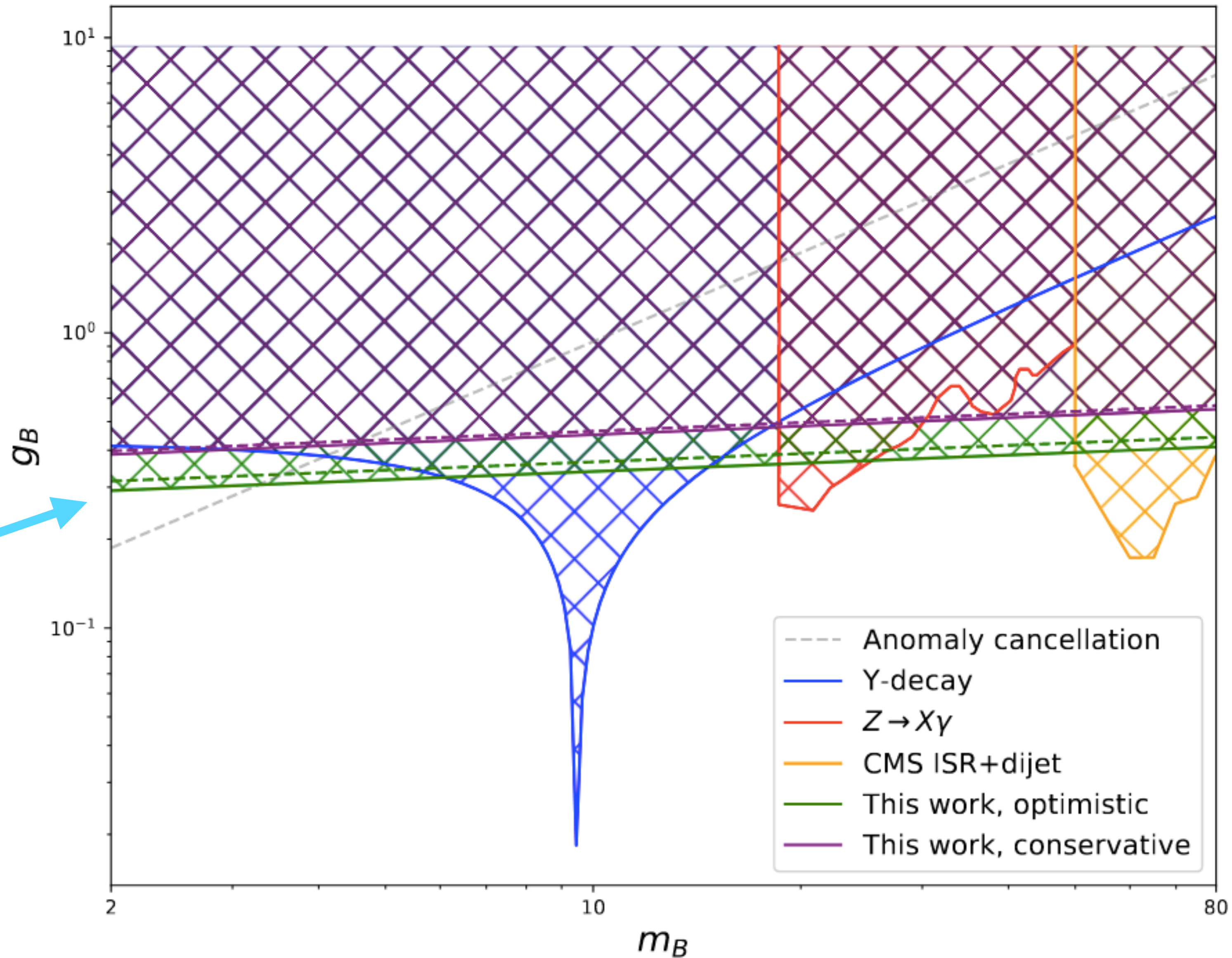
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# Comparison of (projected) bounds

**dashed lines:**  
including  
projected  
HL-LHC PDF  
uncertainty





# Conclusions

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- **Simultaneous determination of PDFs and BSM parameters**, will be **very important in future analyses** (especially as we enter Run III).
- Members of the **PBSP team** have already produced three works in the direction of simultaneous PDF-SMEFT fits: (i) a **phenomenological study** 2104.02723 showing the need for simultaneous extraction; (ii) a **methodology** (SimuNET, 2201.07240) capable of **fast simultaneous fitting**; (iii) a **comprehensive simultaneous extraction** of PDFs and SMEFT couplings from the **full LHC Run II top dataset**, 2303.06159.
- There are interesting directions outside the SMEFT, e.g. studying **light, weakly-coupled particles** inside the proton, like our **dark photon** study, 2203.12628.

**Thanks for listening!**  
**Questions?**