Hide and Seek: Can PDFs fit away New Physics signals?



James Moore, University of Cambridge

For PDF4LHC 2023, CERN, based on 2307.10370 (by the PBSP team + Michelangelo Mangano)



PBSP: Physics Beyond the Standard Proton

- The PBSP group is based at the University of Cambridge, and is headed by Maria Ubiali; the project is ERC-funded.
- The aim is to investigate interplay between BSM physics and proton structure - the subject of the rest of this talk!
- The team members are:
 - Postdocs: Zahari Kassabov (former), Maeve Madigan, Luca Mantani, **James Moore**
 - PhD students: Mark Costantini, Shayan Iranipour (former), Elie Hammou, Manuel Morales, Cameron Voisey (former)





Established by the European Commission



Imagine Nature is described by SM + some New Physics





Imagine Nature is described by SM + some New Physics

Collider data is then drawn from a distribution centred on the SM + New Physics







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...but imagine a PDF fitting collaboration assumes the **SM** during a PDF fit to the collider data







'Reality'

Predictions are formed from **TRUE** PDFs, and ullet**TRUE** New Physics parameters:

$$\sigma = \hat{\sigma}_{SM+NP} \otimes f_{true}$$



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Result of fit

Predictions are formed from **CONTAMINATED** \bullet PDFs, and **NO** New Physics parameters:

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Predictions are formed from **TRUE** PDFs, and **TRUE** New Physics parameters:

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Key idea: If the fit quality is good, these are approximately equal for the fit dataset, and the PDFs have 'fitted away' the New Physics.



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Predictions are formed from **CONTAMINATED** \bullet PDFs, and **NO** New Physics parameters:

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Key questions for the talk...

1. Does there exist a New Physics model which can be 'absorbed' by the PDFs in this way? (Spoiler alert: yes!)

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- 1. (Spoiler alert: yes!)
- effects of using the PDF on out-of-fit isn't really there? (Spoiler alert: yes!)

Does there exist a New Physics model which can be 'absorbed' by the PDFs in this way?

2. Given a 'contaminated' PDF fit, what are the datasets? Could we see New Physics that

1. - Contaminated fits for a W' model

 Let's suppose that the true theory -boson:

$$\mathcal{L}_{\rm UV}^{W'} = \mathcal{L}_{\rm SM} - \frac{1}{4} W'^{a}_{\ \mu\nu} W'^{a,\mu\nu} + \frac{1}{2} M^{2}_{W'} W'^{a}_{\ \mu} W'^{a,\mu} - g_{W'} W'^{a,\mu} \sum_{f_L} \bar{f}_L T^a \gamma^{\mu} f_L - g_{W'} (W'^{a,\mu} \varphi^{\dagger} T^a i D_{\mu} \varphi + \text{h.c.})$$

- Let's suppose that the true theory of Nature is the SM plus some new W^\prime

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Physics' can be characterised entirely by a **single parameter**:

• Let's suppose that the **true theory of Nature** is the SM plus some new W'

• For large W'masses, an EFT approach is valid, and the 'strength of New

$$\sqrt{2}g_{W'}^2$$

 $8G_F M_{W'}^2$

VV

a PDF fit.

• The existence of the W'-boson induces four-fermion interactions which affect both deep-inelastic scattering and Drell-Yan observables entering

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 - CMS DY high-
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 - Total DY (H
- shown above.

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M-only)	260
$-mass \ 13 \ TeV$	43
$-mass 8 { m TeV}$	41
$-mass 7 { m TeV}$	117
gh-mass 8 ~TeV	46
gh-mass 7 ~TeV	13
	ⁿ dat

There are five high-mass DY sets that can be included in PDF global fits,

... and we additionally use four projected HL-LHC high-mass Drell-Yan datasets, generated as in 1810.03639, which are also affected.

HL-LHC HM DY 14 TeV - neutral current - electron channel HL-LHC HM DY 14 TeV - neutral current - muon channel HL-LHC HM DY 14 TeV - charged current - electron channel HL-LHC HM DY 14 TeV - charged current - muon channel

Total HL-LHC: 56 points

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Right: the kinematic coverage of our fit, with the **New-Physics** 'contaminated' points shown with bold outline.



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Mmm, this contamination is just right!

$\hat{W} = 0.00015$

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Fit quality

consistent or not with the bulk of datasets included. In the NNPDF4.0 flagged according to the selection criterion:

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global dataset, and included/excluded on that premise.

• All PDF fitting collaborations must decide a criterion to decide whether a dataset is methodology, a fit is considered 'good' provided that none of the datasets are

• If datasets are flagged, the weighted fit method is applied, and depending on its success, the flagged datasets are either judged consistent/inconsistent with the





 $n_{\sigma} = 2$, the critical rejection value for NNPDF

4.94

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• Left: Values of n_{σ} for datasets from the three fits (plus a **baseline fit**, performed using fake data generated with $\hat{W} = 0$).





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- Left: Values of n_{σ} for datasets from the three fits (plus a **baseline fit**, performed using fake data generated with $\hat{W} = 0$).
- As promised, fit quality **doesn't show** anything unusual for $\hat{W} = 0.00003$ and $\hat{W} = 0.00008$.
- For relatively 'strong' New Physics though, we start to get **flagged sets** amongst the contaminated HL-LHC CC datasets, and amongst lowenergy SM-like fixed target DY datasets, indicating a tension.



Why the tension? - Look at the PDFs!

luminosity in the case of charged current DY.

• The predictions for the high mass DY datasets that are 'contaminated' by New Physics come from the qq PDF luminosity in the case of neutral current DY and from the qq PDF



Why the tension? - Look at the PDFs!

- luminosity in the case of charged current DY.
- **both luminosities** at **smaller invariant masses**:



• The predictions for the high mass DY datasets that are 'contaminated' by New Physics

come from the $q\bar{q}$ PDF luminosity in the case of neutral current DY and from the qq PDF

• As the interaction strength of the New Physics increases, a larger shift is required in




Why the tension? - Look at the PDFs!



• In the $\hat{W} = 0.00003$ and $\hat{W} = 0.00008$ scenarios, the large-x regions of the anti-quark New Physics.

PDFs (which contribute to the large invariant mass regions where the shift is required) are otherwise unconstrained in the PDF fit; hence, they can move to accommodate the

Why the tension? - Look at the PDFs!



• In the $\hat{W} = 0.00015$ scenario however, the luminosity shift is required at a sufficiently to constrain the corresponding region of x-space that the anti-quark PDFs had quark PDFs, e.g. from the EIC or proposed Forward Physics Facility at CERN.

low invariant mass such that other datasets (notably low-energy fixed target DY) begin

previously exploited. This points to the need for better knowledge of the large-x anti-

2. - Consequences of using a contaminated fit

Predictions for SM-like out-of-sample sets

• So far, we have concentrated on whether **New Physics** can **pass** sufficiently low interaction strength by exploiting a lack of constraints on the large-x anti-quark PDFs.

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Predictions for SM-like out-of-sample sets

• So far, we have concentrated on whether **New Physics** can **pass undetected** through a PDF fit - in our W'-model, this is possible for a sufficiently low interaction strength by exploiting a lack of constraints on the large-*x* anti-quark PDFs.

• Next natural question: Is there a value of \hat{W} for which the PDFs **absorb** the New Physics, but give wrong conclusions when applied to out-offit datasets? As promised earlier, yes.

• Consider W^+W^- production, an observable not usually included in PDF fits. This observable is **unaffected** by New Physics in our W'-model, therefore if we generate fake data, it will be SM-like.

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- Generating a fake HL-LHC W⁺W⁻ dataset, shown right in blue, we compare with predictions obtained from the 'contaminated' PDFs.
- For $\hat{W} = 0.00003$, predictions are consistent, but for $\hat{W} = 0.00008$ a deviation of 3σ is observed (shown in red)!



To the naïve BSM practitioner, who simply uses PDFs as given to them by the fitting collaborations, this looks like New Physics!



3. - Disentangling PDFs and New Physics

Physics effects, which can lead to erroneous discoveries of New Physics.

Key question for last part of talk:

Can we do anything about this?



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- **Possible strategies for disentanglement:**
 - 1. large-*x* anti-quarks.



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If you can think of other strategies, let us know!



quark PDFs whose freedom was exploited to absorb the New Physics earlier.



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• Future precision data from LHCb might be expected to **better constrain** the **large-***x* **anti-**

In particular, measurement of **on-shell forward** W and Z production at the HL-LHC

• We generate **fake data** for these observables, as they would be measured by LHCb, and check the quality of predictions from the $\hat{W} = 0.00008$ PDFs, hoping they will perform

• We see that the agreement is **excellent**.



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the forward region probed by LHCb

• Why? In the **forward region** probed by LHCb, one parton has **very large** x, but the other has very small x. Since valence quarks at large-x are much more abundant, in the vast majority of collisions we end up probing the large-x quarks instead of the large-x anti-quarks.





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ulletconstraints.

the forward region probed by LHCb

Other observables might be useful from LHCb though - we have yet to explore the forward/ backward asymmetry and differential angular distributions, which may provide useful





study.

Including new low-energy data will hopefully protect the PDF fit from contamination. However, even if the PDF is contaminated, BSM practitioners can still make reliable conclusions about New Physics by limiting the PDF dependence of the observables they



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• Suppose that instead of studying W^+W^- earlier and **erroneously** discovering New Physics there, a BSM practitioner studies the ratio $W^+W^-/(NC DY)$ to **neutral-current DY**.

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conclusions about New Physics by limiting the PDF dependence of the observables they study.

- Suppose that instead of studying W^+W^- earlier and **erroneously** discovering New Physics there, a BSM practitioner studies the ratio $W^+W^-/(NC DY)$ to **neutral-current DY**.
- Here, the PDF dependence mostly cancels in the ratio, keeping us safe from contamination effects.

Including new low-energy data will hopefully protect the PDF fit from contamination. However, even if the PDF is contaminated, BSM practitioners can still make reliable



• Indeed, we see that studying this ratio, the BSM practitioner would **correctly** conclude New Physics in **either** W^+W^- or NC DY in this case (or both).



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If the **observables** are studied ulletindependently, they would wrongly conclude New Physics in W^+W^- as we saw above.



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Conclusions

Conclusions

PDFs.

Physics.

against contamination from New Physics.

avoid wrong conclusions about New Physics.

There exist New Physics scenarios which can be 'fitted away' into the

• If these PDFs are used for BSM searches, we might erroneously see New

PDF fits should aim to include more low-energy SM-like data to guard

• BSM practitioners should aim to study **PDF-independent observables** to

Future work (advertisements)



case).

 The best-case scenario for BSM studies would be to simultaneously extract PDFs and BSM parameters. This has previously been studied in 2303.06159, for example. The **PBSP group** will shortly release a **public** code which allows BSM practitioners to do this for linear BSM models:

SIMUnet

• This public code will **also** support the reproduction of the results of this talk, and allow for users to assess the possibility of PDF contamination for their own user-defined models (which are not restricted to the linear

Thanks for listening! Questions?

Backup A: Validity of the SMEFT approach

Is the SMEFT approach valid?

 We approximated the W'-model with a linear EFT approach. This is useful because the New Physics contamination to observables is then given by linear Kfactor multiplication, allowing us to scan many more scenarios than if we used the UV model.

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- Right: For the $\hat{W} = 0.00008$ scenario, we show the SM, the UV model, and the SMEFT approximation (at linear and quadratic order) for CC DY.
- The UV model deviates from the SM implying interesting New Physics. The linear SMEFT agrees well with the UV.



Backup B: Random seed dependence

Random seed dependence

• When we generate **fake data** in this study, it is possible that the results might **depend** on the random seed that was used to make the fake data. We have **verified extensively** that this is not the case.
- When we generate fake data in this study, it is possible that the results might depend on the random seed that was used to make the fake data. We have verified extensively that this is not the case.
- At the PDF level, the choice of random seed is much less important than the strength of the New Physics that is used to generate the fake data.
- *Right:* Comparison of the CC luminosity for the three *Ŵ*-values, across **two different choices** of **random seed**.



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- We see that the distributions for the SM baseline $(\hat{W} = 0), \hat{W} = 0.00003$ and $\hat{W} = 0.00008$ are all **extremely similar**.
- On the other hand, for $\hat{W} = 0.00015$, the distribution is **skewed** to **higher** n_{σ} **s**.
- This shows that **on average**, we would not flag datasets for the lower interaction strengths, but we would for the highest interaction strength.



Backup C: The SIMUnet methodology

 The SIMUnet methodology extends the existing NNPDF neural network with an additional convolution layer.

Input layer

 $\ln x$







- The SIMUnet methodology extends the existing NNPDF **neural network** with an additional convolution layer.
- The SMEFT couplings are added as weights of neural network edges, and are trained alongside the PDFs.

Input layer

 $\ln x$





 The SIMUnet methodology allows for **a lot of flexibility**:

Input layer







 The SIMUnet methodology allows for **a lot of flexibility**:

Input layer

- Can easily include **PDF**independent observables.







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 $\ln x$

- Can easily include **PDF**independent observables.
- Can perform **fixed PDF** fits by freezing the PDF part of the network.
- The **code release** will also provides the ability to perform **contaminated fits**, like those presented in this talk.





Backup D: Pitfalls of the Monte Carlo Replica method

$$t(c) = t^{SM} + t^{lin}c + t^{quad}c^2$$

ullet

$$c_p(d_p) = \operatorname{arg\,min}_c \left(\frac{(t(c) - d_p)^2}{\sigma^2} \right)$$

For simplicity, consider a single data point d with experimental variance σ^2 , which we attempt to describe using the **quadratic** theory, involving a single theory parameter c:

The Monte-Carlo replica method propagates the uncertainty from the data to the theory parameter by fitting to **pseudodata**. We sample lots of pseudodata replicas from a normal distribution based on the data, $d_p \sim N(d, \sigma^2)$, and define the corresponding **parameter**

replicas to be a random function of the pseudodata given by minimising the χ^2 -statistic:

parameter replicas analytically; it is given by:

• In this very simple example, one can compute the distribution function of the

parameter replicas analytically; it is given by:

$$P_{c^{(i)}}(c) \propto \delta\left(c + \frac{t^{\text{lin}}}{2t^{\text{quad}}}\right) \int_{-\infty}^{t_0} dx \exp\left(-\frac{1}{2\sigma^2}(x-d)^2\right) + 2\left|2ct^{\text{quad}} + t^{\text{lin}}\right| \exp\left(-\frac{1}{2\sigma^2}(d-t(c))^2\right)$$

• Here, t_0 is the minimum value of the theory (which is a parabola).

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parameter replicas analytically; it is given by:

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• Here, t_0 is the minimum value of the theory (which is a parabola).

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 - why...?

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- There is also a **delta function spike** in the distribution - interesting to ask:



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- This gives rise to the spike in the distribution at $c = -t^{\text{lin}}/2t^{\text{quad}}$

- method (orange) and a Bayesian method with uniform prior (blue).
- We see that Monte-Carlo massively underestimates uncertainties.



• These problems extend to our top fit... for example in a realistic quadratic fit of one operator c_{dt}^8 , we get the following comparison between the Monte-Carlo