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## THE DARK SIDE OF THE PROTON





## TALK OUTLINE

- 1. Background: PDFs and dark matter
- 2. PDFs for colourless partons
- 3. 'Dark' PDF sets
- 4. Phenomenology of the 'dark' PDF sets

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1. BACKGROUND: PARTON

# DISTRIBUTIONS AND DARK MATTER



## HADRON STRUCTURE THROUGH PDFS

Hadrons are QCD bound states - they are strongly-coupled, non-perturbative objects.

$$\mathscr{L} = -\frac{1}{4}G^{a}_{\mu\nu}G^{a,\mu\nu} + \sum_{q} \overline{q}(i\gamma^{\mu}L)$$

- Solution: package all non-perturbative elements into unknown functions, called parton distribution functions (PDFs).



But we still want to make predictions for experiments involving hadrons!



## HADRON STRUCTURE THROUGH PDFS

- (infinitesimal) interval [x, x + dx] is given by:

 $\int g/H(x) \, dx$ parton flavour

In more detail, PDFs describe the number density of different constituents of a hadron carrying different fractions of the hadron's total momentum\*.

• The number of partons of type q inside a hadron H with momentum in the

momentum fraction



## HADRON STRUCTURE THROUGH PDFS

• Theory predictions are then obtained from the **QCD factorisation** theorems, e.g. for processes with two hadrons in the initial state:

 $\sigma_{H_1H_2}(s) = \sum_{X,q_1,q_2} \iint dx_1 dx_2 f_{q_1/H_1}(x_1) f_{q_2/H_2}(x_2) \hat{\sigma}_{q_1q_2 \to X}(sx_1x_2)$ 

## Formula valid provided we work at sufficiently high energies.

## partonic cross-section, from QCD perturbation theory



## PDF EVOLUTION

- Infrared divergences in the partonic cross-section require that we regulate and renormalise the theory, similar to the way ultraviolet divergences are handled in basic QFT.

momentum fraction

In particular, collinear infrared divergences are absorbed into the PDFs, so that they acquire a dependence on an arbitrary factorisation scale  $\mu_F$ :





## PDF EVOLUTION



Factorisation scale is usually identified with a characteristic energy scale for a process under consideration,  $\mu_F^2 = Q^2$ , so PDF evolution corresponds to increasing resolution of a hadron's structure.

Invariance of observables under changing the factorisation scale implies a Callan-Symanzik equation for the PDFs, called the DGLAP equation:

 $\mu_F^2 \frac{\partial f_{q_i/H}}{\partial \mu_F^2} = \sum_{q_j} \int_{x} \frac{dy}{y} P_{q_i q_j} \left(\frac{x}{y}\right) f_{q_j/H}(y, \mu_F^2)$ 'splitting function'



## PDF EVOLUTION

 $\mu_F^2 \frac{\partial f_{q_i/H}}{\partial \mu_F^2} = \sum_{q_j} \int_x^1 \frac{dy}{y} P_{q_i q_j} \left(\frac{x}{y}\right) f_{q_j/H}(y, \mu_F^2)$ 

- Splitting functions  $P_{q_iq_i}$  roughly correspond to the 'probability of radiating one parton flavour from another'.
- They can be computed in **perturbation theory**, in particular by looking

$$P_{ij} = \left(\frac{\alpha_S}{2\pi}\right) P_{ij}^{(1,0)} + \left(\frac{\alpha_S}{2\pi}\right)^2 P_{ij}^{(2,0)} + \left(\frac{\alpha_S}{2\pi}\right) \left(\frac{\alpha}{2\pi}\right) P_{ij}^{(1,1)} + \cdots$$

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at the most collinearly divergent part of certain partonic cross-sections.



## DETAILED EXAMPLE: PROTON PDFS

factorisation scale 2 GeV.



In the proton (naively thought of as '2 up quarks and 1 down quark') the (NNPDF 3.1) PDFs for the **up** and **down** quarks are shown below at the

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## DETAILED EXAMPLE: PROTON PDFS

Naively expect distributions to be **peaked at 1/3**, but quantum



## fluctuations produce additional virtual long-lived partons with small momentum fractions, pushing up the distributions at smaller values of x.



## DETAILED EXAMPLE: PROTON PDFS

- the momentum carried by the proton.
- colourless particles, e.g. the photon.

Quantum fluctuations don't just push up the distributions of the valence quarks u and d; they also result in non-zero PDFs for other flavours too.

In particular, we also obtain gluon PDFs which account for almost a half of

Similarly, we have PDFs for other coloured particles (strange, etc.), but also



## Is there enough space inside the proton for new, hypothetical particles (e.g. dark matter)?

## KEY QUESTION:



## NEW CONSTITUENTS OF THE PROTON?

- The idea is not too far-fetched!
- alter proton structure.
- continue to reduce in the near future, could we do the same for a colourless particle too?
- E.g. a dark matter candidate: neutral and colourless.

 The inclusion of new coloured particles, e.g. gluinos, has already been studied by Berger et al. in 0406143 (from 2005) and 1010.4315 (from 2010). Strong constraints can be derived assuming that new coloured particles

Idea: now PDFs are known very precisely, and their uncertainties will



## DARK MATTER IN THE PROTON

- leptons.
- augments the SM Lagrangian by an **effective** interaction term:

• The best chance we have to see a significant change in proton structure is to choose a dark matter candidate coupling primarily to quarks instead of

We choose to introduce a leptophobic dark photon B, which simply

 $\mathscr{L}_{\text{int}} = \frac{1}{3} g_B \overline{q} \gamma^\mu B_\mu q$ 



## DARK MATTER IN THE PROTON



- agnostic about any specific UV-completion.
- requirement of certain anomaly-cancelling fermions.

 $\mathscr{L}_{\text{int}} = \frac{1}{3} g_B \overline{q} \gamma^\mu B_\mu q$ 

• As long as we treat this as an **effective theory**, valid up to the **mass of the Z-boson** where **kinetic mixing** effects become important, we can **remain** 

In particular, we don't commit to any model-dependent features, e.g. the



## DARK MATTER IN THE PROTON



We hence focus on the region  $m_R \in [2,80]$  GeV.

## (MORE SPECIFIC) KEY QUESTION:

Is there enough space inside the proton for an additional leptophobic 'dark' photon, described by the model above, with mass  $m_B \in [2,80]$  GeV?



2. PDFS FOR COLOURLESS PARTONS



## COLOURLESS PARTONS

- subtle because the dark photon is colourless.
- In particular, PDFs for colourless partons are very small compared to coloured flavours, so they can be **challenging to determine**.
- treated historically.

How can we include a new dark photon PDF? In general, this is more

• To introduce the main ideas, let's see how the (SM) photon PDF has been



- organised chronologically:
  - motivated model, as in MRST 0411040 (from 2004).
  - MRST assume a photon PDF at some **initial scale**  $Q_0^2$  of the form:

 $\gamma(x, Q_0^2) = \frac{\alpha}{2} \sum e_q^2$ Q

• There are three main routes one can take in introducing a photon PDF,

1. Avoid determination altogether. Instead, use a phenomenologically-

$$2\log\left(\frac{Q_0^2}{m_q^2}\right)P_{\gamma q}\otimes q(Q_0^2)$$





- Essentially, this is a leading-order solution to the DGLAP equations assuming the quarks PDFs are 'frozen' beneath the initial scale  $Q_0^2$ .
- by quark splitting at this scale.

Physically we imagine that photons in the proton are generated only



Choosing this functional form for the photon PDF at the initial scale, we then evolve using the **QED-modified DGLAP equations:** 



$$\frac{dy}{y} P_{q_i q_j} \left(\frac{x}{y}\right) f_{q_j}(y, Q^2)$$

extra splitting functions

$$\frac{(1-x)^2}{x}$$

$$P_{\gamma\gamma}(x) = -\frac{4}{3}\delta(1-x)$$



- The quark and gluon PDFs are now modified relative to the original reference set, because of the inclusion of the photon PDF in the PDF evolution (the gluon effect is second-order, though).
- This modifies predictions for observables, allowing us to assess the impact of including a photon PDF in the proton structure, versus ignoring its contribution.
- Same idea holds completely analogously for a dark photon PDF.



PDFs from MRST 0411040



- second chronologically is:
  - partonic cross-section in the factorisation formula.
  - to many observables.

However, **improved methods** do exist for photon PDF determination. The

2. Fitting the photon PDF to data. Instead of just modifying PDF evolution by including extra splitting functions and an extra PDF, we also modify the

This allows us to **fit the photon PDF** like any other flavour. But this is much more labour-intensive: need to compute photon contributions



- This method was adopted by members of the NNPDF collaboration in 1308.0598.
- **Deep-inelastic scattering** data, along with W/Z production data from the LHC, was used to provide the first **fitted** photon PDF, including uncertainties.
- The photon PDF uncertainties were initially relatively large.





- reducing PDF uncertainty on the photon distributions.
  - introduced by Manohar et al. in 1607.04266.
  - PDF at **all scales**.

• The final approach is the most surprising! It played an essential role in

3. Amazingly, the photon PDF can be described **perturbatively** in terms of DIS structure functions; this is the cutting-edge LUXQED method. It was

The 'bare bones' description is: the photon can be treated either as a mediator of DIS or as a constituent of the proton; the requirement that both approaches agree gives an **analytic formula** for the photon



$$\gamma(x,\mu^2) = \frac{1}{2\pi\alpha(\mu^2)} \int_{x}^{1} \frac{dz}{z} \int_{x^2m_P^2/(1-z)}^{\mu^2/(1-z)} \frac{dQ^2}{Q^2} \alpha^2(Q^2) \left[ \frac{1}{2\pi\alpha(\mu^2)} \int_{x}^{1} \frac{dz}{z} \int_{x^2m_P^2/(1-z)}^{\mu^2/(1-z)} \frac{dQ^2}{Q^2} \alpha^2(Q^2) \right]$$

- The formula is **perturbative**, and can be improved **order by order in** QED.
- Since structure functions are (essentially) observable, can just do integration to get the photon PDF!

 $Q^{2}\left[\left(zP_{\gamma q}(z)+\frac{2x^{2}m_{P}^{2}}{Q^{2}}\right)F_{2}^{\gamma}\left(\frac{x}{z},Q^{2}\right)\right]-z^{2}F_{L}^{\gamma}\left(\frac{x}{z},Q^{2}\right)\right]$ structure function  $-\alpha^{2}(\mu^{2})z^{2}F_{2}^{\gamma}\left(\frac{x}{z},Q^{2}\right)$ 

## for photon-induced DIS



- The method was eventually included in the **NNPDF framework**, in 1712.07053, allowing for the production of the precise NNPDF3.1 LUXQED set.
- Not only were uncertainties drastically reduced compared to the previous NNPDF determinations, but additionally the central value shifted by up to 40% in regions with less data in the former fit!



Photon PDF from 1712.07053

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3.'DARK' PDF SETS



## DARK PDF SETS

- three approaches outlined above:
  - DGLAP and see how other PDFs change. Possible!
  - -

In order to include a dark photon then, we can try to follow one of the

- Method 1: Compute dark photon splitting functions, and use an ansatz for the dark photon PDF at the initial scale. Evolve using modified

Method 2: Fit to data. Not possible without new, very labour-intensive technology (would need to generalise the fast-convolution grids -APPLgrids - produced by MadGraph5 to include dark photons).



## DARK PDF SETS

- (and an analytic formula can be derived), but there are some technical subtleties. In particular:
  - machinery.
  - PDFs in Manohar et al., 1803.06347.

- Method 3: Use the LUXQED method for the dark photon PDF. This is possible

\* We would need to split the experimental structure functions into 'photon' induced' and 'dark-photon induced', which would involve some novel fitting

\* More concerning: interference between photon-mediated and dark-photon mediated DIS implies the need to introduce an additional **photon-dark** photon interference PDF. This is described in an analysis of Z-boson



## DARK PDF SETS

- In short: Method 1 is only viable option for a first study. The steps are:
  - 1. Compute the dark photon splitting functions, and add them to the DGLAP evolution.
  - 2. Starting from an appropriate initial-scale ansatz, and a reference PDF set, evolve using the modified DGLAP equations.
  - 3. Compare resulting PDF set predictions with SM predictions to see impact of inclusion of a dark photon.



## DARK SPLITTING FUNCTIONS

The first step is **straightforward**: the splitting function calculation is



Splitting occurs in four channels, giving four splitting functions:

$$P_{qq}(x) = \frac{1+x^2}{9(1-x)_+} + \frac{1}{6}\delta(1-x)$$

$$P_{qB}(x) = \frac{x^2 + (1-x)^2}{9}$$

## completely analogous to that of the **photon** splitting function calculation.

$$P_{BB}(x) = -\frac{2}{27}\delta(1-x)$$

$$P_{Bq}(x) = \frac{1}{9}\left(\frac{1+(1-x)^2}{x}\right)$$

$$\frac{1}{34}\left(\frac{1+(1-x)^2}{x}\right)$$



## DARK SPLITTING FUNCTIONS

- All four splitting functions are multiplied by  $\alpha_B = g_B^2/4\pi$  in the DGLAP literature for this model), we see that we must also include:
  - NNLO QCD effects,  $\alpha_s^3 \sim 0.001$

  - QED-QCD mixing,  $\alpha \alpha_{s} \sim 0.001$
- These contributions are well-known and already implemented in the **APFEL public evolution code**, which we modify in our work.

equations. Assuming a dark coupling of order  $\alpha_{R} \sim 0.001$  (reasonable in the

LO QED effects,  $\alpha \sim 0.01$  (this implies that we must use a photon PDF)



## DARK SPLITTING FUNCTIONS

Overall, the DGLAP equations are modified to: 

$$\mu^2 \frac{\partial g}{\partial \mu^2} = \sum_{j=1}^{n_f} P_{gq_j} \otimes q_j + \sum_{j=1}^{n_f} P_{gq_j}$$
$$\mu^2 \frac{\partial \gamma}{\partial \mu^2} = \sum_{j=1}^{n_f} P_{\gamma q_j} \otimes q_j + \sum_{j=1}^{n_f} P_{\gamma q_j}$$
$$\mu^2 \frac{\partial q_i}{\partial \mu^2} = \sum_{j=1}^{n_f} P_{q_i q_j} \otimes q_j + \sum_{j=1}^{n_f} P_{q_j}$$
$$\mu^2 \frac{\partial B}{\partial \mu^2} = \sum_{j=1}^{n_f} P_{Bq_j} \otimes q_j + \sum_{j=1}^{n_f} P_{p_j}$$

 $_{Q\bar{q}_{j}}\otimes \bar{q}_{j}+P_{gg}\otimes g+P_{g\gamma}\otimes \gamma$ 

 $_{\gamma \bar{q}_{j}} \otimes \bar{q}_{j} + P_{\gamma g} \otimes g + P_{\gamma \gamma} \otimes \gamma$ 

 $P_{q_i\bar{q}_j}\otimes \bar{q}_j + P_{q_ig}\otimes g + P_{q_i\gamma}\otimes \gamma + P_{q_iB}\otimes B$ 

 $P_{B\bar{q}_j}\otimes \bar{q}_j + P_{BB}\otimes B,$ 



## INITIAL DARK PDFS

- Still need to specify initial conditions to solve these equations.
- use a quark-splitting ansatz like the photon one we saw earlier).
- In particular, we **freeze** the dark photon PDF to **zero** throughout the evolution from 1.65 to 2 GeV, then 'turn on' its inclusion above this scale.

Modern PDF fits use the standard initial scale  $Q_0^2 = 1.65$  GeV. Since we assume  $m_R \ge 2$  GeV, for the purposes of initial conditions we should treat the dark photon in the same way as heavy quarks (otherwise, we could



## INITIAL DARK PDFS

- of some fixed **reference set** which we will compare against.
- the updated NNPDF4.0 LUXQED set.

## • For the other PDFs, we choose to set their initial values to the initial values

We choose to take the NNPDF3.1 NNLO LUXQED set, which is the stateof-the-art set including a photon. It will be replaced in the near future by



set made with  $\alpha_R = 3 \times 10^{-3}$ ,  $m_R = 50$  GeV in the next few slides.



as the photon, but has smaller abundance.

## With everything specified, we can see an example! We look at a 'dark' PDF

## In the 'dark' set, the dark photon PDF takes the same functional form



defined to be:

 $\langle x \rangle_q(Q) =$ 

Tabulating momentum fractions at 1 TeV, we have:

$$\langle x \rangle_f (Q = 1 \text{ TeV})$$
  
Baseline  
Dark set

## Quantitavely, we can look at the **momentum** carried by each flavour in the 'dark' proton. The momentum fraction carried by flavour q at scale $Q^2$ is

$$\int_{0}^{1} dx \ x f_q(x, Q^2) \, .$$

$f = \Sigma$	$f=\gamma$	f = B
48.36%	0.5279%	0%
48.12%	0.5275%	0.1357%



- We can also assess the impact of the inclusion of a dark photon on the other flavour's evolution. E.g. for the **singlet PDF** (the sum of all quark flavours' PDFs), we have the comparison on the right.
- Light blue bands correspond to projected PDF uncertainty at the **HL-LHC** (see 1810.03639.)



- Significant modification in this region is phenomenologically interesting because it's mainly constrained by **Drell-Yan data** in PDF fits.
- Some values of the dark mass and coupling might lead to PDF sets which **perform too** poorly on Drell-Yan sets, relative to the baseline.



• Similar behaviour is seen in the  $u_V$  valence distribution, the difference between the up and anti-up PDFs.





4. PHENOMENOLOGY OF THE 'DARK' PDF SETS



- sufficiently low mass) can distort other PDF flavours considerably. In particular, we expect to be able to obtain constraints from Drell-Yan data.
- In hadron-hadron collisions like DY, PDFs contribute through parton luminosities, which are double-differential quantities defined by:

$$\frac{d\mathscr{L}_{ij}}{dyd\tau} = f_i(x_1, Q^2) f_j(x_2, Q^2),$$
  
invariant mass of find

We have seen that including dark photons of sufficiently high coupling (or

 $x_{1,2} = \sqrt{\tau} \exp(\pm y), \quad \tau = m_X^2/s$ partonic centre of mass nal state energy



• To assess the impact of including a dark photon on dark luminosities, we look at integrated singlevariable versions of the parton luminosities instead:

$$\Phi_{ij}(M_X^2) = \frac{1}{s} \int_{M_X^2/s}^{1} \frac{dx}{x} f_i(x, M_X^2) f_j\left(\frac{M_X^2}{xs}, M_X^2\right)$$

Right, we show the luminosities for  $\alpha_{R} = 3 \times 10^{-3}, m_{R} = 50$  GeV.



- The *BB* luminosity is very small relative to the  $q\bar{q}$  channel, since it is suppressed by two powers of the dark coupling.
- On the other hand, the Bq channel becomes more important than the  $\gamma\gamma$  luminosity, suggesting that the dark photon starts to have an impact on some phenomenology at this mass and coupling.

![](_page_46_Figure_4.jpeg)

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![](_page_46_Picture_6.jpeg)

reference set luminosities, we get the following:

![](_page_47_Figure_2.jpeg)

(a)  $m_B = 50 \text{ GeV}, \alpha_B = 3 \times 10^{-3}$ 

• The relevant channel in the case of DY is the  $q\bar{q}$  luminosity. Comparing the 'dark' luminosities for different values of the coupling and mass to the

![](_page_47_Figure_6.jpeg)

![](_page_47_Picture_7.jpeg)

![](_page_48_Figure_1.jpeg)

Indications of incompatibility at the level of projected HL-LHC uncertainties!

![](_page_48_Figure_4.jpeg)

![](_page_48_Picture_7.jpeg)

- We obtain **projected bounds** as follows:
  - in dark parameter space (we use 32 points, so 32 PDF sets).
  - compute the  $\chi^2$ -statistic.
  - bounds.

Results we have seen so far suggest that we can definitely hope to constrain the dark photon's mass and coupling using DY data, provided we work with HL-LHC projections and assume that PDF uncertainties will shrink as predicted.

1. Construct a large ensemble of 'dark' PDF sets, one for each point for a grid

2. Construct predictions for a specific DY observable for each PDF set and

3. Compare to the reference fit's  $\chi^2$ -statistic, and hence obtain projected

![](_page_49_Picture_12.jpeg)

- projected data we use is a small modification of that produced by Maeve and Wilson coefficients, 2104.02723.
- - with five-fold reduction in systematics.
  - available), with two-fold reduction in systematics.

• The specific HL-LHC observable we choose to use is neutral current Drell-Yan at a centre-of-mass-energy  $\sqrt{s} = 14$  TeV, in 12 bins of lepton invariant pair-mass. The Madigan for the PBSP group's study of the simultaneous determination of PDFs

• Two sets of projected data are used, corresponding to the following two scenarios:

Optimistic: Total integrated luminosity 6  $ab^{-1}$  (both CMS and ATLAS available),

Conservative: Total integrated luminosity 3  $ab^{-1}$  (only CMS or ATLAS is

![](_page_50_Picture_10.jpeg)

 Right: a comparison of the projected data (shown in grey) with the SM baseline (NNPDF3.1 LUXQED) and two 'dark' PDF sets used in the grid scan.

			٦
da/dm <sub>iī</sub>	10 <sup>-4</sup>		
	10 <sup>-5</sup>		
	10 <sup>-6</sup>		
	10 <sup>-7</sup>	-	
	10 <sup>-8</sup>		

![](_page_51_Figure_3.jpeg)

- *Right top:* The previous plot as a ratio to the central data values. Dark grey is 'optimistic', light is 'conservative'.
- Right bottom: The previous plot, as a ratio to central theory, with (projected) PDF uncertainties displayed.

![](_page_52_Figure_3.jpeg)

![](_page_52_Picture_5.jpeg)

## dashed lines: including PDF uncertainty

![](_page_53_Figure_2.jpeg)

 $m_B$ 

![](_page_53_Picture_4.jpeg)

- Dashed: From 1404.3947. UV-completing our theory requires the introduction of anomaly-cancelling fermions, which acquire masses from  $U(1)_B$ -breaking, mediated by some Higgs-like scalar.
- The resulting Yukawa Higgs-fermion coupling then looks like  $\lambda \sim m_F / v_B$ , whilst our coupling looks like  $g_B \sim m_B / v_B$ . So:  $g_B \sim \lambda m_B / m_F$ .
- Assuming perturbativity,  $\lambda \leq 4\pi$ , and  $m_F = 90$  GeV gives the bound.

![](_page_54_Figure_4.jpeg)

- All remaining constraints are experimental.
- Blue: From 9411256, 9809522 and ARGUS 1986. Bound from upsilondecays, which are enhanced by the presence of a dark photon.
- Red: From 1705.06726 and the 1996 LEP study of  $Z \rightarrow H\gamma$ ,  $H \rightarrow$  hadrons. Bound from  $Z \rightarrow B\gamma$  decays (called X there), and subsequent SM decay of B.

![](_page_55_Figure_4.jpeg)

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![](_page_55_Picture_6.jpeg)

- Yellow: From CMS studies 1905.10331 and 1909.04114. Bounds from
   resonances decaying into qq pairs dark photon signal would enhance
   dijet invariant mass spectrum.
- Purple and green: This work.

![](_page_56_Figure_3.jpeg)

![](_page_57_Figure_1.jpeg)

 $m_B$ 

![](_page_57_Picture_3.jpeg)

CONCLUSIONS

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![](_page_58_Picture_2.jpeg)

## CONCLUSIONS

- the near future of the LHC.
- energy, experimental probes and theoretical bounds from assumptions on the UV-completion.

**New BSM particles** can be included in DGLAP evolution by computing their **splitting functions**; this distorts the DGLAP evolution of **SM PDFs**.

Even for colourless BSM particles, which have very small abundance in the proton, inclusion in proton structure will significantly affect predictions in

Projected sensitivity of this method is competitive with current, lower-

![](_page_59_Picture_8.jpeg)